



# MD study of Poiseuille/Couette flow and the vapor-liquid interface of methane in nanochannels

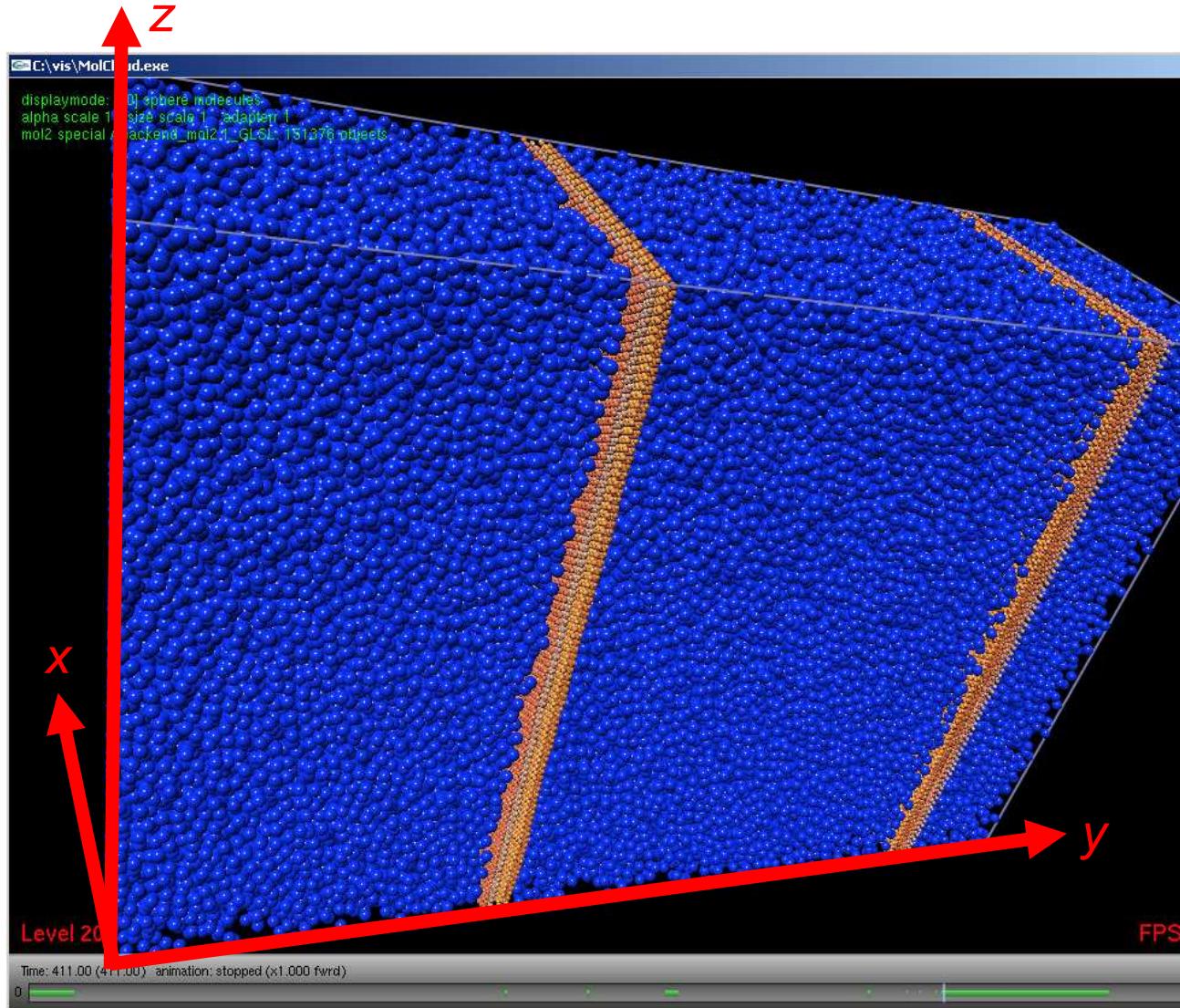


Institute for Computational Physics, Stuttgart  
**Oberseminar “Physik mit Höchstleistungsrechnern”**

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## Methane confined in a nanochannel



Poiseuille flow:

The fluid is accelerated in z direction

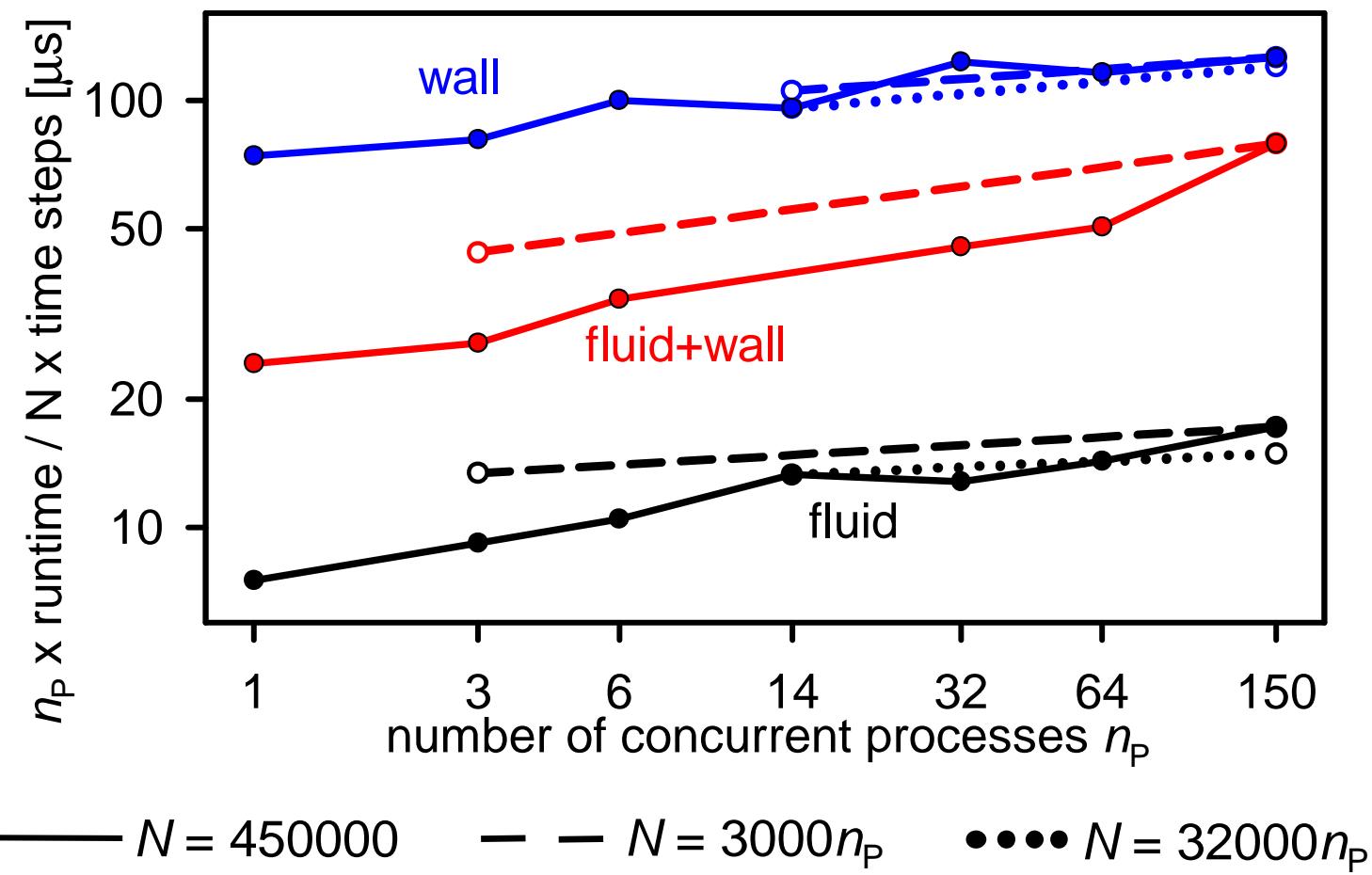
Couette flow:

