



Reliable molecular modelling and massively-parallel molecular simulation



Martin Horsch, Max Kohns, Kai Langenbach, Stephan Werth, Hans Hasse

Lehrstuhl für Thermodynamik
Technische Universität Kaiserslautern

Stuttgart, 18th June 2015
Collaborative Research Centre 716



**Computational
Molecular Engineering**



Reliable molecular modelling and massively-parallel molecular simulation

SFB  716

“A1”

memo

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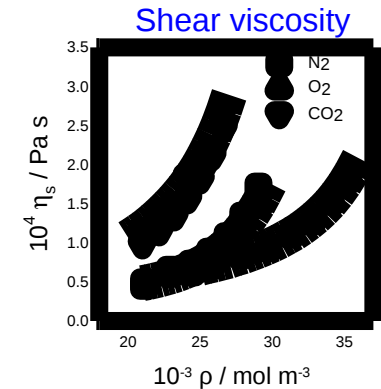
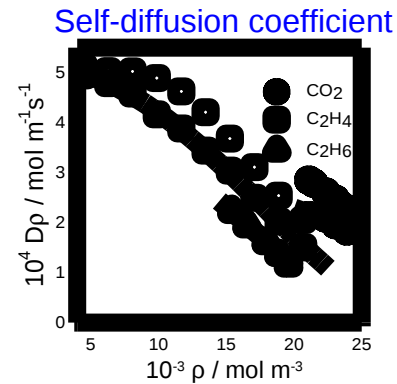
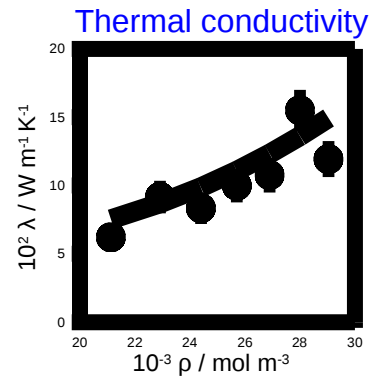
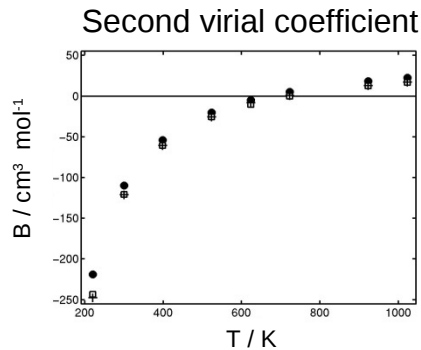
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**Computational
Molecular Engineering**

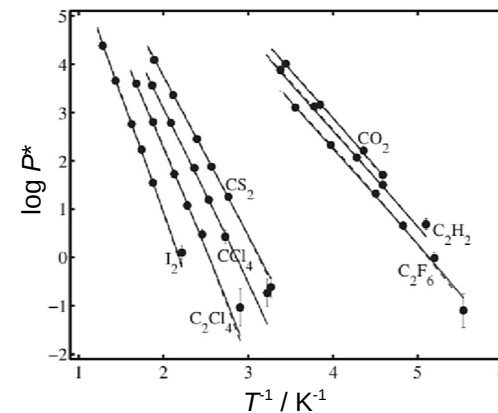
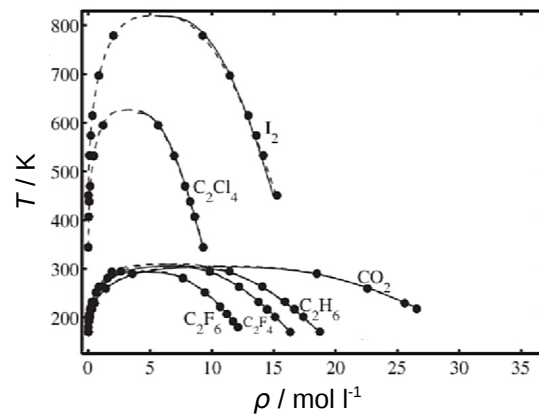


Homogeneous systems in equilibrium: ms2



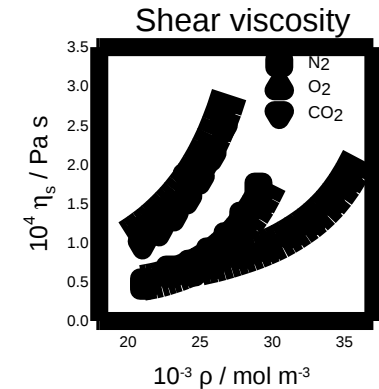
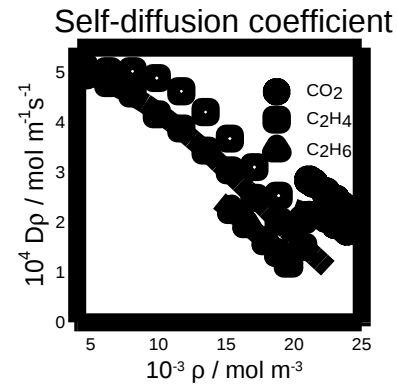
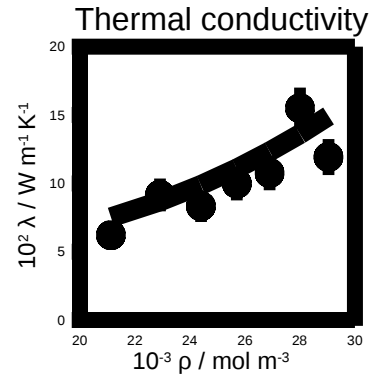
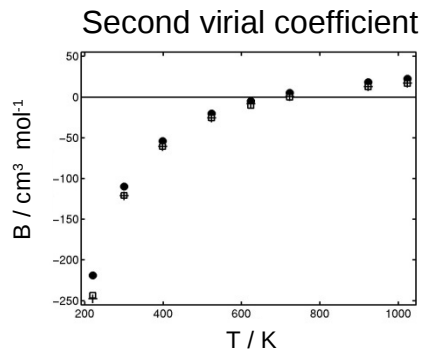
transport properties from equilibrium MD simulation

Vapour-liquid equilibria: Saturated densities and vapour pressures



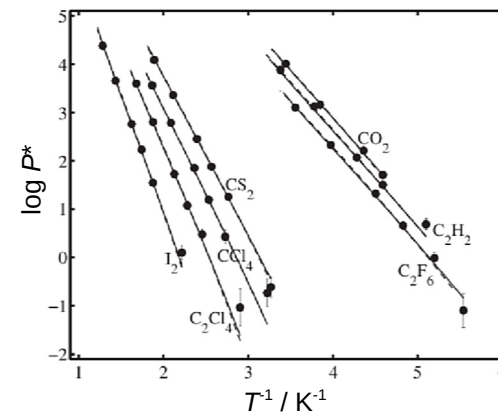
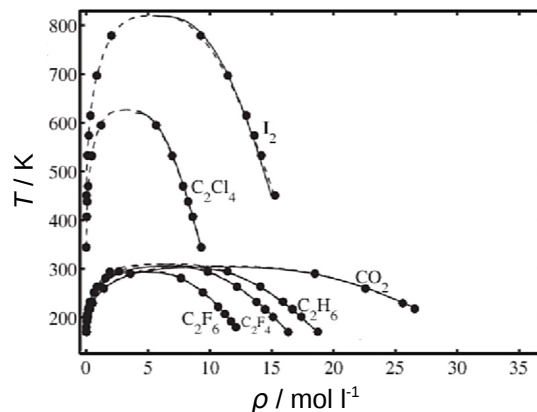


Homogeneous systems in equilibrium: ms2

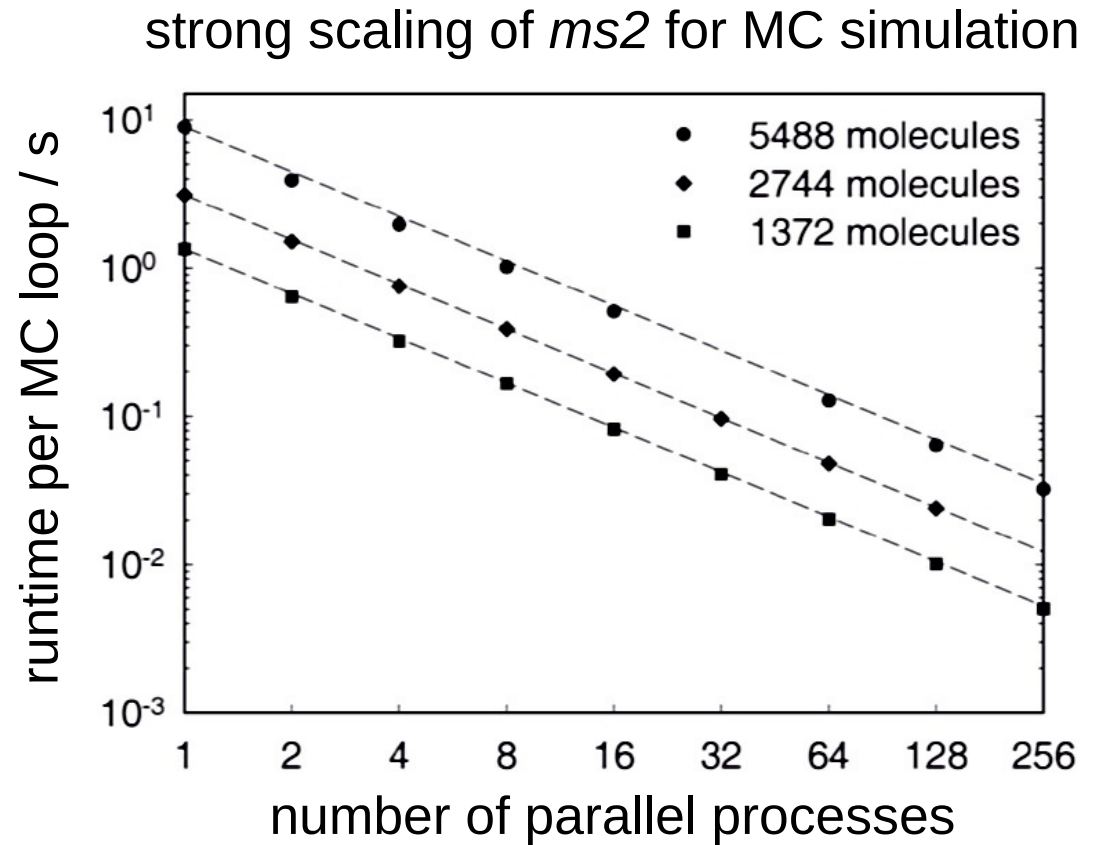
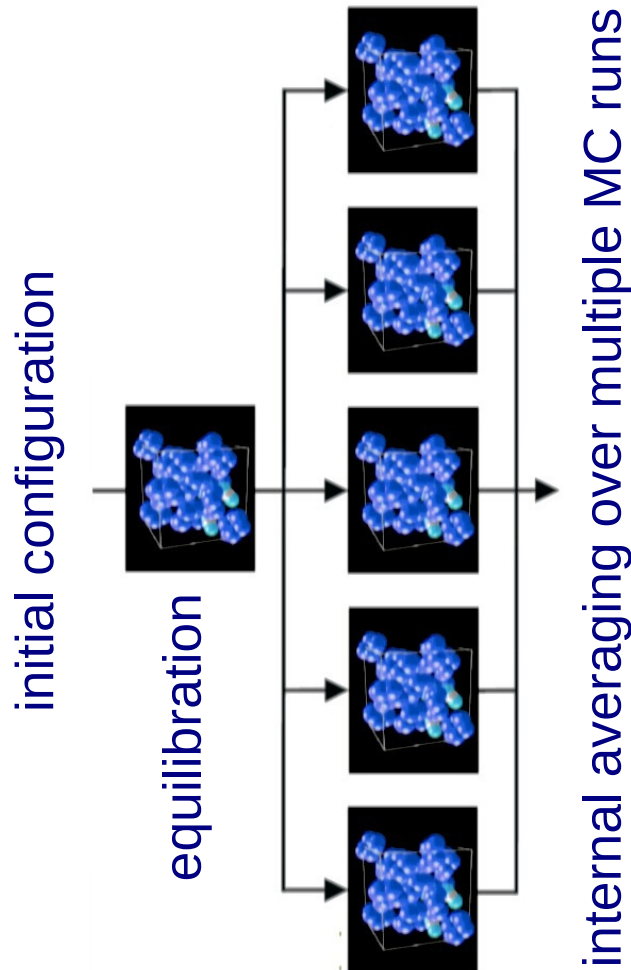


