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# Molecular simulation of aqueous and non-aqueous electrolyte solutions

M. T. Horsch,<sup>1</sup> S. Reiser,<sup>1</sup> S. Deublein,<sup>1</sup> J. Vrabec,<sup>2</sup> and H. Hasse<sup>1</sup>

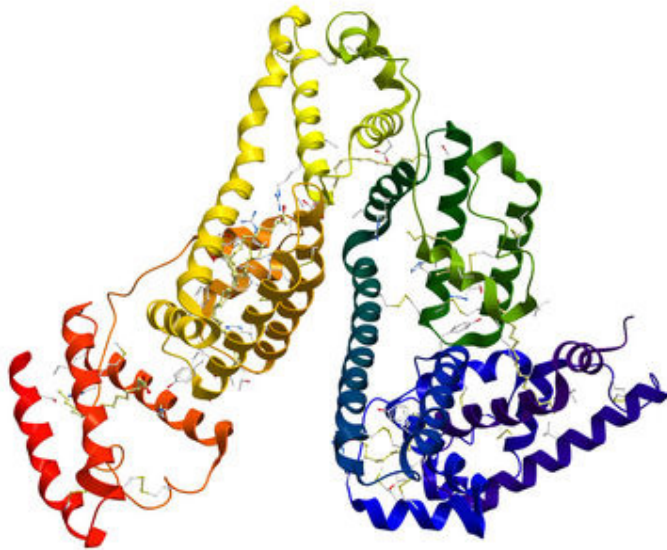
<sup>1</sup> Laboratory of Engineering Thermodynamics, University of Kaiserslautern, Germany

<sup>2</sup> Thermodynamics and Energy Technology, University of Paderborn, Germany



**Computational  
Molecular Engineering**

# Electrolyte Solutions – Applications



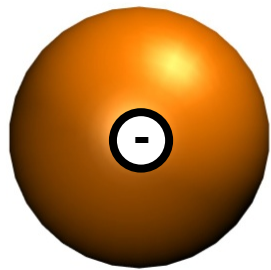
Buffer solutions in pharmaceutical  
and biochemical industry /  
purification of proteins

Electrochemistry /  
energy storages

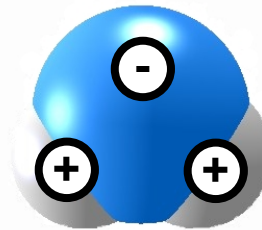


# Simulation of aqueous electrolyte solution

## Molecular models:



Ions  
1 CLJ  
1 point charge



Water  
1 CLJ  
3 partial charges

## Literature models:

- Scattering of model parameters

Parameters  $\text{Na}^+$  :

$$1.9 < \sigma_{\text{Na}^+} / \text{\AA} < 4.1$$

$$0.06 < \epsilon_{\text{Na}^+} / \text{K} < 1068.8$$

## Reference property:

- Density  $\rho$

⇒ Large deviation from experiments

# Parameter optimization for alkali halides

## Adjustable parameters:

- Ions: 1 CLJ with 1 point charge ( $\pm 1e$ ) – 2 parameters

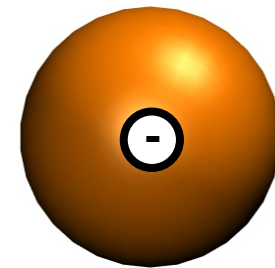
## Target:

- Reduced density for varying salinity at  $T = 293$  K,  $p = 1$  bar

$$\tilde{\rho} = \frac{\rho_{\text{Electrolyte solution}}}{\rho_{\text{Solvent}}} = \tilde{\rho}(\sigma_+, \sigma_-, \varepsilon_+, \varepsilon_-, x_{\pm})$$

## Simulation conditions:

- Monte Carlo simulation
- SPC/E water model
- Simulation code: extended version of *ms2*\*