The walls are accelerated in opposite z directions

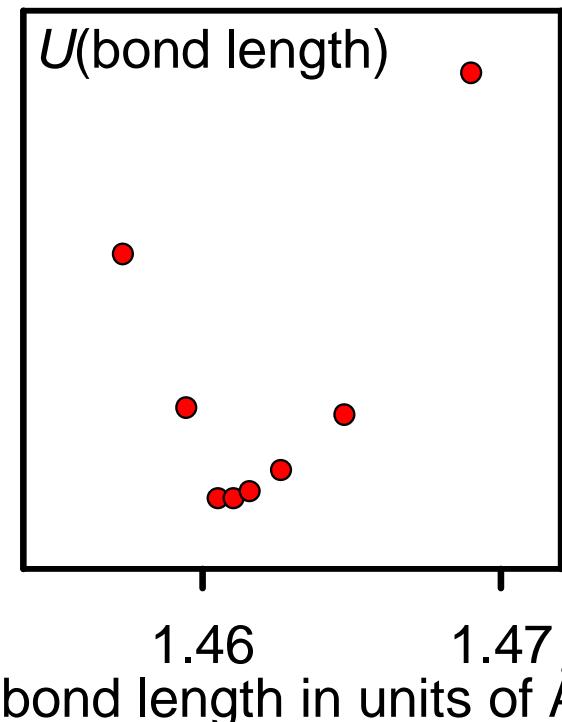
Contact angle:  
Meniscus perpendicular to the z axis

## Scaling with isotropic domain decomposition

Molecular dynamics code *Mardyn* (developed by the ls1 project):

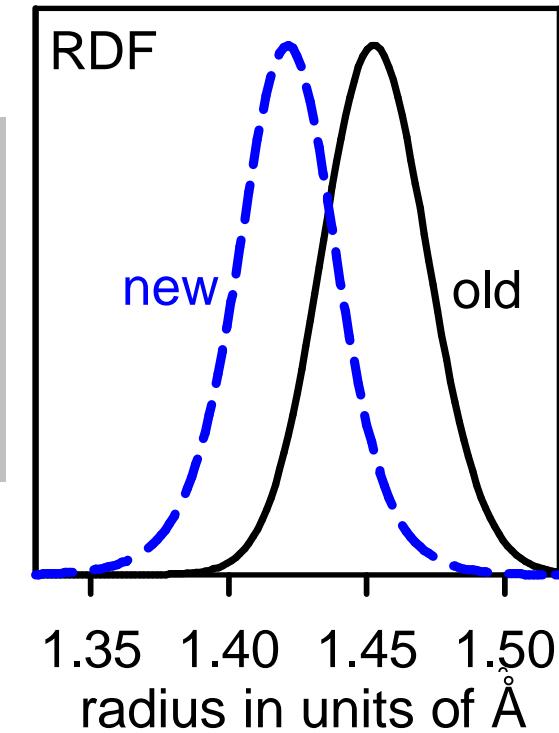


## Reparametrization of the Tersoff potential



**Bond length:**

Tersoff potential: 1.461 Å  
Actual graphite: 1.421 Å



Optimized Tersoff potential parameters for graphite:

Cutoff

$$R = 2.0 \text{ \AA} (1.8 \text{ \AA}) \\ S = 2.35 \text{ \AA} (2.1 \text{ \AA})$$