ms2 is freely available for academic use – register at <http://www.ms-2.de/>

Vapour-liquid equilibria: Saturated densities and vapour pressures



Parallel sampling of configurations



Force fields for low-molecular fluids

Geometry

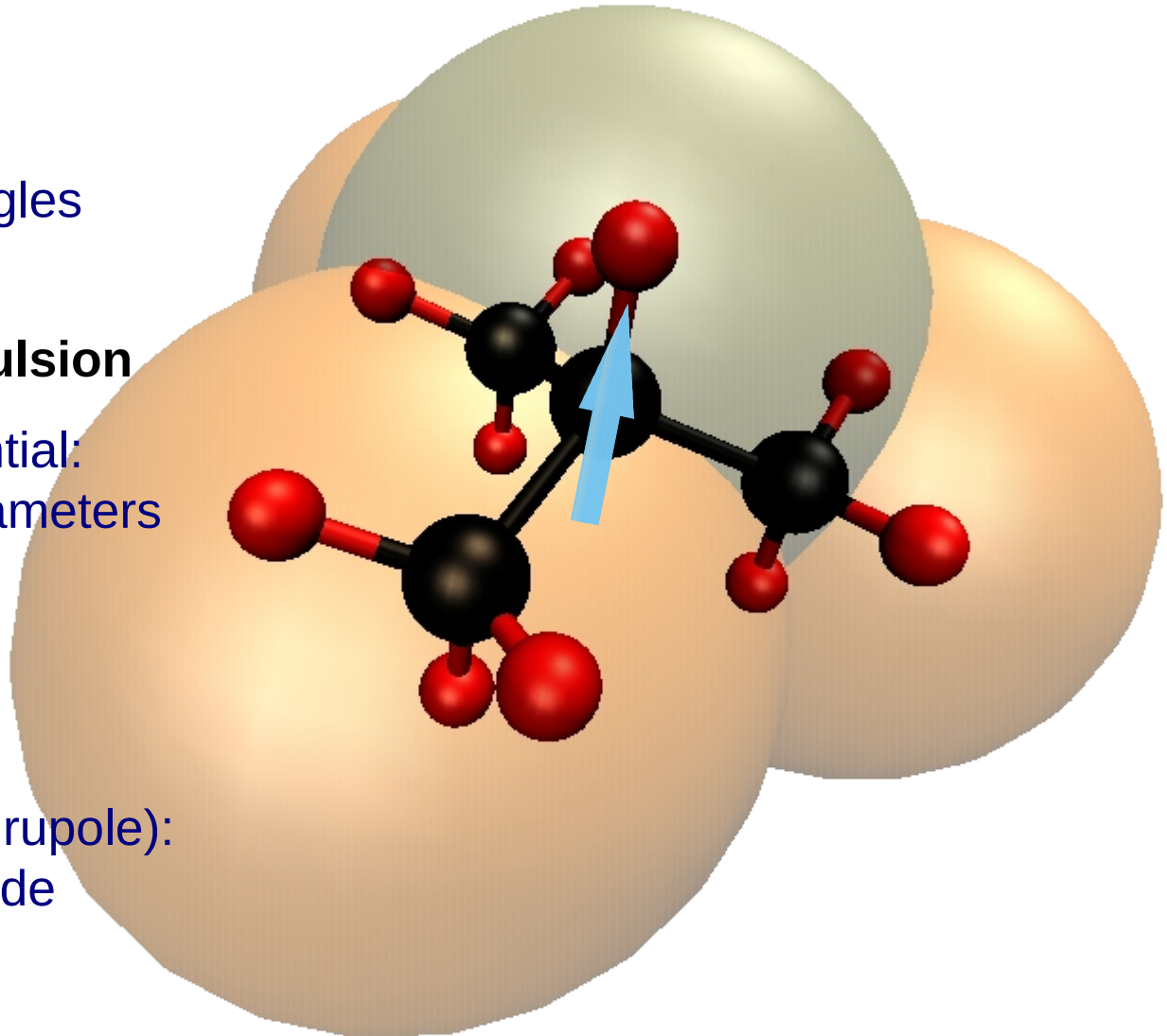
Bond lengths and angles

Dispersion and repulsion

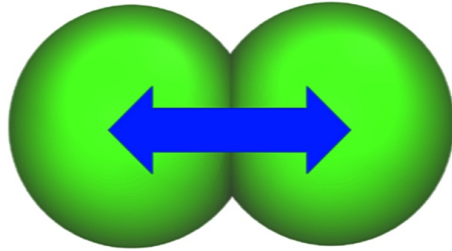
Lennard-Jones potential:
Size and energy parameters

Electrostatics

Point polarities
(charge, dipole, quadrupole):
Position and magnitude



Parameterization of molecular models



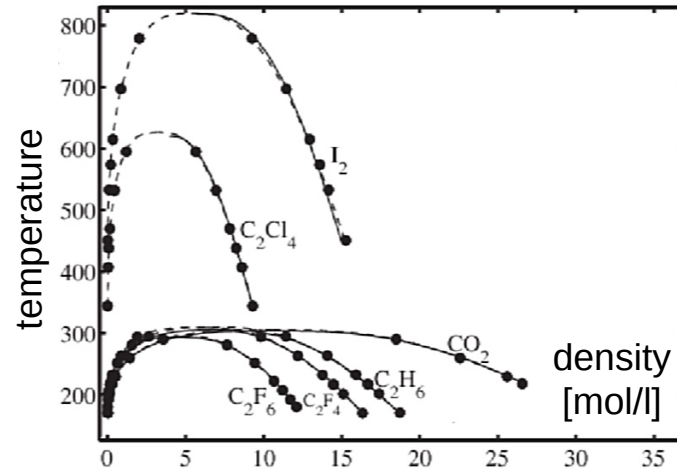
2CLJQ models:

- 2 LJ centres
- Quadrupole

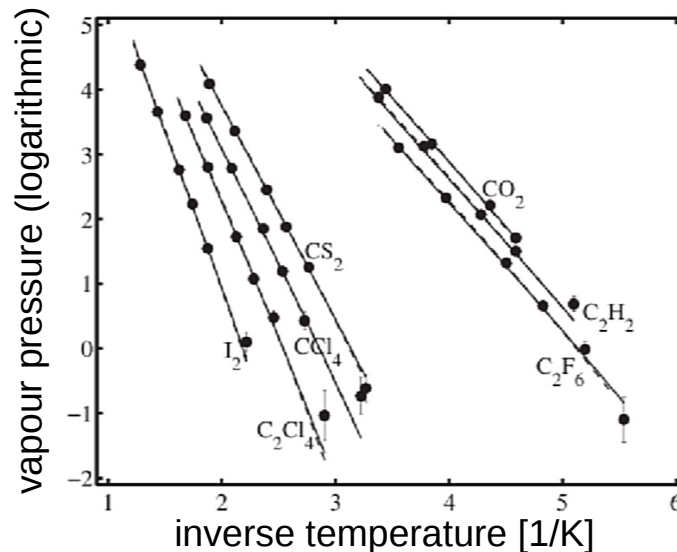
Fit of parameters σ , ϵ , L , Q to VLE data of 29 fluids by Stoll *et al.*

Deviation:

- $\delta\rho' \approx 1\%$
- $\delta P^{\text{sat}} \approx 5\%$



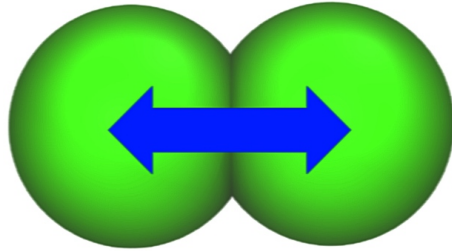
- simulation
- DIPPR correlation



No interfacial properties were considered for the parameterization.