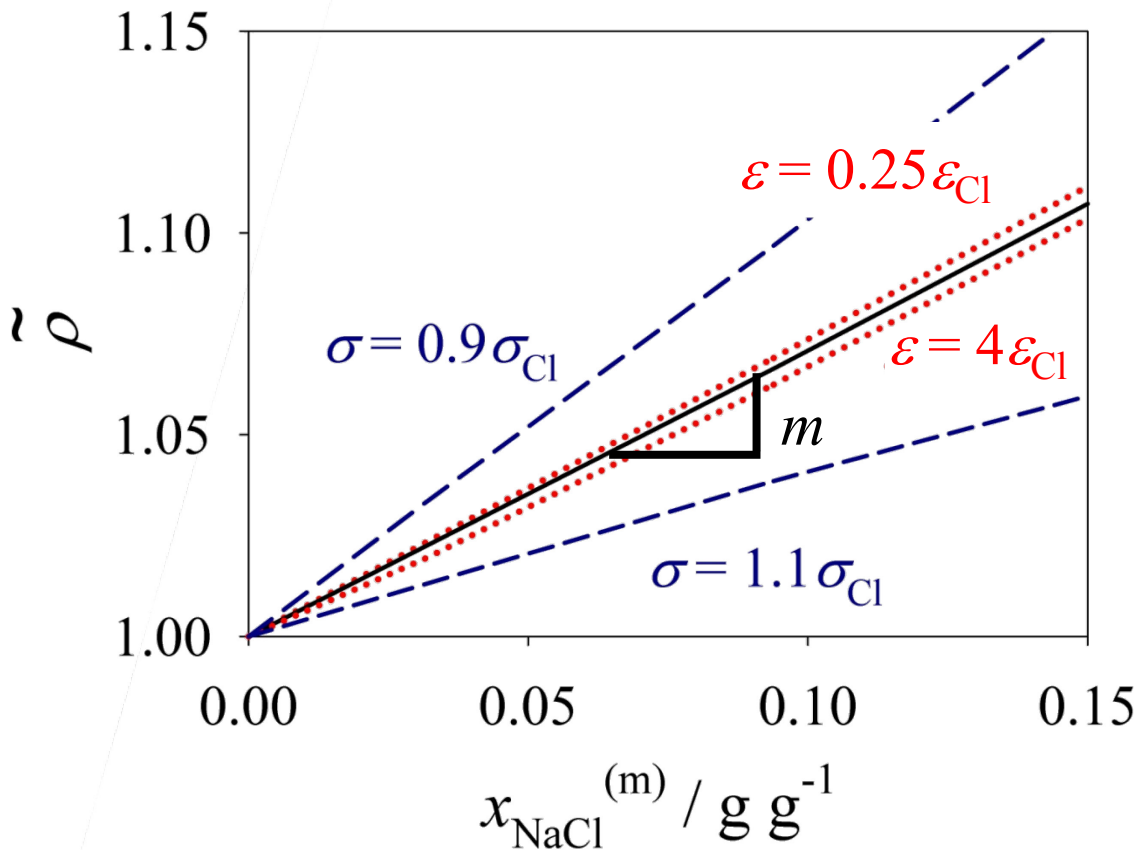
$\sigma_{\text{Ion}}, \varepsilon_{\text{Ion}}$

\*Deublein et al., Computer Physics Communications (2011), 182, 2350 – 2367; <http://www.ms-2.de>



# Target: Slope of the reduced density over the salt mass fraction

Reduced density of NaCl solutions ( $T = 298 \text{ K}$ ,  $p = 1 \text{ bar}$ )



Sensitivity study of  $\tilde{\rho}^{\text{Sim}}$ :

- $\sigma_{\text{lon}}$  dominant
- $\varepsilon_{\text{lon}}$  negligible

$$\tilde{\rho}^{\text{Sim}} = \tilde{\rho}^{\text{Sim}}(\sigma_+, \sigma_-, x_{\pm})$$

Adjustment:

$$m = \frac{d\tilde{\rho}^{\text{Sim}}}{dx^{(m)}} = \frac{d\tilde{\rho}^{\text{Sim}}}{dx^{(m)}}(\sigma_+, \sigma_-)$$

# Parameter optimization for alkali halides

## Electrolyte systems:

5 cations:  $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Rb}^+$ ,  $\text{Cs}^+$  } 20 salts modeled by  
 4 anions:  $\text{F}^-$ ,  $\text{Cl}^-$ ,  $\text{Br}^-$ ,  $\text{I}^-$  } 9 parameter

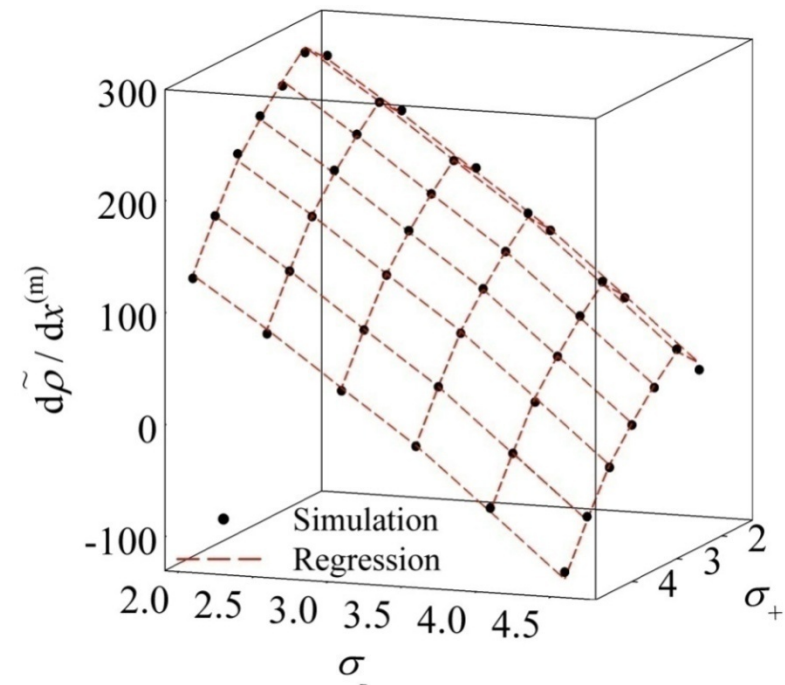
## Size adjustment:

- Global fit

$$\sigma_+ [1.5; 4.5] \text{ \AA}$$

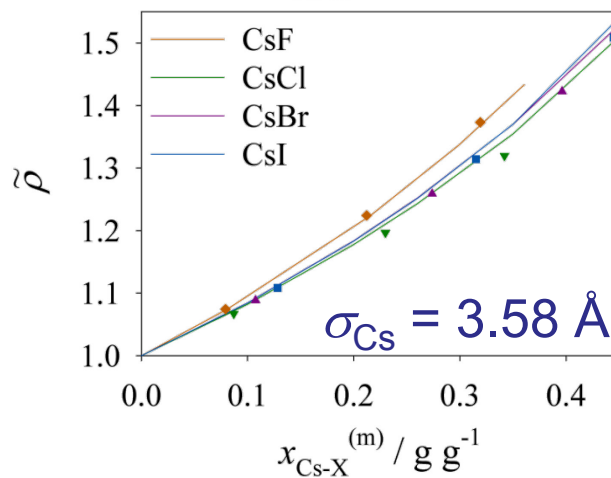
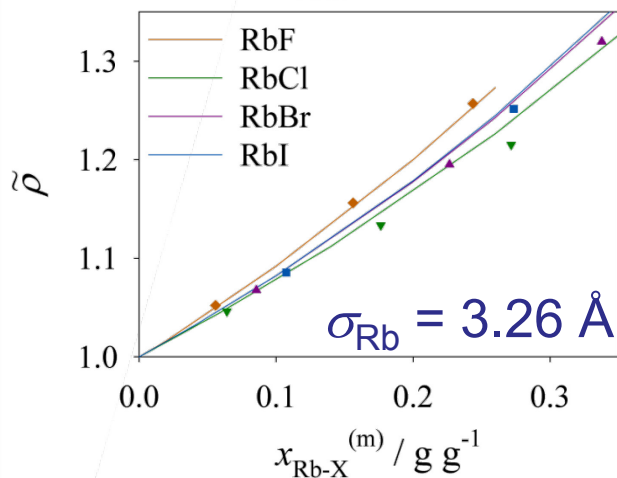
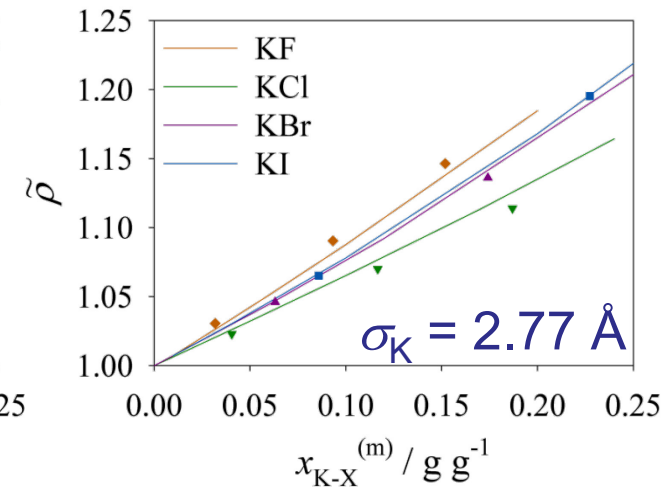
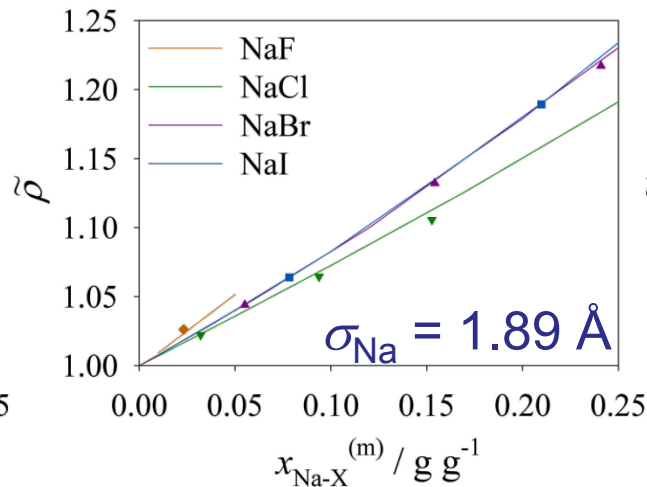
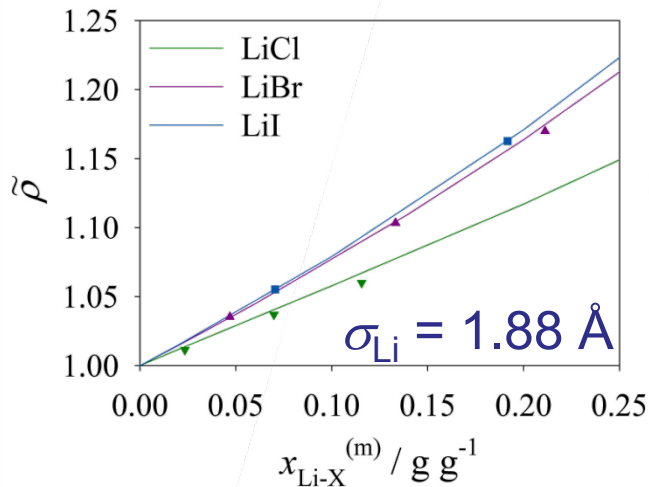
$$\sigma_- [2.0; 4.5] \text{ \AA}$$

$$\frac{d\tilde{\rho}^{\text{Exp}}}{dx^{(\text{m})}} \stackrel{!}{=} \frac{d\tilde{\rho}^{\text{Sim}}}{dx^{(\text{m})}} (\sigma_+, \sigma_-)$$