Attraction

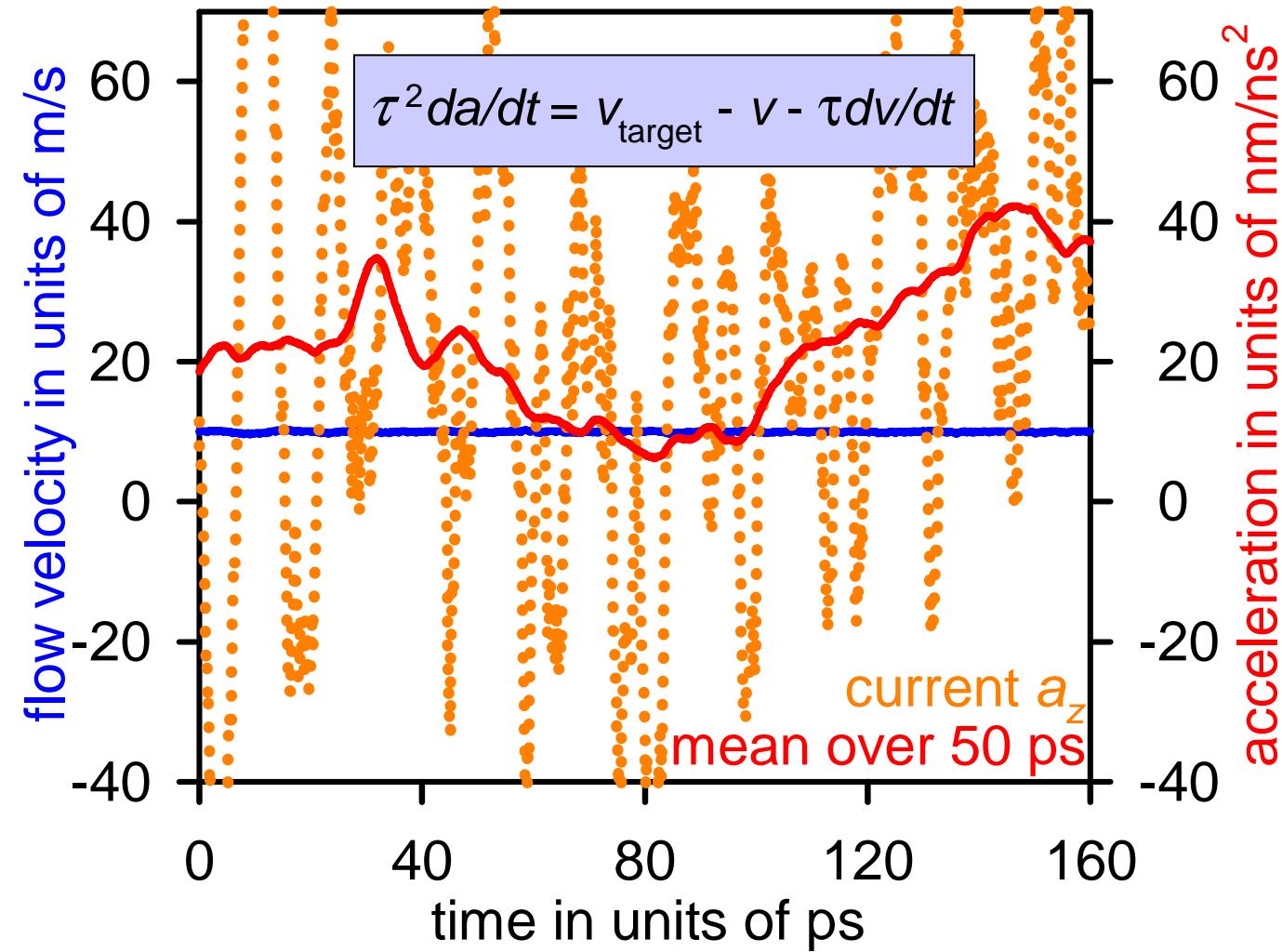
$$\mu = 2.275 \text{ \AA}^{-1} (2.2119 \text{ \AA}^{-1})$$

Repulsion

$$\lambda = 3.587 \text{ \AA}^{-1} (3.4879 \text{ \AA}^{-1})$$

## Uniform acceleration (PI controller)

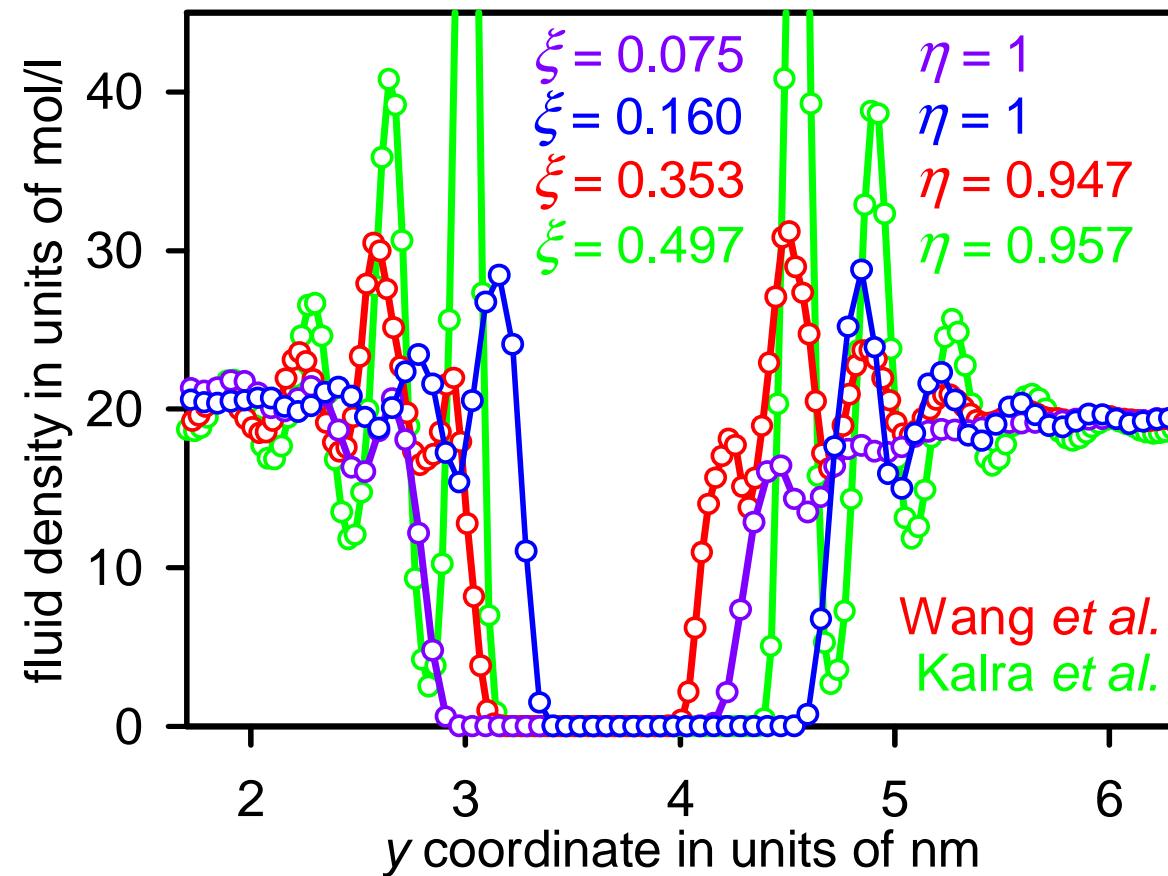
Poiseuille,  $v_{\text{target}} = 10 \text{ m/s}$ ,  $\tau = 3 \text{ ps}$ ,  $L = 15 \text{ nm}$ , liquid CH<sub>4</sub> at 166 K