Model validation and predictive simulations



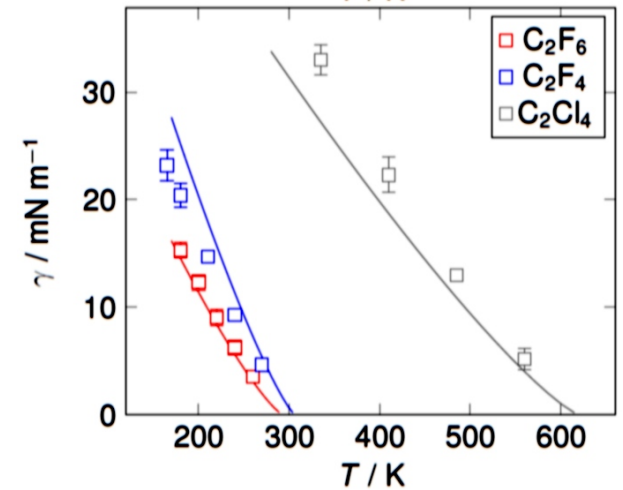
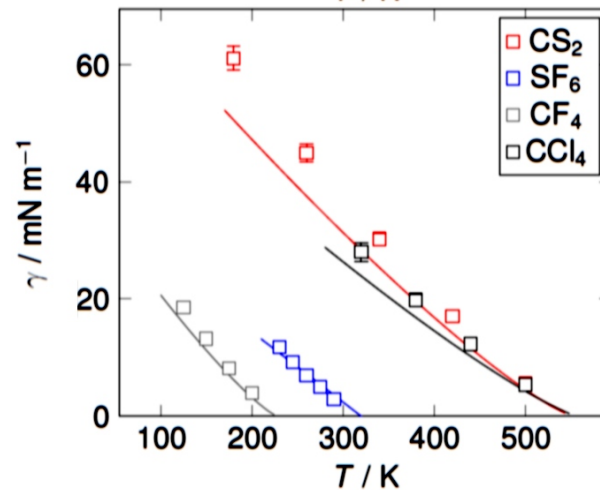
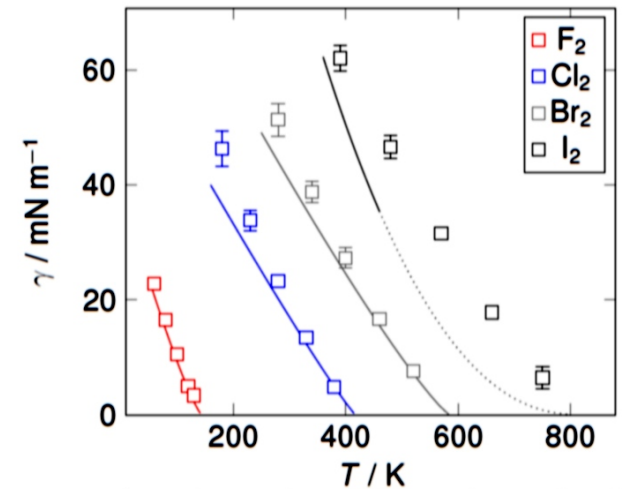
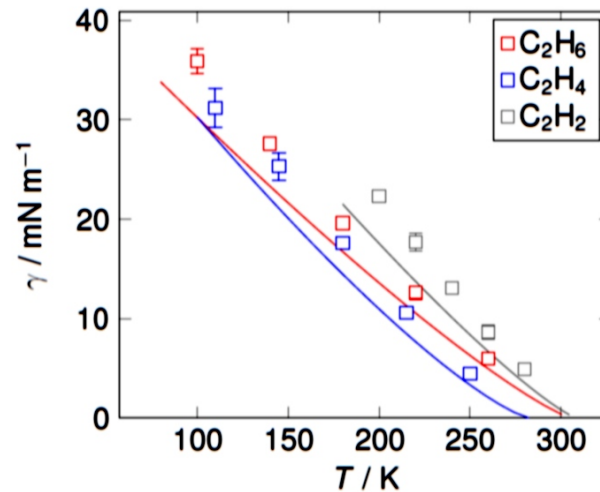
2CLJQ models:

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Fit of parameters σ , ε ,
 L , Q to VLE data of
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Deviation:

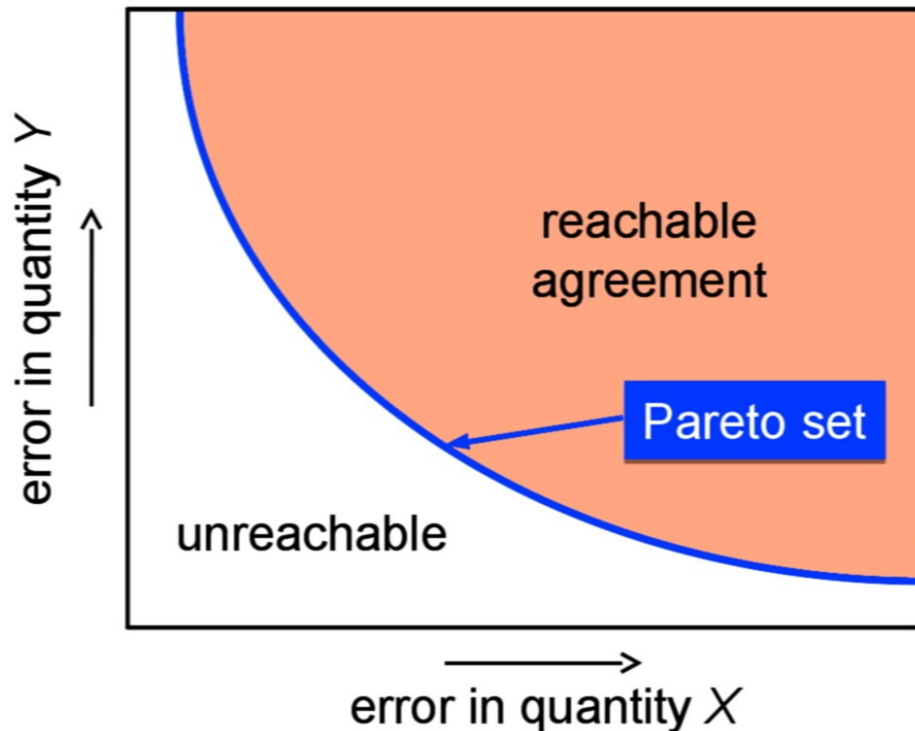
- $\delta\gamma \approx 10 - 20 \%$



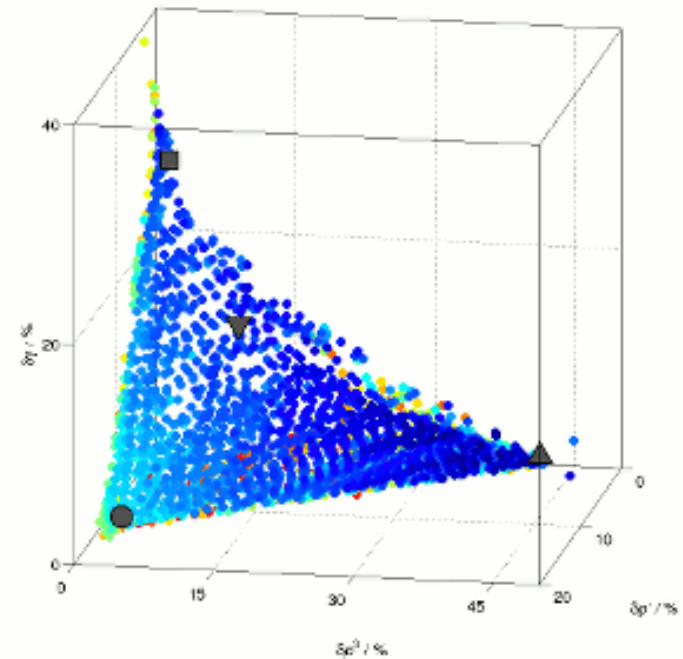


Model tailoring by multicriteria optimization

Pareto optimality criterion



Pareto set for carbon dioxide

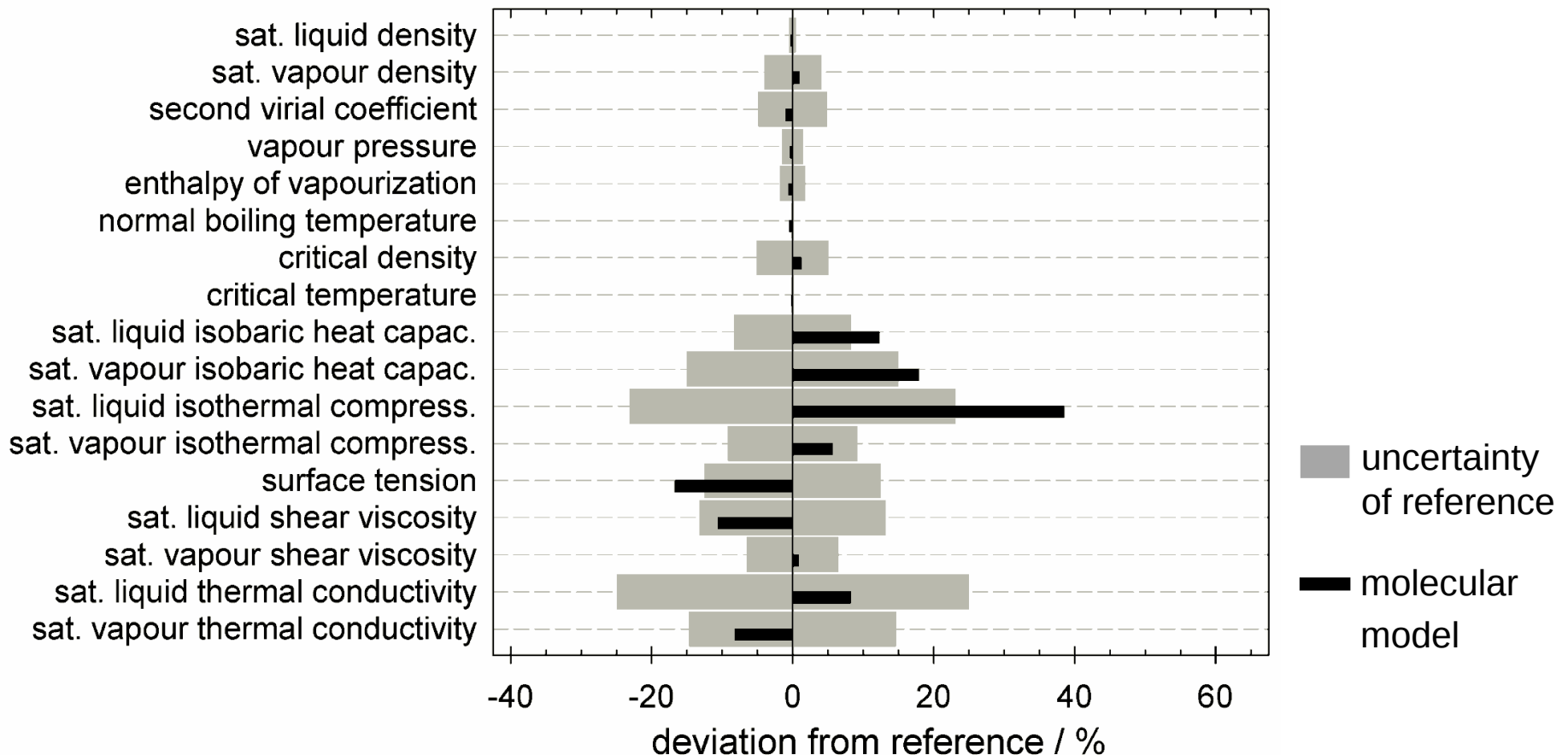


Multicriteria optimization requires massively-parallel molecular modelling.



Quantitative reliability of molecular models

ethylene oxide model by Eckl *et al.* (2008)

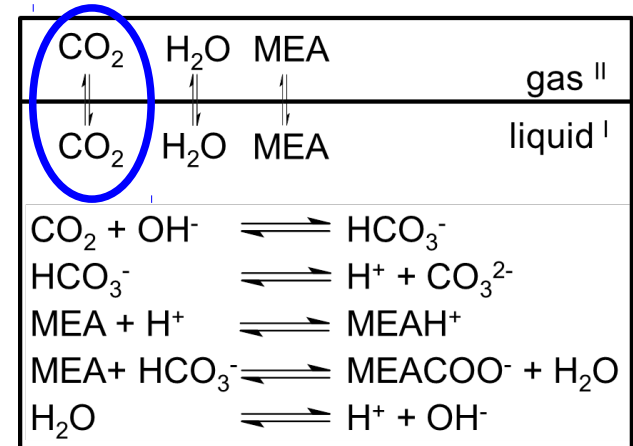




Case study: Analogy between CO₂ and N₂O

Engineering application scenario:

- Gas cleaning by reactive absorption
- Physical gas solubility of CO₂
 - Key property
 - Sometimes impossible to determine





Case study: Analogy between CO_2 and N_2O

Engineering application scenario:

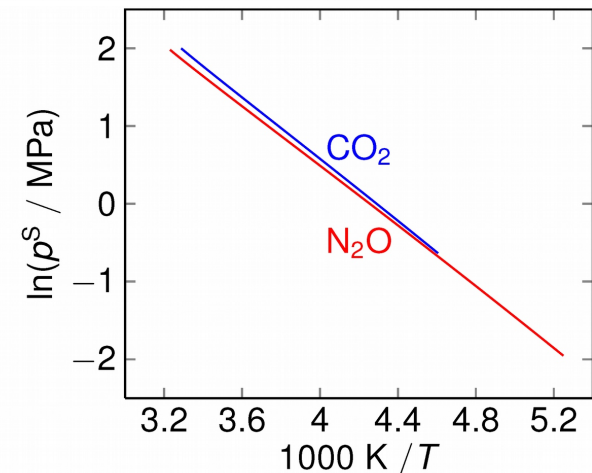
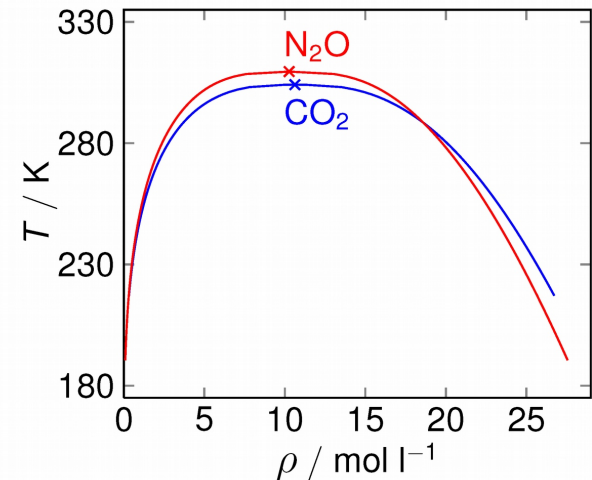
- Gas cleaning by reactive absorption
- Physical gas solubility of CO_2
 - Key property
 - Sometimes impossible to determine

Henry's law: $P y_i = H_i x_i$

Rule of thumb for Henry's law coefficients:

- Analogy with nitrous oxide
- Assumption:

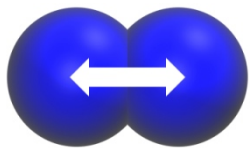
$$R_H = \frac{H_{\text{N}_2\text{O},\text{water}}}{H_{\text{CO}_2,\text{water}}} = \frac{H_{\text{N}_2\text{O},\text{aqueous solution}}}{H_{\text{CO}_2,\text{aqueous solution}}} = \text{const.}$$



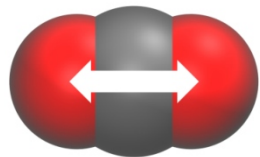


Force field for the pure fluids

Solutes

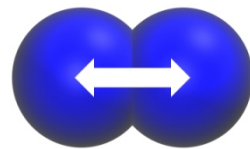


CO₂ (Vrabec *et al.*)

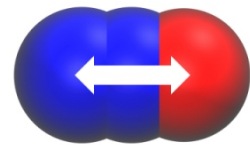


CO₂ (Merker *et al.*)

new molecular models

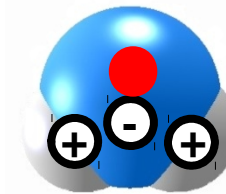


N₂O two-site model

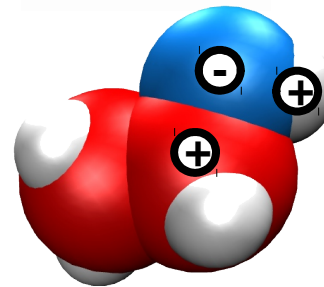


N₂O three-site model

Solvents



Water (TIP4P/2005)

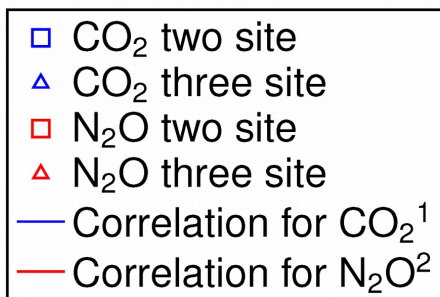
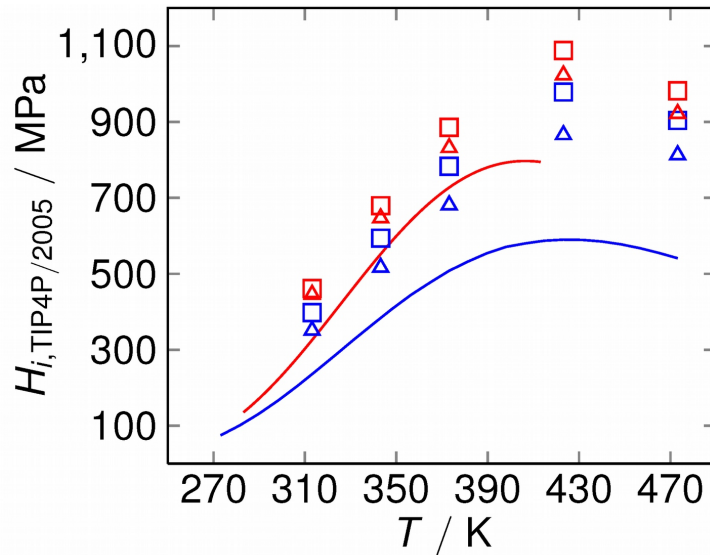


Ethanol (Schnabel *et al.*)

Do mixed solvents containing water and ethanol behave as predicted by the CO₂-N₂O analogy?

Physical solubility in pure water

TIP4P/2005 water, prediction



1) Rumpf and Maurer, Ber. Bunsenges. Phys Chem. 97 (1993) 85.

2) Penttilä *et al.*, Fluid Phase Equilib. 311 (2011) 59.