# Aqueous electrolyte solutions

Reduced density ( $T = 293 \text{ K}$ ,  $p = 1 \text{ bar}$ )



## Anions

$$\sigma_{\text{F}} = 3.66 \text{ \AA}$$

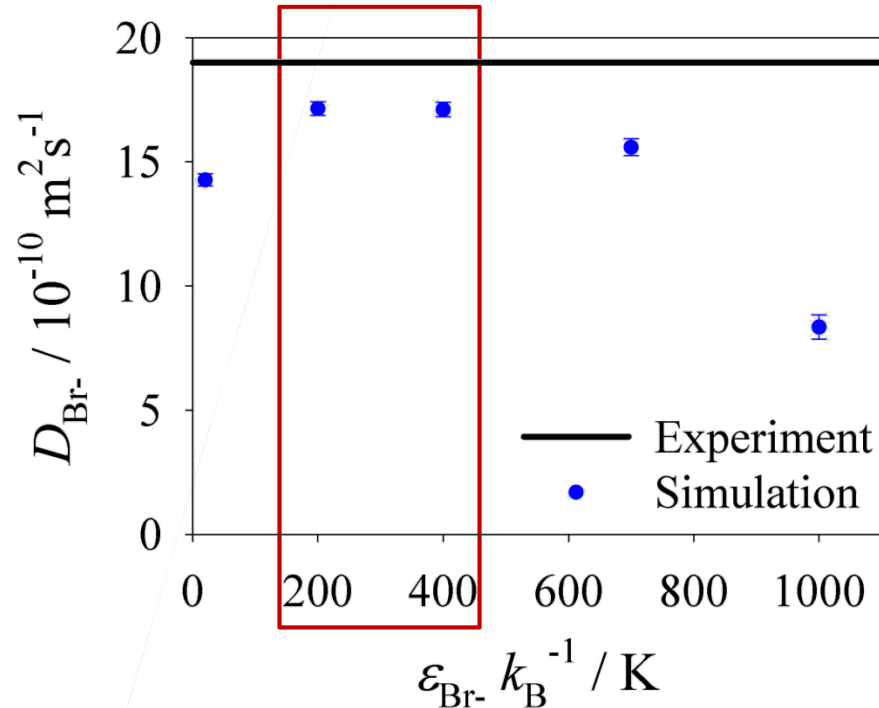
$$\sigma_{\text{Cl}} = 4.41 \text{ \AA}$$

$$\sigma_{\text{Br}} = 4.54 \text{ \AA}$$

$$\sigma_{\text{I}} = 4.78 \text{ \AA}$$

# Self-diffusion coefficient of ions in aqueous solution (Example bromide)

Adjustment of the LJ energy parameters  $\varepsilon_{\text{ion}}$  to the self-diffusion coefficient in solution ( $T = 298 \text{ K}$ ,  $p = 1 \text{ bar}$ )

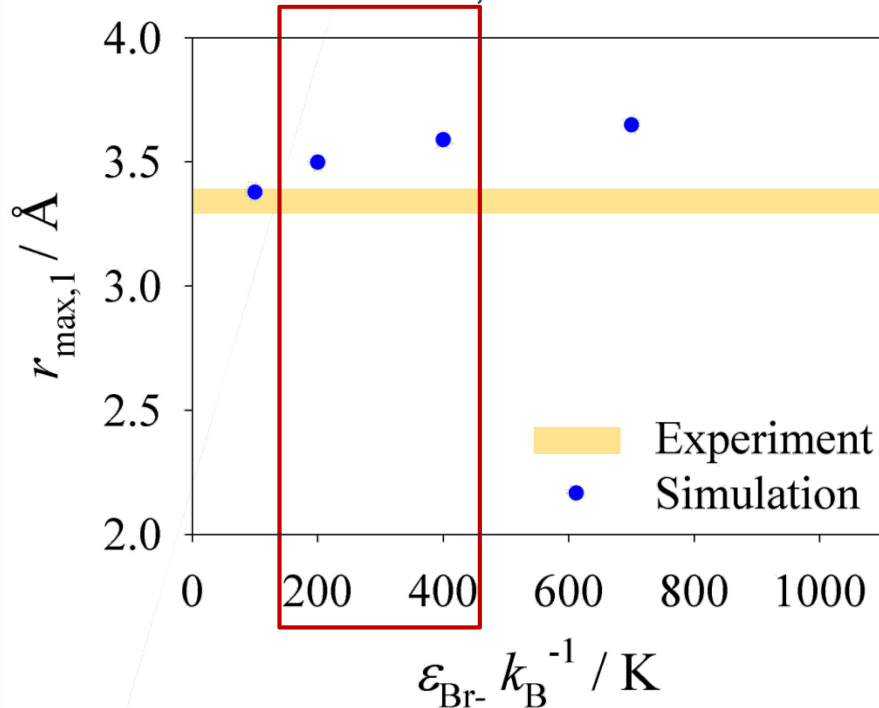


- Reasonable parameter range:  
 $200 \text{ K} \leq \varepsilon_{\text{Br}^-} \leq 400 \text{ K}$
- Similar dependence of  $D_i$  on  $\varepsilon_i$  for all alkali and halide ions