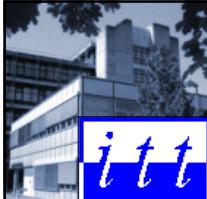


## Fluid-wall interaction

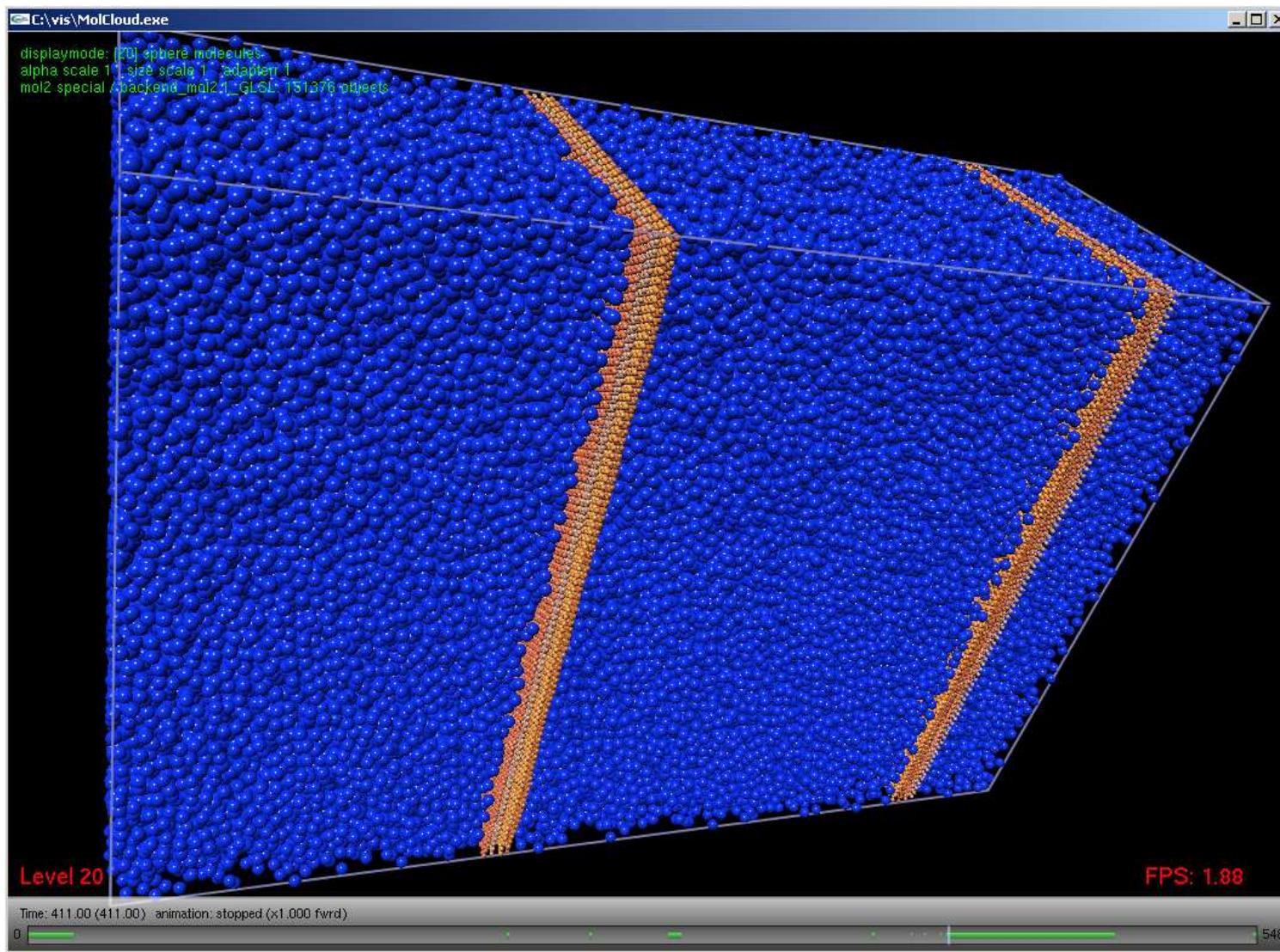
Lennard-Jones energy parameter:  $\varepsilon_{FW} = \xi \cdot \varepsilon_{FF}$