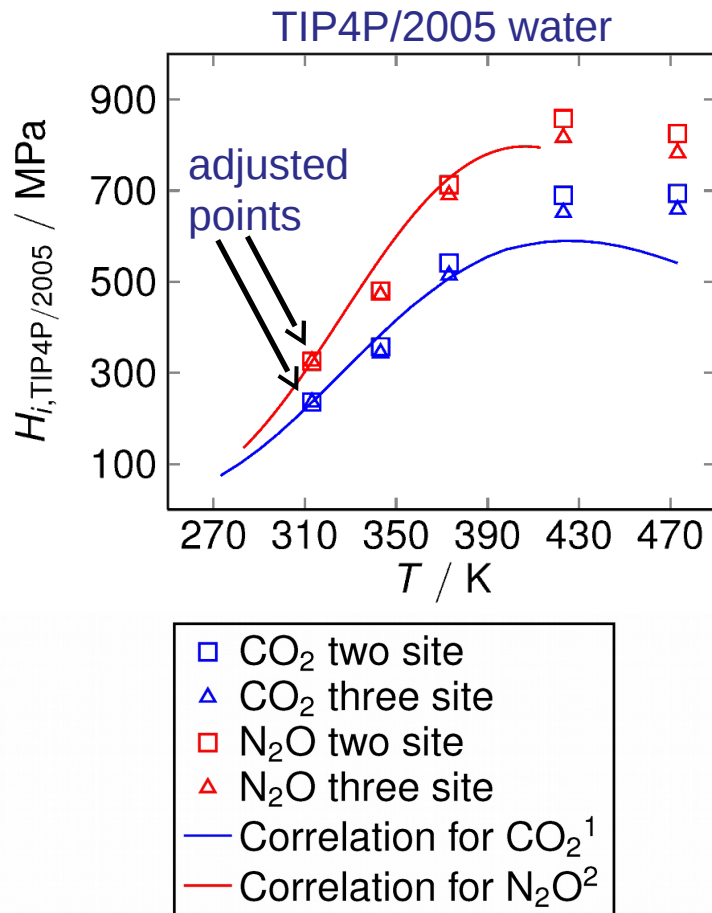
- Lorentz-Berthelot combining rule:

$$\sigma_{AB} = \frac{\sigma_A + \sigma_B}{2}$$

$$\epsilon_{AB} = \sqrt{\epsilon_A \epsilon_B}$$

- Overestimation of Henry's law constant in all cases
- Adjustment of a binary interaction parameter necessary

Physical solubility in pure water



- Modified Lorentz-Berthelot combining rule:

$$\sigma_{AB} = \frac{\sigma_A + \sigma_B}{2}$$

$$\epsilon_{AB} = \xi_{AB} \sqrt{\epsilon_A \epsilon_B}$$

- Temperature dependence is well captured by all models
- Best agreement for two-site model of N₂O and three-site model of CO₂

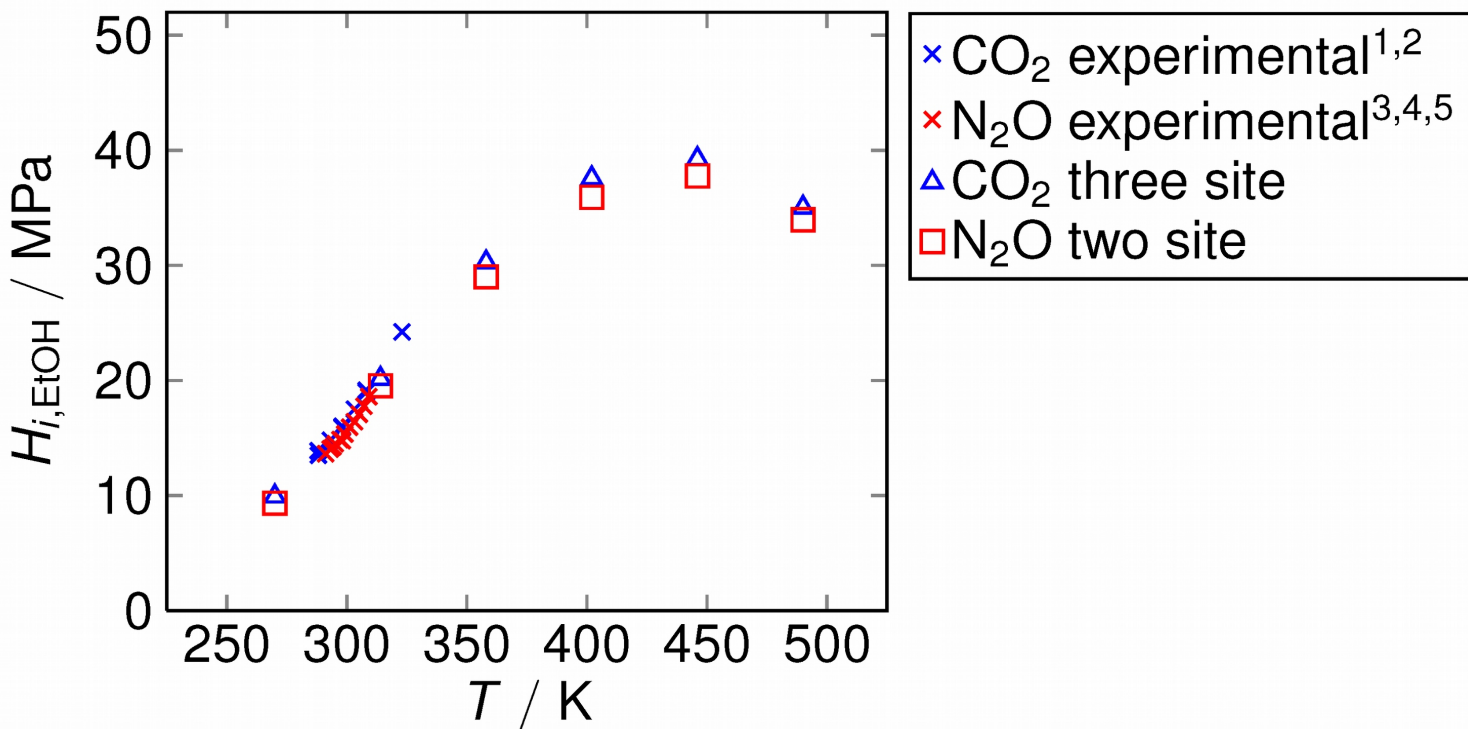
1) Rumpf and Maurer, Ber. Bunsenges. Phys Chem. 97 (1993) 85.

2) Penttilä *et al.*, Fluid Phase Equilib. 311 (2011) 59.



Solubility in pure ethanol

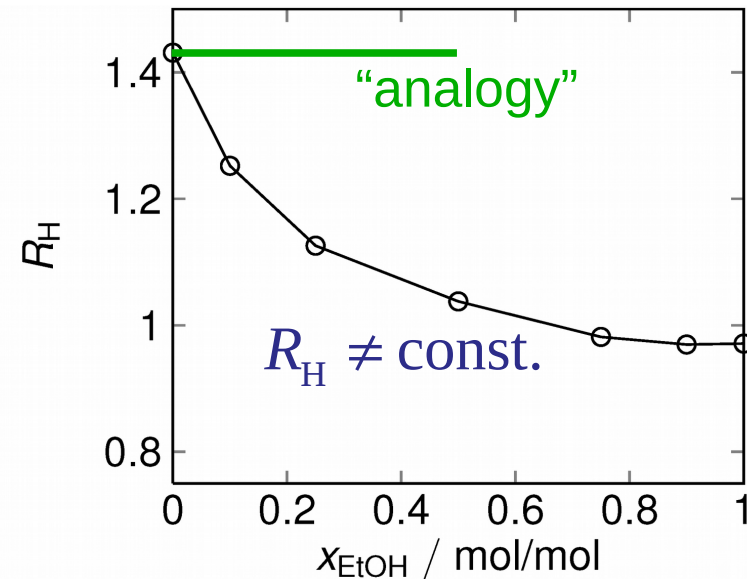
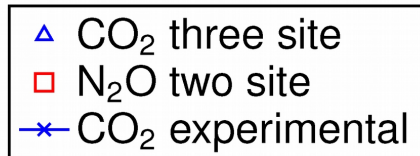
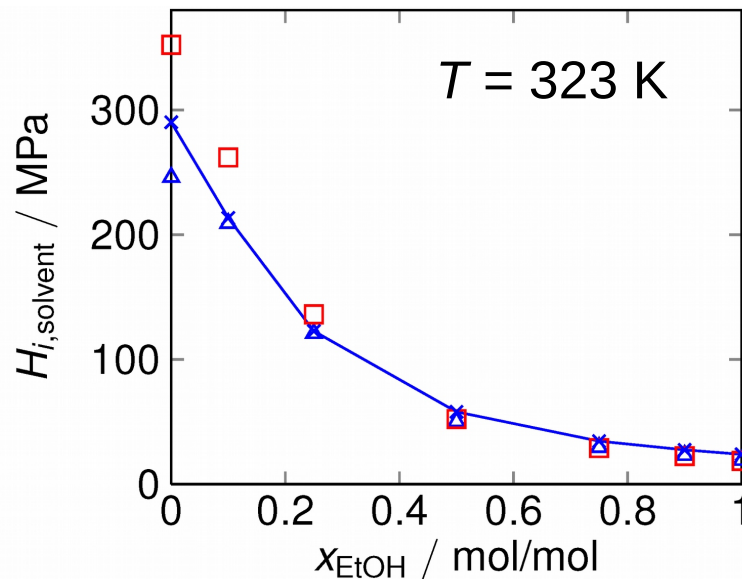
Predictive simulations, i.e. $\xi_{ab} = 1$ in all cases



1) Postigo and Katz, J. Solution. Chem. 16 (1987) 1015; 2) Dalmolin et al., Fluid Phase Equilib. 245 (2006) 193; 3) Kunerth, Phys. Rev. 19 (1922) 512; 4) Sada et al., Ind. Eng. Chem. Fundam. 14 (1975) 232; 5) Hsu and Campbell, Aerosol Age 9 (1964) 34.



