



# Multicriteria optimization of molecular force field models

Martin Horsch,<sup>1</sup> Katrin Stöbener,<sup>1, 2</sup> Stephan Werth,<sup>1</sup> and Hans Hasse<sup>1</sup>

<sup>1</sup>Laboratory of Engineering Thermodynamics, University of Kaiserslautern <sup>2</sup>Fraunhofer Institute for Industrial Mathematics, Kaiserslautern



Leipzig, 27<sup>th</sup> November 2015 NTZ CompPhys15 Workshop Computational Molecular Engineering





### **Computational molecular engineering**



## From Physics (qualitative accuracy)

- Physically realistic modelling of intermolecular interactions
- Separate contributions due to repulsive and dispersive as well as electrostatic interactions

#### To Engineering (quantitative reliability)

- No blind fitting, but parameters of *effective pair potentials* are adjusted to experimental data
- Physical realism facilitates reliable interpolation and extrapolation





### Vapour-liquid equilibria

#### **Bulk properties**



vapour pressure, saturated densities, composition, enthalpy of vaporization, etc., by Grand Equilibrium simulation

#### **Interfacial properties**



heterogeneous systems with finite-size effects and long-range interactions



### **Long-range correction at planar interfaces**



Full evaluation of all pairwise interactions is too expensive ... **short-range interactions** are evaluated only for **neighbours**.

27th November 2015

Martin Horsch, Katrin Stöbener, Stephan Werth, and Hans Hasse



### Long-range correction at planar interfaces

#### For planar interfaces:

Long-range correction from the density profile, following Janeček.



**Angle-averaging** expression for multi-site models, following **Lustig**.

Two-centre LJ fluid (2CLJ)



Dipole and dispersion lead to analogous long-range correction expressions. The long-range contribution of the quadrupole can be neglected.



#### Validation of molecular force field models



2CLJQ models:

- 2 LJ centres
- Quadrupole

Fit of parameters  $\sigma$ ,  $\varepsilon$ , L, Q to VLE data of 29 fluids by Stoll et al.

Deviation:

 $\cdot \delta \rho' \approx 1\%$  $\cdot \delta P^{\text{sat}} \approx 5\%$ 

inverse temperature [1/K]

6



### Validation of molecular force field models





### Massively parallel molecular modelling





#### Model parameters:

- LJ size parameter  $\sigma$
- LJ energy parameter  $\varepsilon$
- Elongation L
- Quadrupole moment Q

• Systematic exploration of the four-dimensional model parameter space



### **Massively parallel molecular modelling**



- Systematic exploration of the four-dimensional model parameter space
- Correlation of the surface tension by a critical scaling expression

27th November 2015

Martin Horsch, Katrin Stöbener, Stephan Werth, and Hans Hasse



### **Multicriteria model optimization**



Multicriteria optimization requires massively parallel molecular modelling.





### **Computation of the Pareto set**

#### **Multicriteria optimization problem**

Simultaneously minimized objective functions  $f_{\xi}$  with  $\xi \in \{\rho', \rho^s, \gamma\}$  given by

$$f_{\xi} = \langle \delta \xi^{2} \rangle_{0.55T_{c}^{\exp} < T < 0.95T_{c}^{\exp}} = \lim_{N \to \infty} \frac{1}{N+1} \sum_{i=0}^{N} \left( 1 - \frac{\xi^{sim}(T)}{\xi^{exp}(T)} \right)_{T/T_{c} = 0.55+0.4i/N}^{2}$$
(here:  $N = 9$ ).

#### Sandwiching

Alternating construction of inner (reachable) and outer (unreachable) approximations, assuming *local convexity* of the Pareto set.

#### Hyperboxing

In non-convex regions ("hyperboxes"), Pascoletti-Serafini scalarization is employed to obtain a suitable local single-criterion optimization problem.

27th November 2015



#### **Invariants of Pareto-optimal models**



For obtaining a rough approximation of the Pareto set, the dimension of the parameter space can be reduced from four to three (or even two).



### Pareto sets for 2CLJQ models of real fluids

Representation of objective and parameter spaces by **patch plots**:



#### Pareto-optimal 2CLJQ models of molecular oxygen







### Model tailoring by the end user

For each specific application, accuracy requirements can be specified:



Restrictions imposed on 2CLJ models of molecular oxygen







### Model tailoring by the end user

Intersection of the highlighted areas within all replicas of the patch plot:



2CLJ models of molecular oxygen fulfilling all requirements







### Summary

#### The traditional art of molecular modelling

An expert modelling artist designs and publishes

- a single optimized model for a particular fluid,
- according to his choice of criteria (often unknown to the public),
- users are passive, they have to live with the artists' decision.





### Summary

#### The traditional art of molecular modelling

An **expert modelling artist** designs and publishes

- a single optimized model for a particular fluid,
- according to his choice of criteria (often unknown to the public),
- users are passive, they have to live with the artists' decision.

#### Scientific modelling by multicriteria optimization

For established model classes and multiple thermodynamic criteria,

- the dependence of thermodynamic properties on the model parameters is determined and correlated,
- the deviation between model properties and real fluid behaviour is characterized, and the Pareto set is published,
- users can design their own tailored model with minimal effort.