Lennard-Jones size parameter:  $\sigma_{FW} = \eta \cdot \sigma_{FF}$



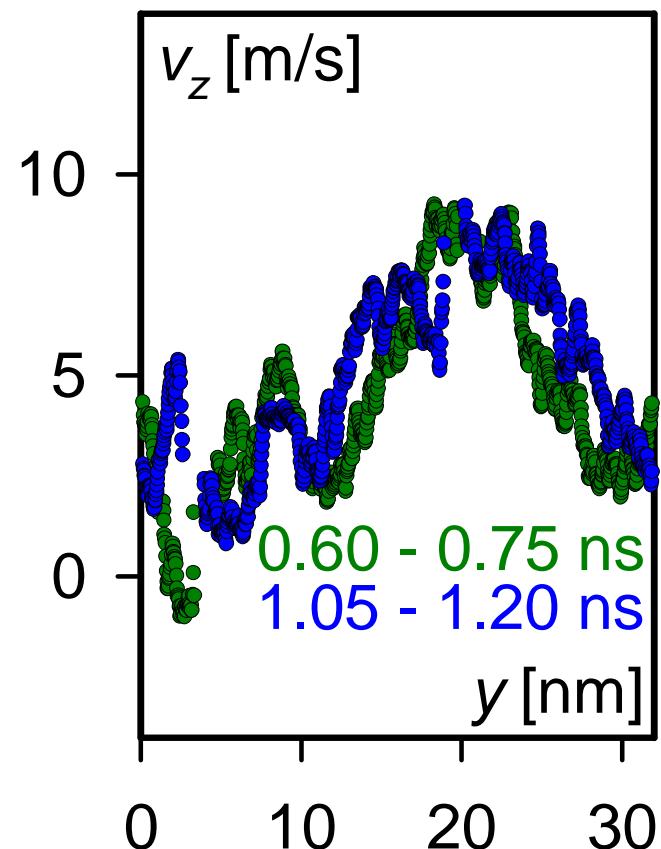


# MD simulation of Couette flow

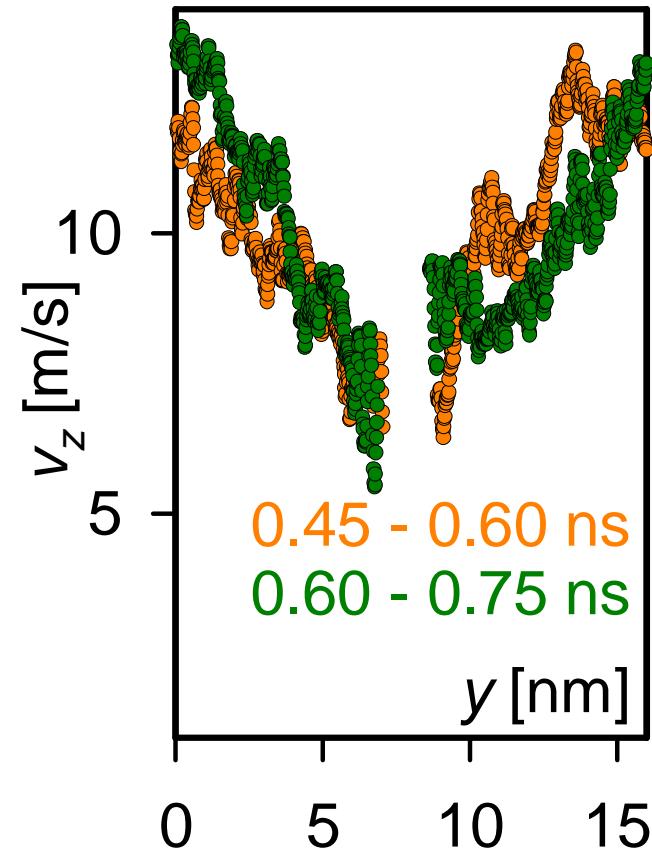


## Poiseuille and Couette flow: velocity profile

$T = 0.95 \varepsilon/k$ ,  $\rho = 1.005 \rho'$ ,  $v_{\text{target}} = 10 \text{ m/s}$ ,  $\xi = 0.353$ ,  $\eta = 0.9466$  (Wang et al.)



Couette flow



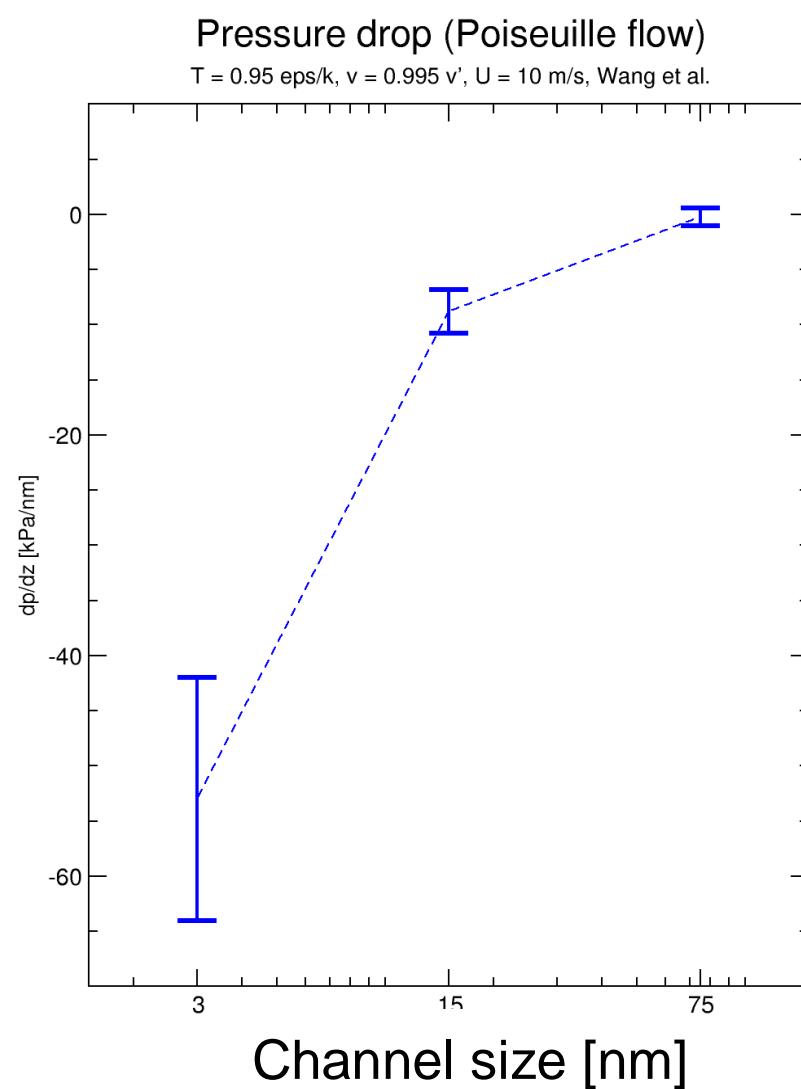
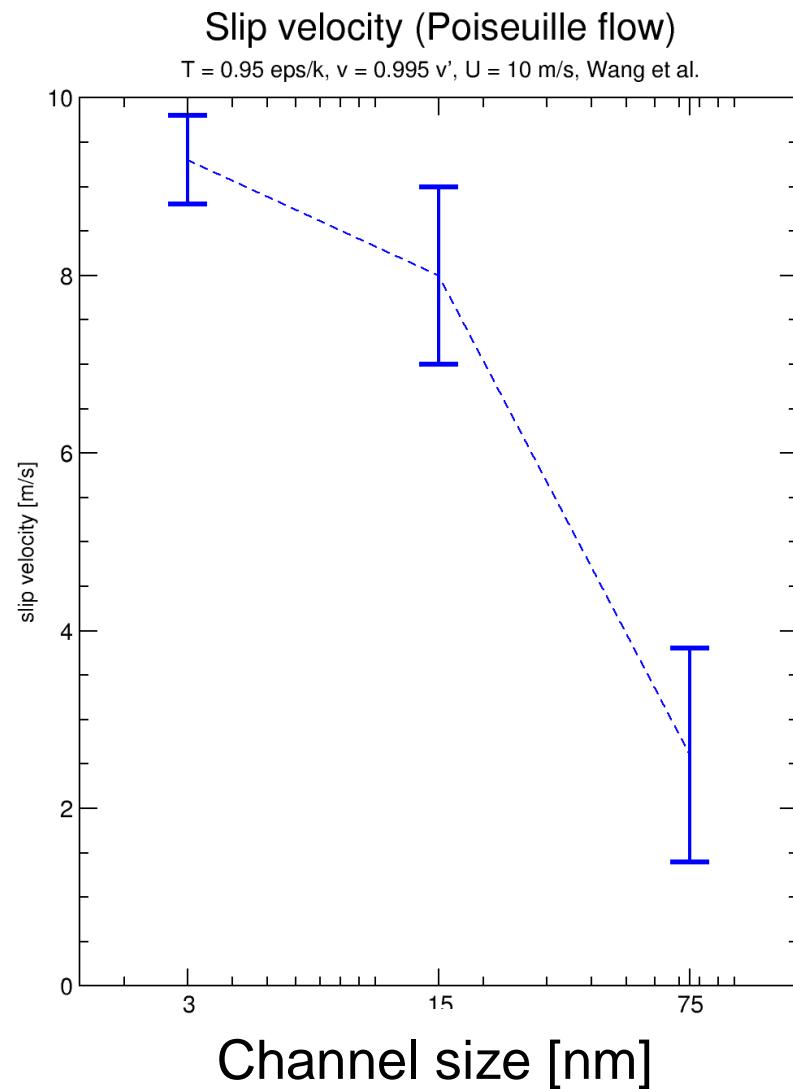
Poiseuille flow