Physical solubility in the mixed solvent

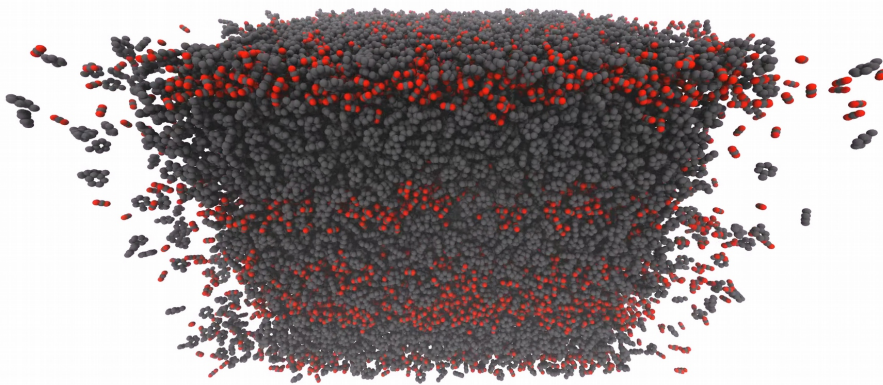


- models adjusted to solubility in pure water
- validated for pure EtOH (both), mixture (CO₂)
- predictive use: breakdown of the “analogy”

Efficient simulation of fluids at interfaces

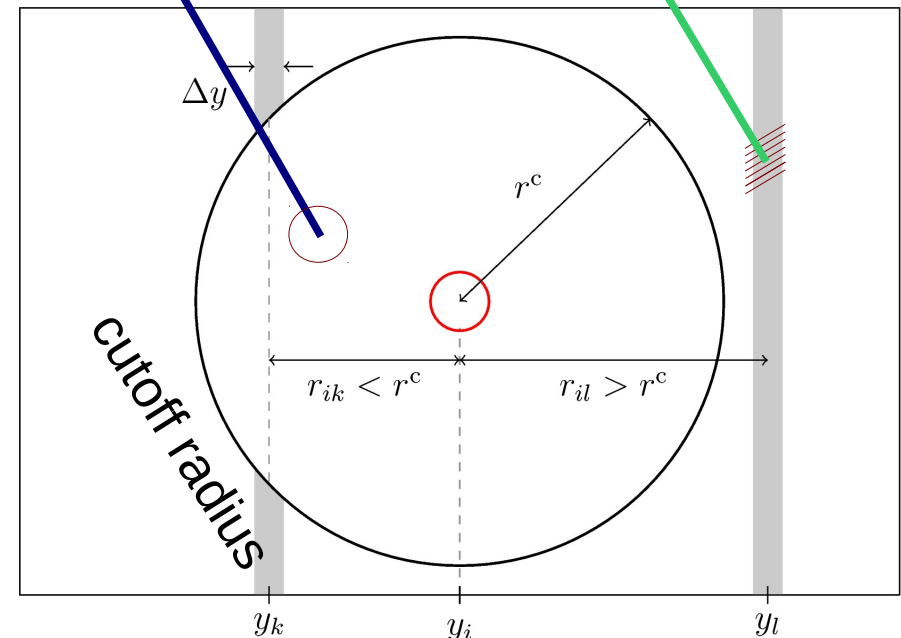
For planar interfaces:

Long-range correction from the density profile, following **Janeček**.



short range
(explicit)

long range
(correction)



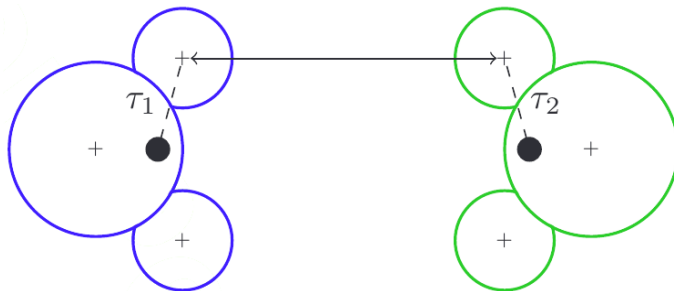
Full evaluation of all pairwise interactions is too expensive ...

... instead, **short-range interactions** are evaluated for **neighbours**.

Efficient simulation of fluids at interfaces

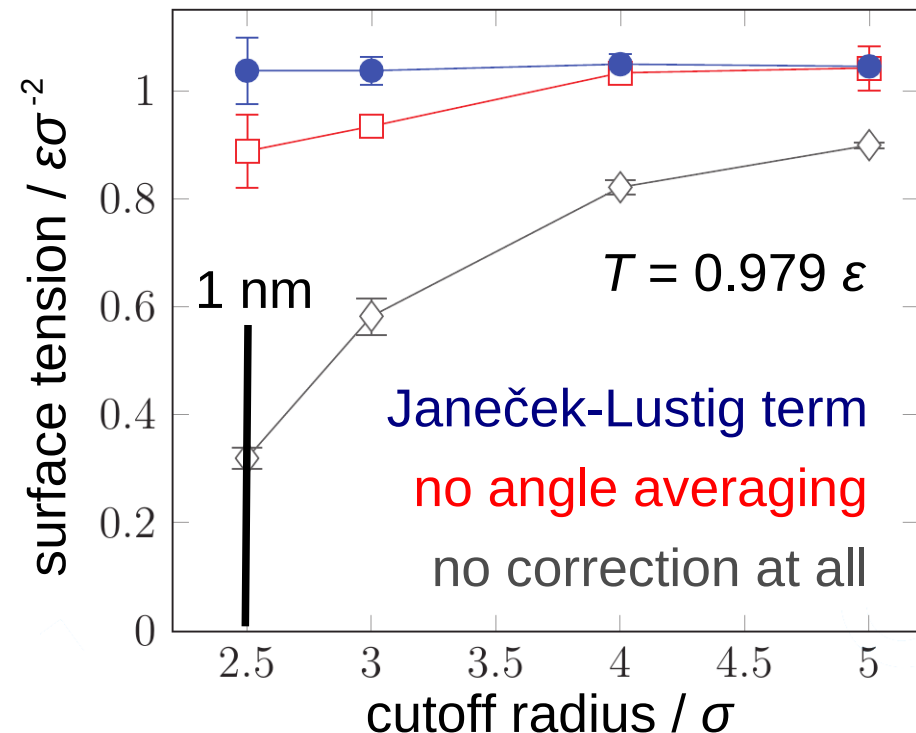
For planar interfaces:

Long-range correction from the density profile, following **Janeček**.



Angle-averaging expression for multi-site models, following **Lustig**.

Two-centre LJ fluid (2CLJ)

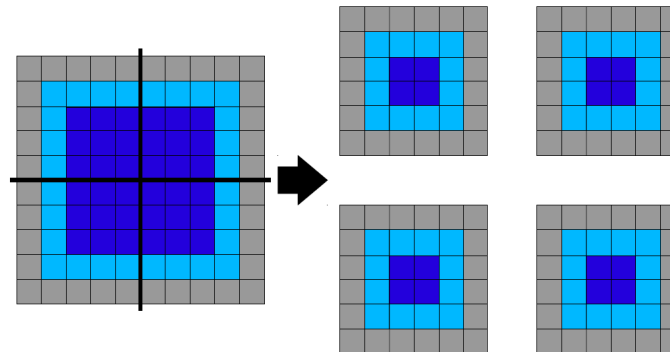


For arbitrary geometries, e.g. the fast multipole method can be employed.



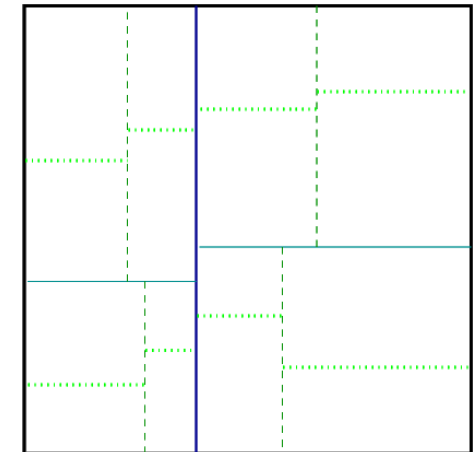
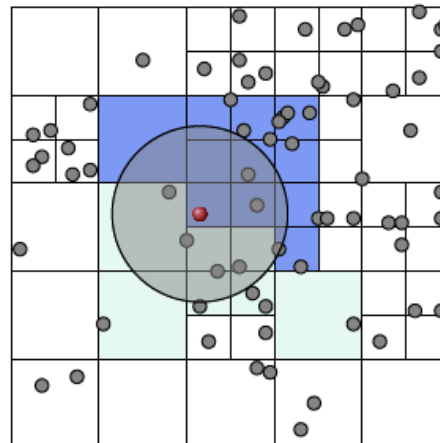
Efficient simulation of large systems

Linked-cell data structure suitable for spatial domain decomposition:



(non-blocking, overlapping MPI send/receive operations)

Methods for heterogeneous or fluctuating particle distributions:



large systems “1”: molecular dynamics

<http://www.ls1-mardyn.de/>



Efficient simulation of large systems

Memory-efficient implementation based on the linked-cell data structure:

21	22	23	24	25	26	27	28	29	30
11	12	13	14	15	16	17	18	19	20
1	2	3	4	5	6	7	8	9	10

sliding window

Optionally, forces acting on molecules are only stored until their cell leaves the sliding window.

large systems “1”: molecular dynamics

<http://www.ls1-mardyn.de/>



Efficient simulation of large systems

Memory-efficient implementation based on the linked-cell data structure:

21	22	23	24	25	26	27	28	29	30
11	12	13	14	15	16	17	18	19	20
1	2	3	4	5	6	7	8	9	10

hyperthreaded sliding window

Optionally, forces acting on molecules are only stored until their cell leaves the sliding window.

Efficient vectorization:

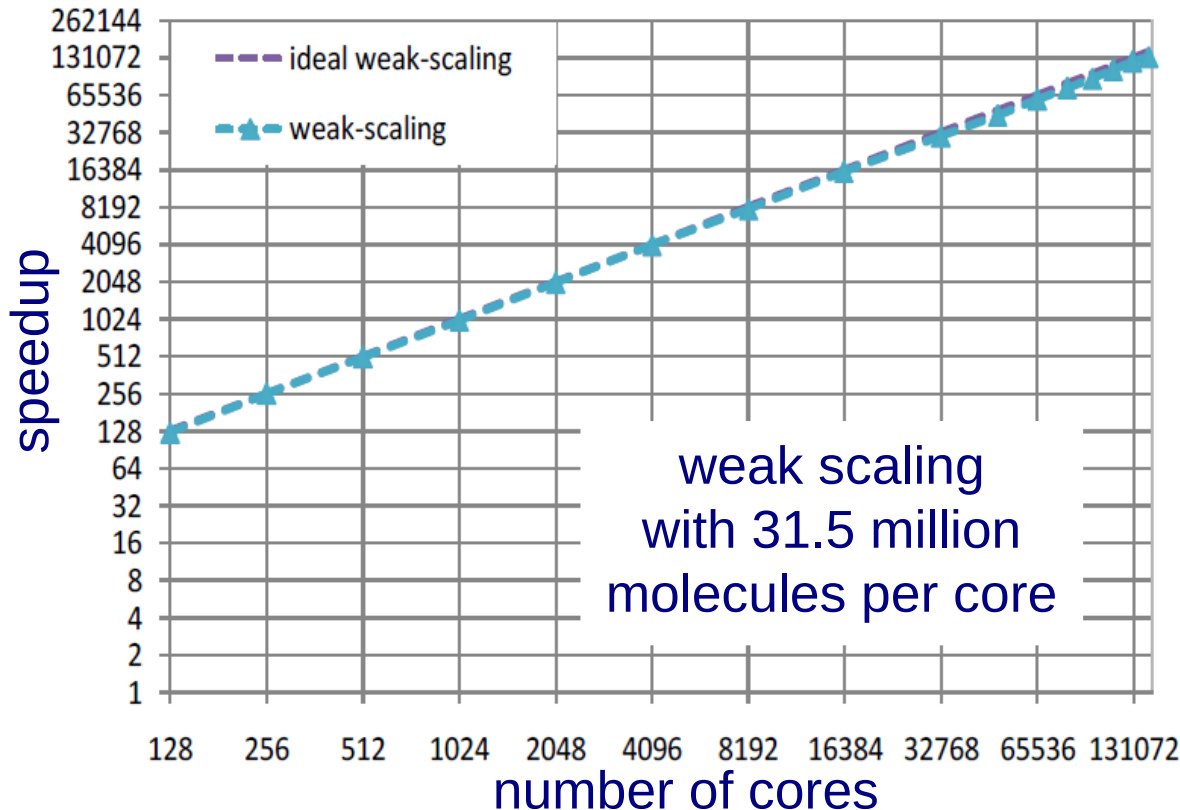
- Optimization by hand, using advanced vector extensions (AVX).
- Conversion from array of structures (AoS) to structure of arrays (SoA).