Water model: SPC/E

# Radial distribution function of water around the ions (Example bromide)

Adjustment of the LJ energy parameters  $\varepsilon_{\text{ion}}$  to the first maximum  $r_{\text{max},1}$  in the RDF ( $T = 293 \text{ K}$ ,  $p = 1 \text{ bar}$ )



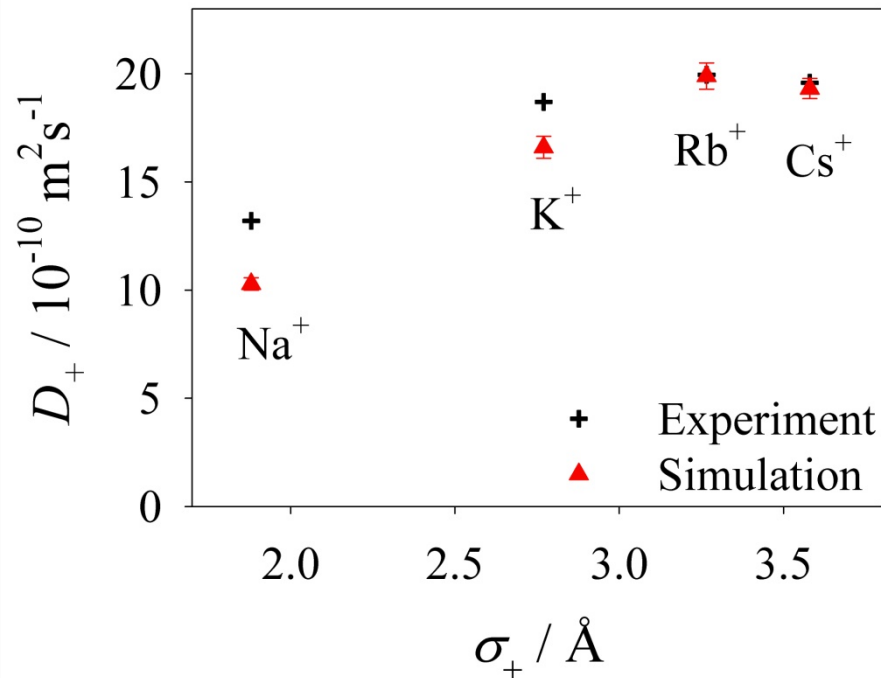
- Reasonable match:  
 $\varepsilon_{\text{Br}^-} = 200 \text{ K}$
- Best choice:  
 $\varepsilon_+ = \varepsilon_- = 200 \text{ K}$

Water model: SPC/E

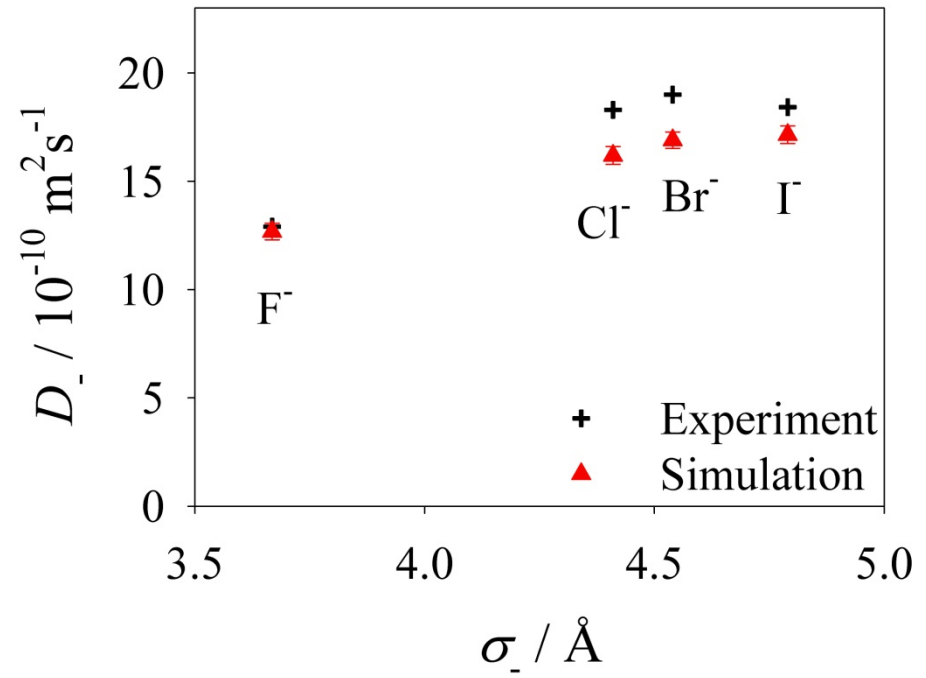
# Self-diffusion coefficient of alkali cations and halide anions in aqueous solution

Comparison with experimental data ( $T = 298 \text{ K}$ ,  $p = 1 \text{ bar}$ )