## Poiseuille and Couette flow: viscosity

$T = 0.95 \varepsilon/k$ ,  $\rho = 1.005 \rho'$ ,  $v_{\text{target}} = 10 \text{ m/s}$ ,  $\xi = 0.353$ ,  $\eta = 0.9466$  (Wang et al.)

Couette flow	Poiseuille flow
Slip velocity	Slip velocity
$v_s = 2 \text{ m/s}$	$v_s = 8 \text{ m/s}$
Shear stress	Pressure drop
$\tau = 200 \text{ kPa}$	$dp/dz = -9 \text{ kPa/nm}$
Kinematic viscosity	Kinematic viscosity
$\nu = 1 \cdot 10^{-6} \text{ m}^2/\text{s}$	$\nu = 2 \cdot 10^{-7} \text{ m}^2/\text{s}$
Reynolds number	Reynolds number
$0.08 < \text{Re} < 0.6$	$0.6 < \text{Re} < 1.0$

# Dependence of flow properties on the channel size



## Disperse systems: cluster criteria

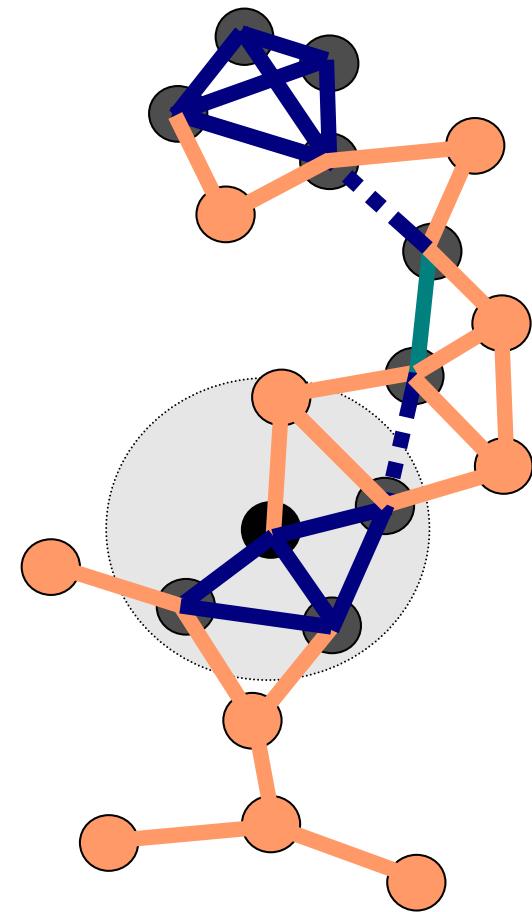
**Stillinger**: molecules with a distance of  $1.5\sigma$  or less are liquid.