large systems “1”: molecular dynamics

<http://www.ls1-mardyn.de/>

Large-scale MD simulation on SuperMUC

Up to $N = 4 \cdot 10^{12}$ molecules on SuperMUC



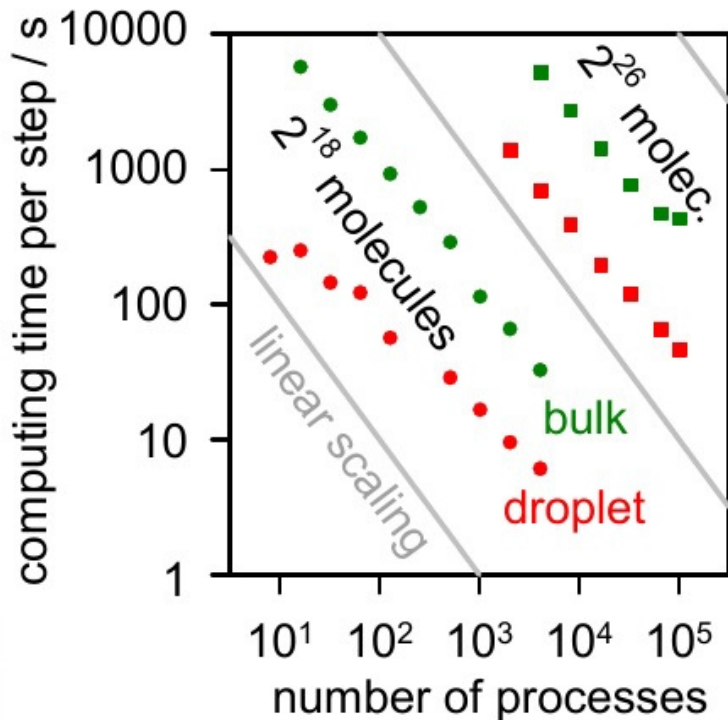
large systems “1”: molecular dynamics

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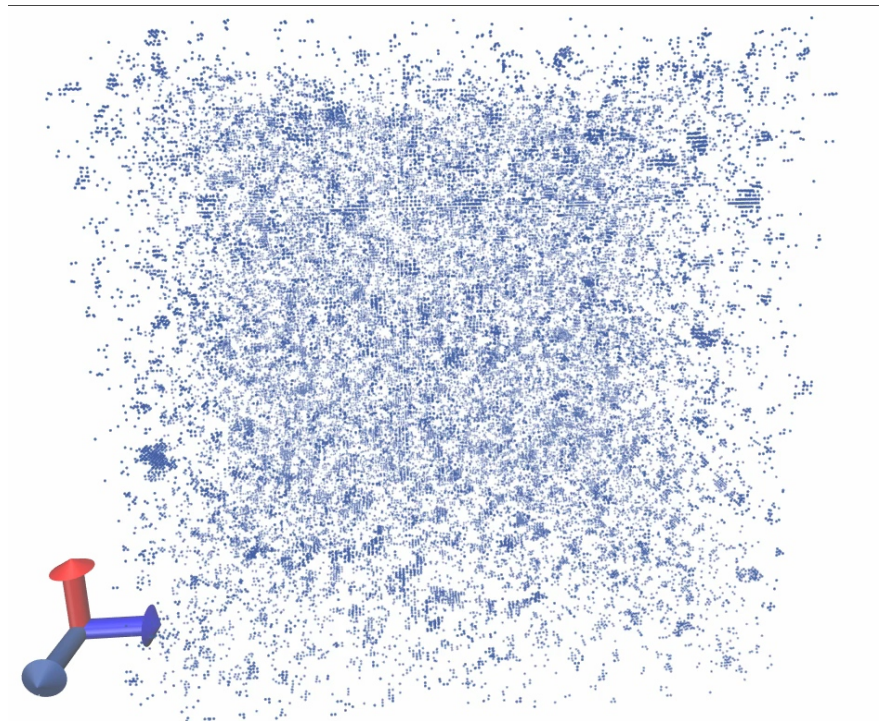


Large-scale MD simulation on hermit

strong scaling (Amdahl)



homogeneous cavitation

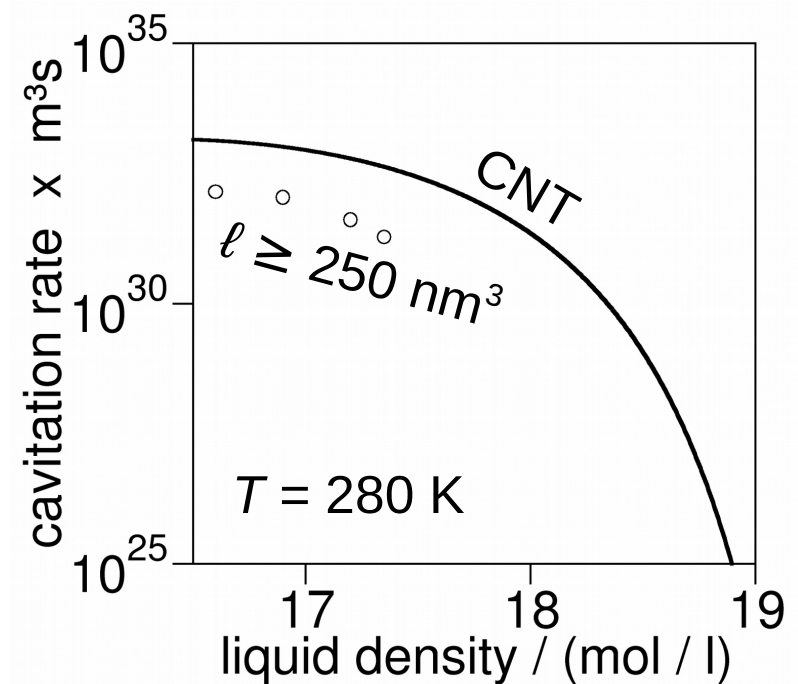
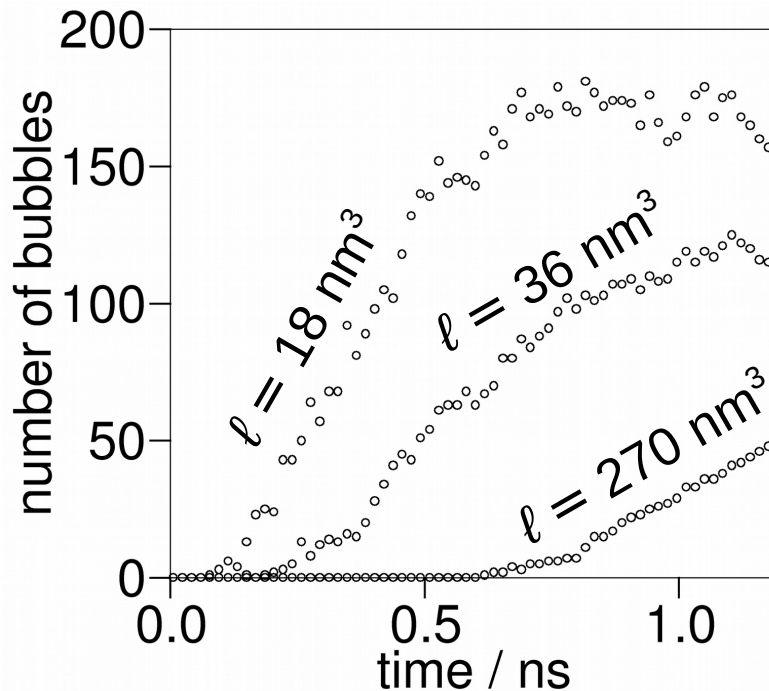


CO₂ ($T = 280$ K and $\rho = 17.2$ mol/l), 3CLJQ
 25 million molecules on 110 592 cores