Cations



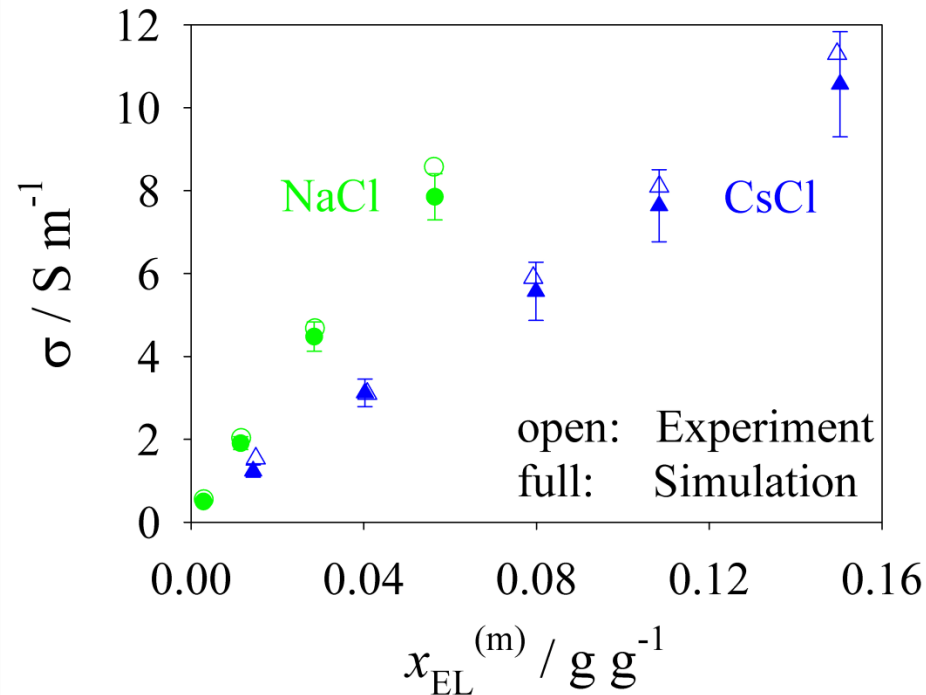
Anions



Water model: SPC/E

# Electric conductivity of NaCl and CsCl in aqueous solutions at various salinities

Predictions ( $T = 298 \text{ K}$ ,  $p = 1 \text{ bar}$ )



Electric conductivity:

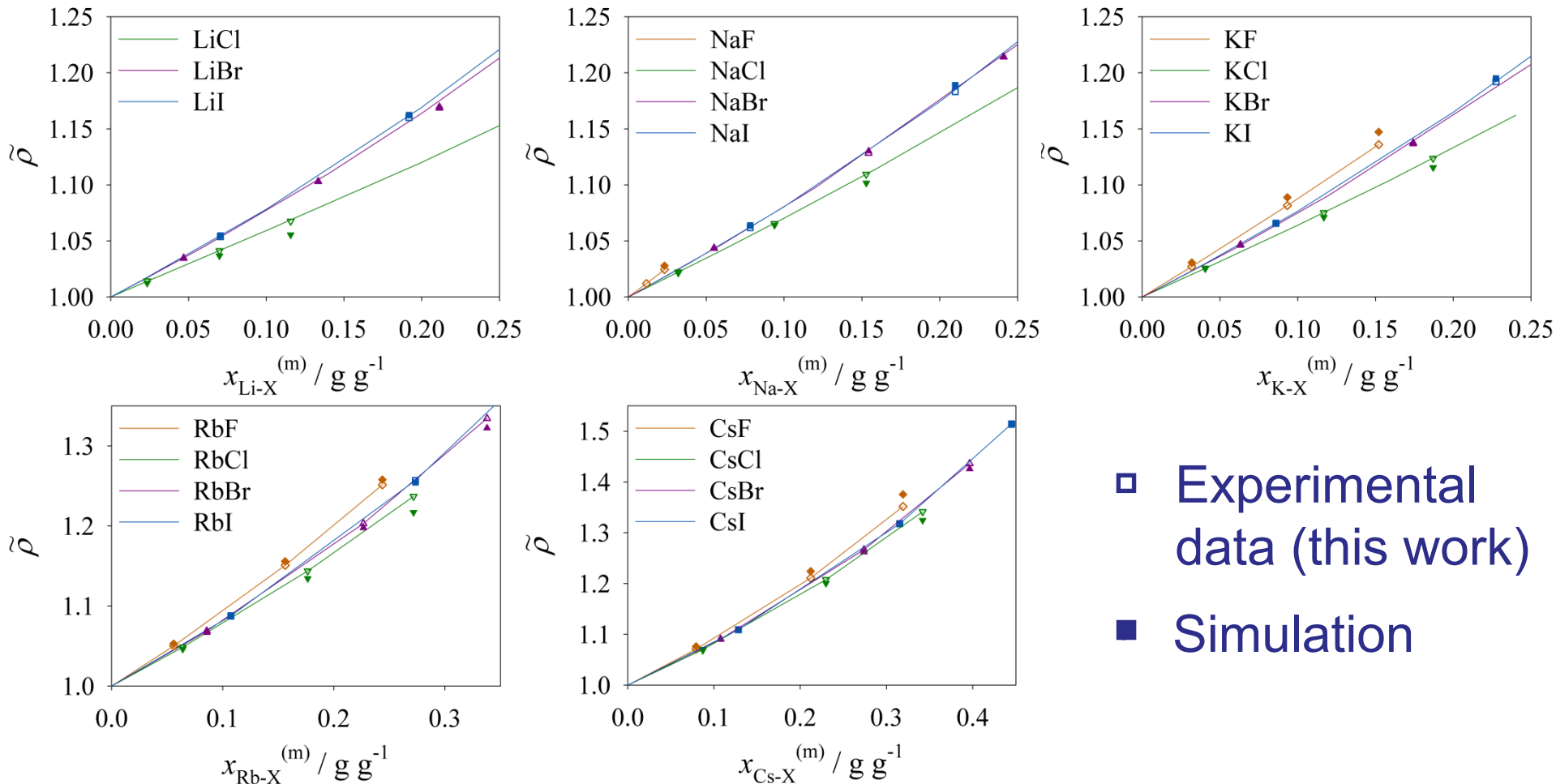
- Correlated motion of the ions in solution