**Ten Wolde and Frenkel** (TWF): molecules with at least four neighbors within a distance of  $1.5\sigma$  are liquid.

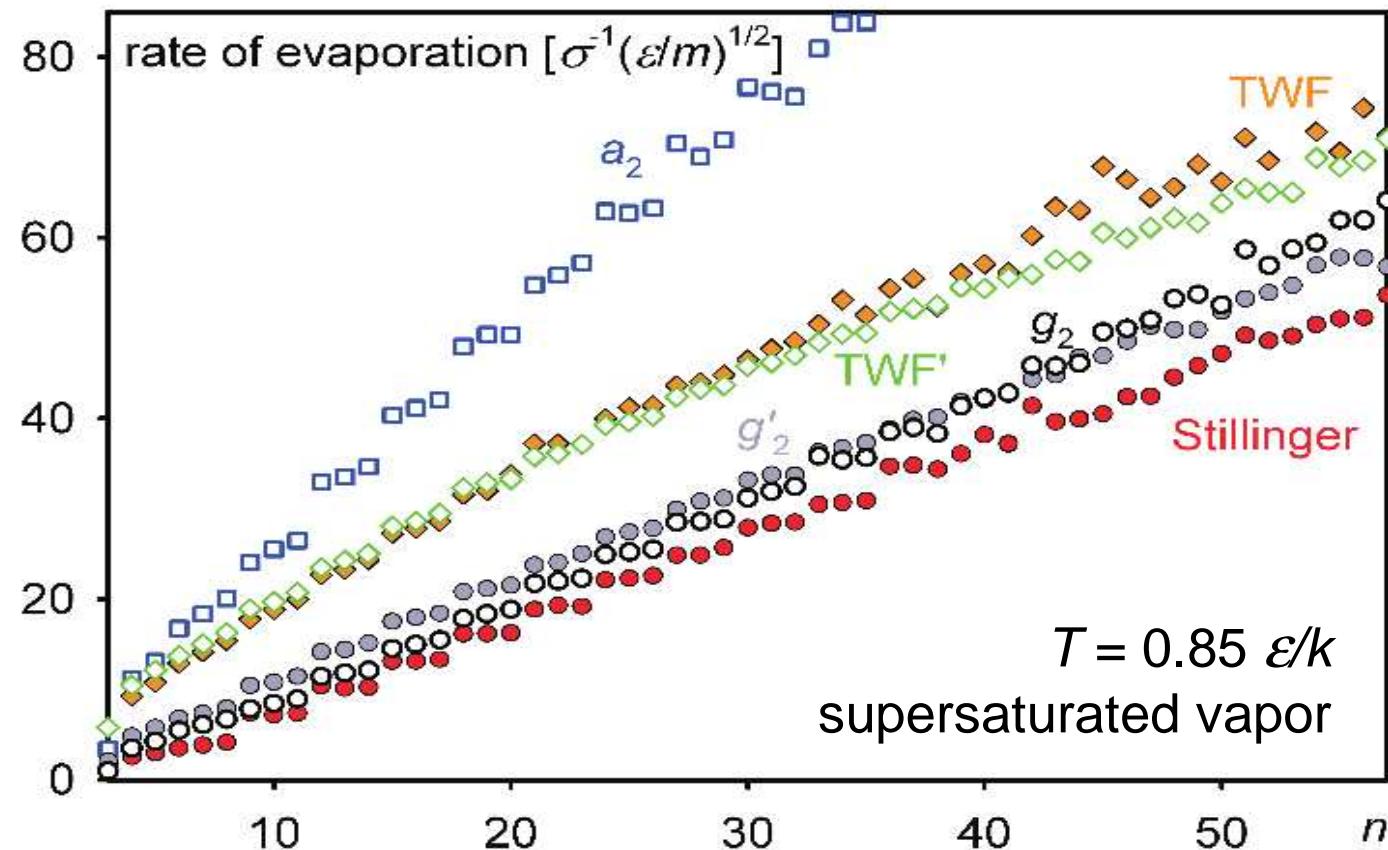
**Arithmetic mean**,  $n$  neighbors ( $a_n$ ): a molecule is liquid if the density in the sphere containing its  $n$  nearest neighbors exceeds  $(\rho' + \rho'')/2$ .

**Geometric mean**,  $n$  neighbors ( $g_n$ ): analogous, the required density is  $(\rho' \rho'')^{1/2}$ .

Nuclei can also be determined as **biconnected** (instead of connected) components, such that no nucleus can be separated by removing a single molecule (TWF' and  $g'_2$  criteria).

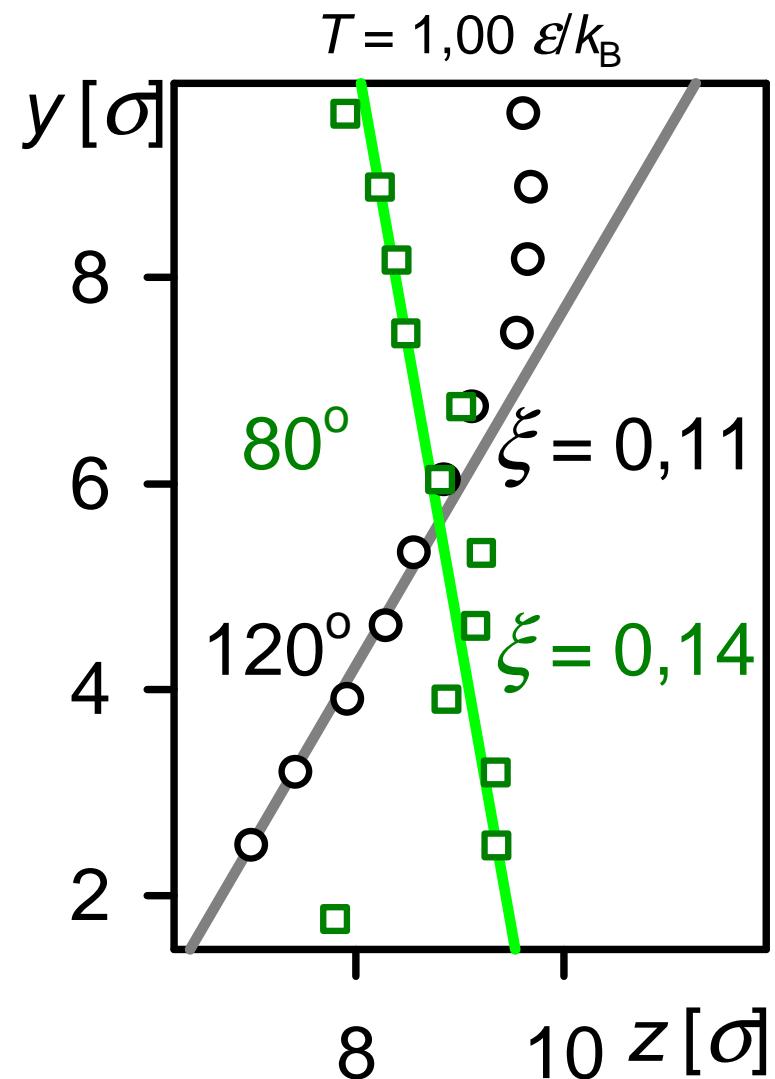
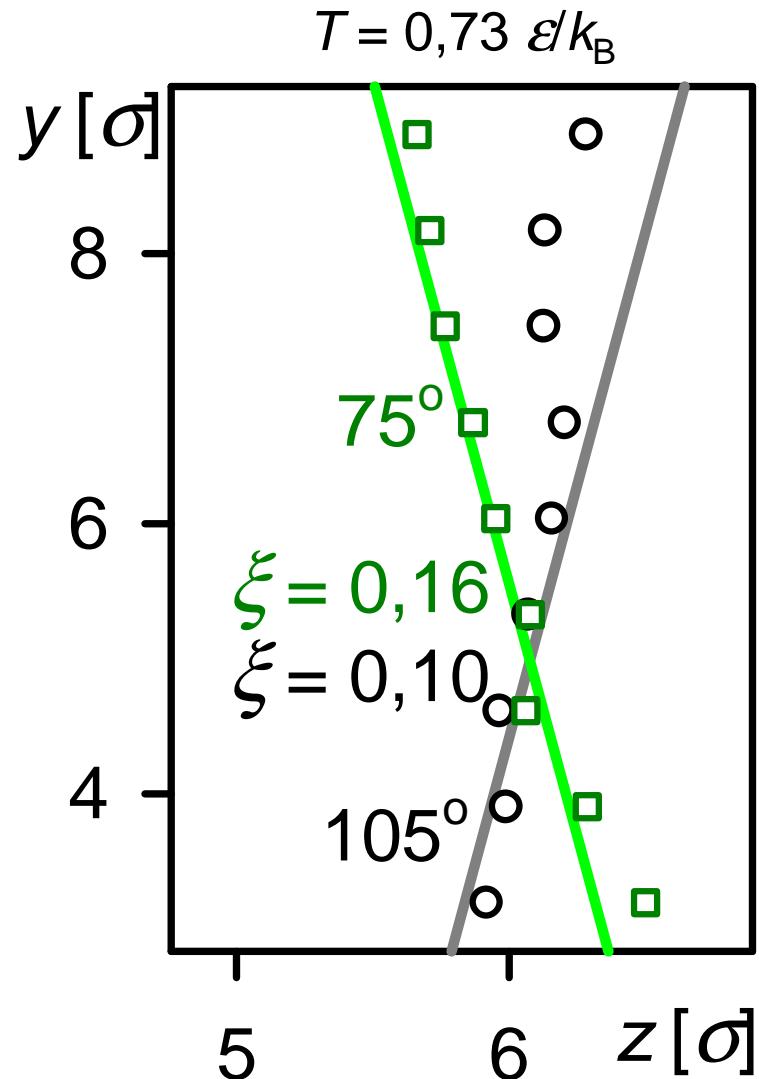