Water model: SPC/E



# Temperature dependence of the density

Predictions for aqueous solution ( $T = 333 \text{ K}$ ,  $p = 1 \text{ bar}$ )

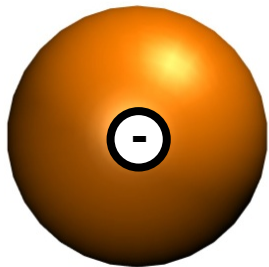


- Experimental data (this work)
- Simulation

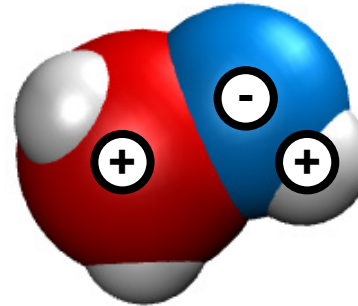


# Simulation of non-aqueous electrolyte solutions: solvent methanol

## Molecular models:



Ions  
1 CLJ  
1 point charge



Methanol  
2 CLJ  
3 partial charges

## Reference property:

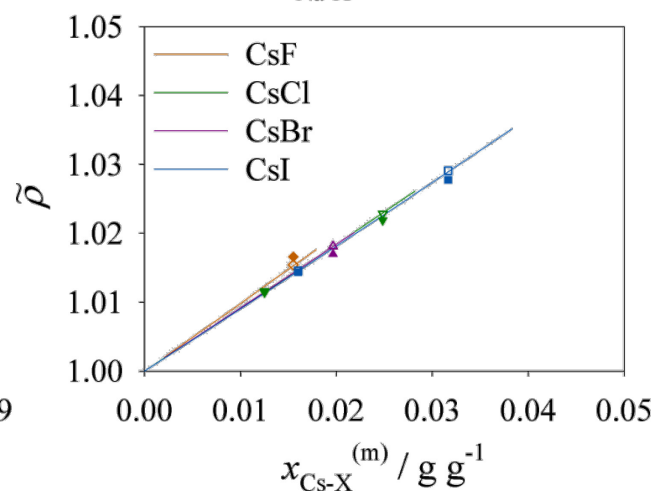
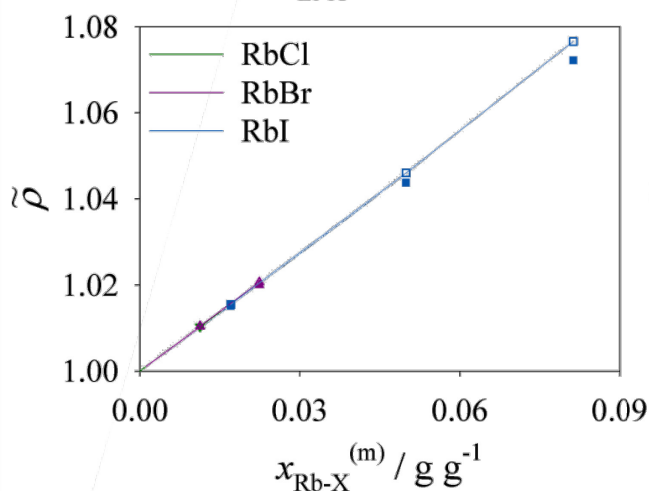
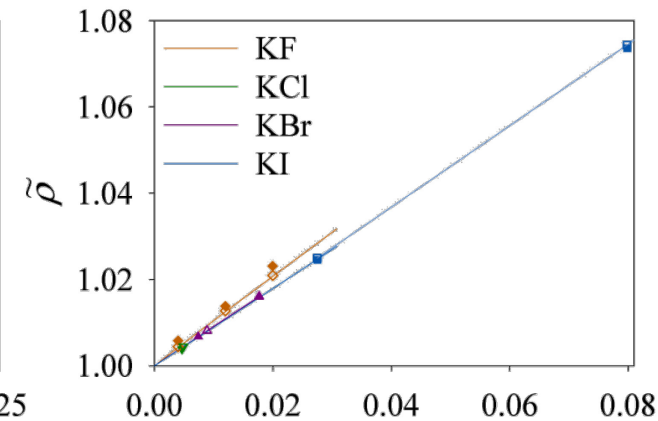
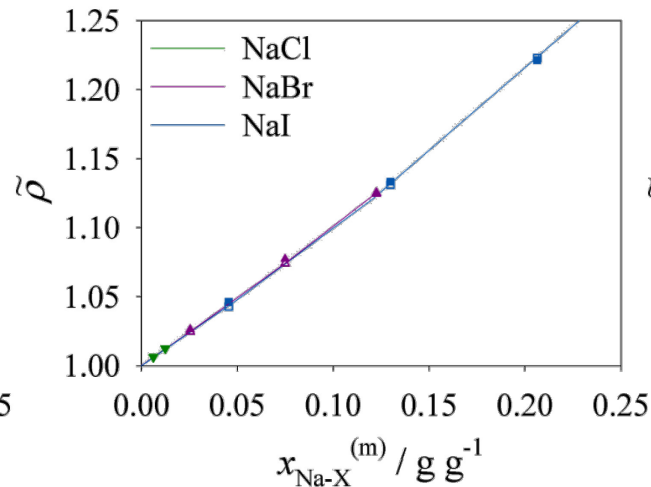
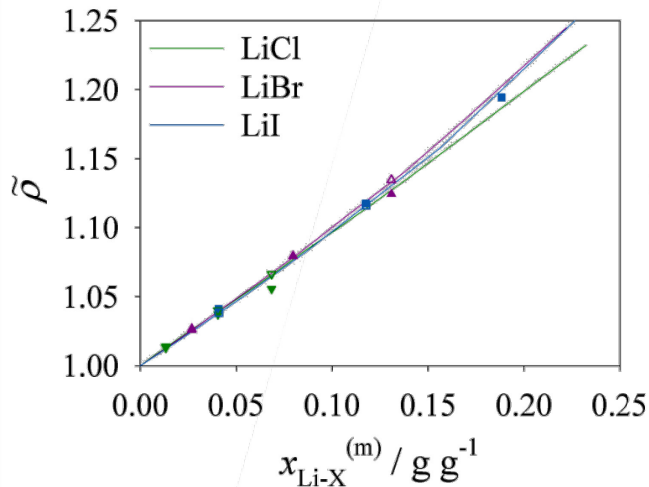
- Reduced density  $\tilde{\rho} = \frac{\rho_{\text{Electrolyt solution}}}{\rho_{\text{Solvent}}}$

## Simulation:

- MC simulations at  $T = 298$  K,  $p = 1$  bar

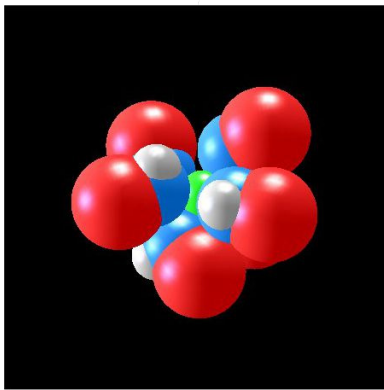
# Methanolic electrolyte solutions

Predictions ( $T = 298 \text{ K}$ ,  $p = 1 \text{ bar}$ )

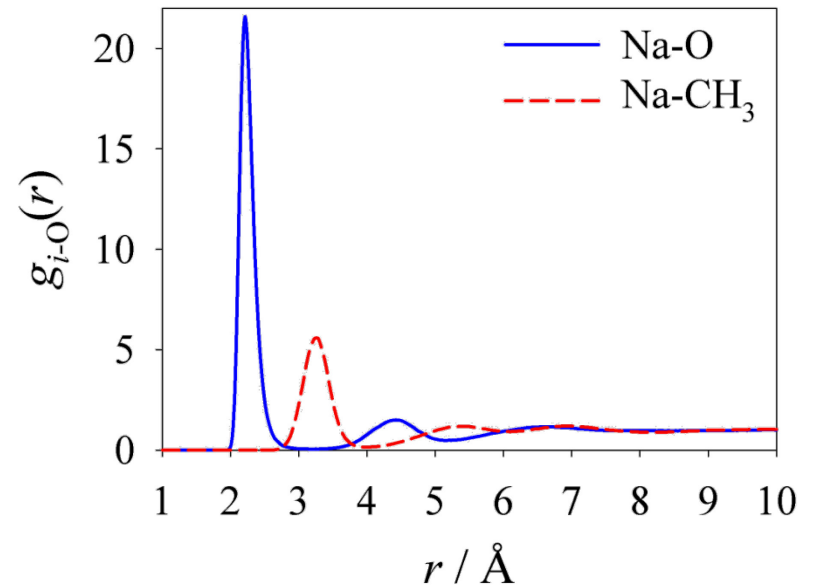


# Radial distribution function of methanol

Diluted methanolic NaCl solution ( $T = 298$  K,  $p = 1$  bar)



Na<sup>+</sup>



	$r_{1. \text{Max}} / \text{Å}$		$r_{1. \text{Min}} / \text{Å}$	
	Methanol	Water	Methanol	Water
Na – O	2.21	2.23	3.17	3.07

# Summary

- ✓ New atomistic force fields for ions
  - ✓ Alkali-cations:  $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Rb}^+$ ,  $\text{Cs}^+$
  - ✓ Halide-anions:  $\text{F}^-$ ,  $\text{Cl}^-$ ,  $\text{Br}^-$ ,  $\text{I}^-$
- ✓ Model adjustment in aqueous systems
  - ✓ Reduced density
  - ✓ Self-diffusion coefficient and RDF
- ✓ Predictions
  - ✓ Electric conductivity
  - ✓ Temperature dependence of the reduced density
  - ✓ Reduced density of methanolic solutions