## Comparison of cluster criteria

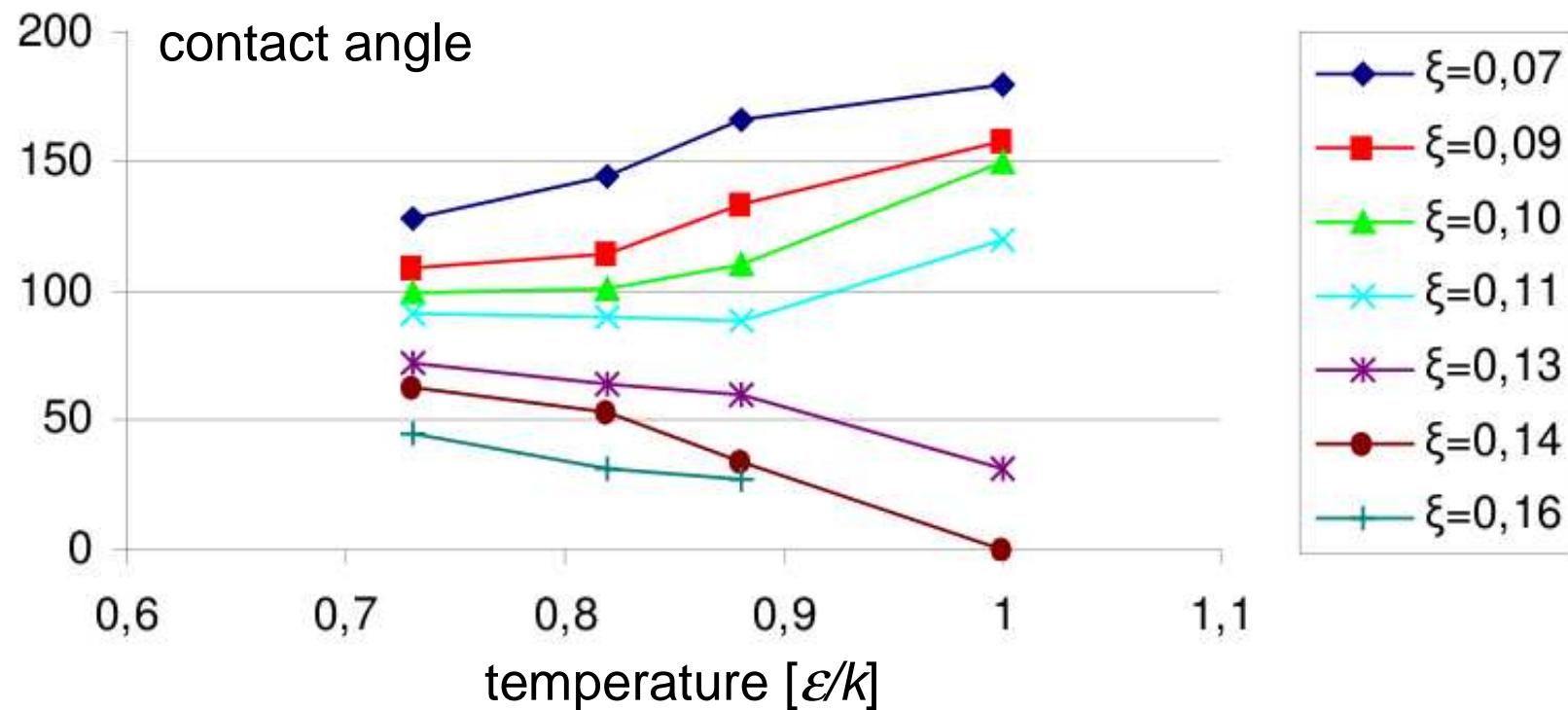


Fluctuation in equilibrium:  $7.0 \cdot 10^{-4}$  (Stillinger),  $7.4 \cdot 10^{-4}$  ( $g_2$ ),  $3.6 \cdot 10^{-4}$  ( $g'_2$ )

## Dependence of the contact angle on $\xi$



## Dependence of the contact angle on $T$ and $\xi$



Simulation results for the LJTS fluid can be correlated as

$$\cos \theta(T^*, \xi) = \tanh[\exp(6.25 T^*)(0.156 \xi - 0.0170)].$$

## Conclusion

System size: acceptable scaling of *Mardyn*,  $L$  up to 75 nm easily possible  
the system geometry requires (static) load balancing

Flow simulations: were carried out in the canonical ensemble  
unknown interaction parameters  $\xi$  and  $\eta$

Vapor-liquid interface: dependence of the contact angle on  $\xi$  and  $T$   
suitable criterion for the interface:  $\rho = (\rho' \rho'')^{1/2}$