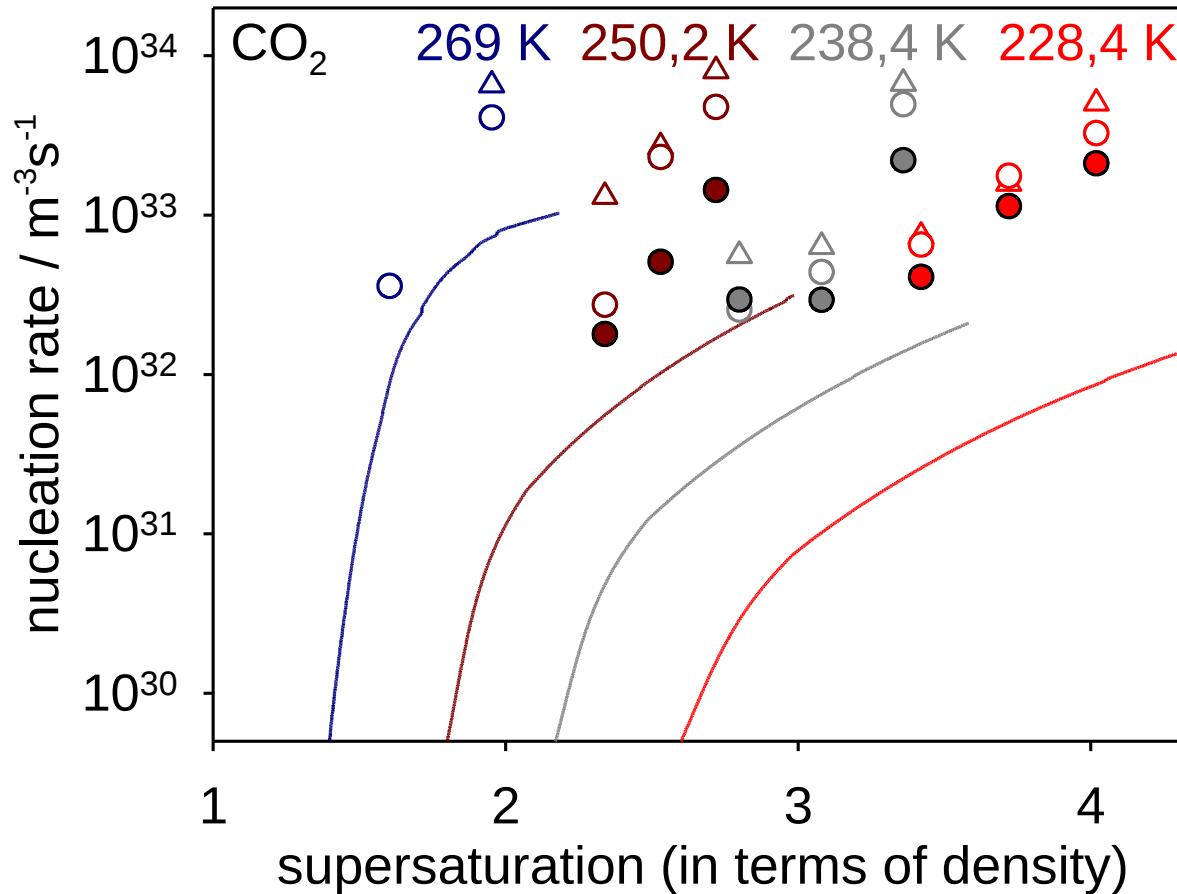
MD simulation of cavitation processes

Yasuoka-Matsumoto method: Count nuclei exceeding a threshold size ℓ .



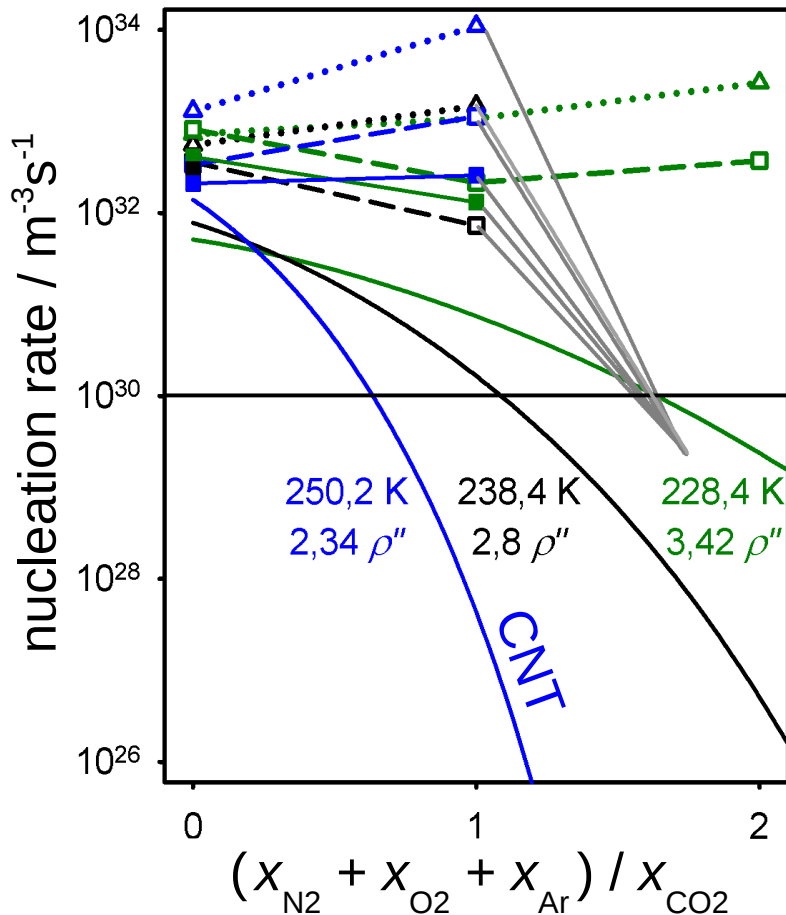
Classical nucleation theory predicts critical cavity sizes from 5 to 100 nm³.

MD simulation of nucleation in vapours



- Classical nucleation theory (CNT)
- \triangle $\ell = 50$ molecules
- \circ $\ell = 75$ molecules
- \bullet $\ell = 300$ molecules

The air pressure effect on CO₂ nucleation



Scenario:

- Vapour contains k components
- Liquid phase is approximately pure
- Other $k - 1$ components: Carrier gas

Carrier gas effect (Wedekind *et al.*):

- Thermalization $\rightarrow J$ increases
- Greater pressure $\rightarrow J$ decreases

— CNT following Wedekind *et al.*

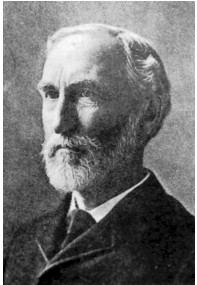
\triangle $\ell = 50$

\square $\ell = 100$

\blacksquare $\ell = 150$



Fluid mixtures: Interfacial thermodynamics



„take some point [...] and **imagine a geometrical surface** to pass through this point and all other points which are similarly situated [...] called the dividing surface“.

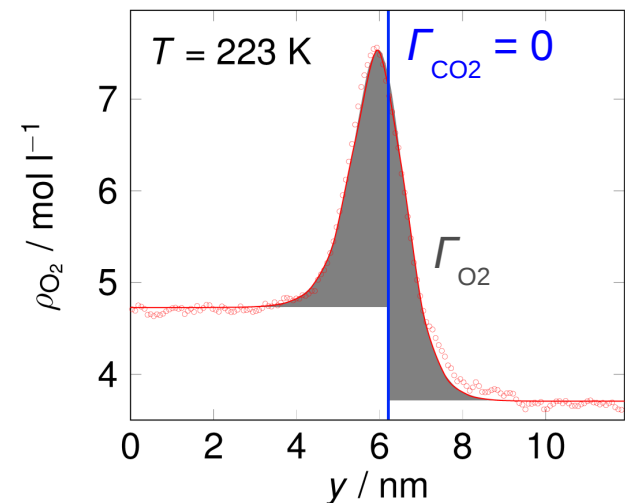
Thermodynamic **excess quantities** are ascribed to the interface

$$X^{\text{System}} = X^I + X^{II} + X^E,$$

e.g. surface free energy or adsorption.

Beside absolute excesses, there are **differential quantities**, such as the surface tension

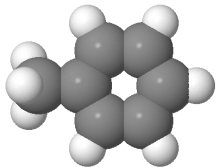
$$\gamma = \left(\frac{\partial F}{\partial A} \right)_{N, V, T}.$$





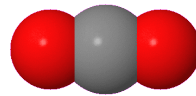
Case study: Adsorption at fluid interfaces

Toluene



7CLJD+5Q
(Huang *et al.*)

CO₂



3CLJQ
(Merker *et al.*)

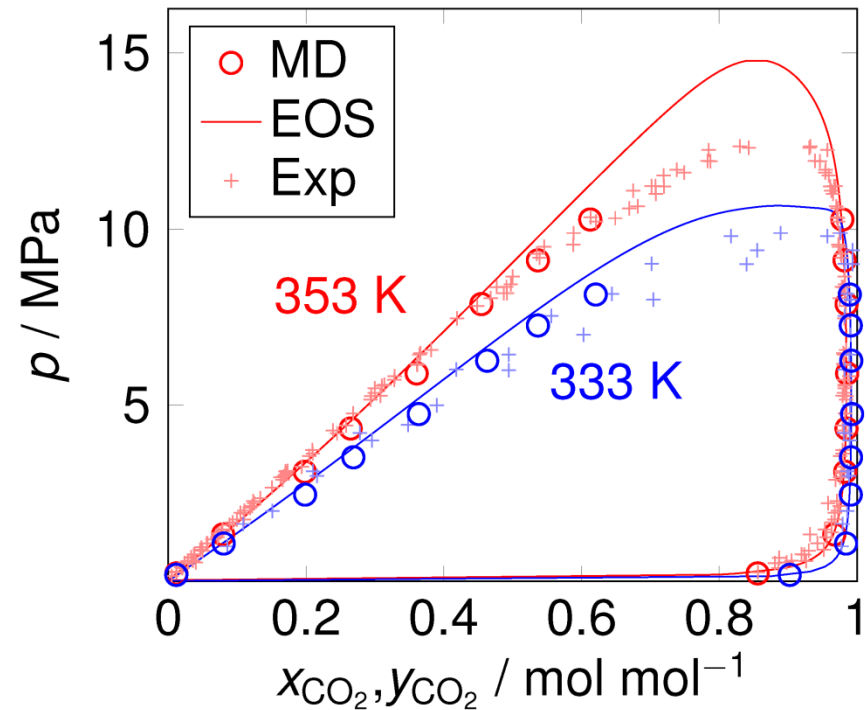
unlike interaction by
modified Lorentz-
Berthelot rule

$$\sigma_{AB} = \frac{\sigma_A + \sigma_B}{2} \quad \epsilon_{AB} = \xi_{AB} \sqrt{\epsilon_A \epsilon_B}$$

with $\epsilon_{AB} = 0.95$

adjusted to Henry's law coefficients

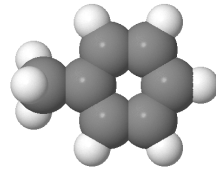
vapour-liquid equilibrium



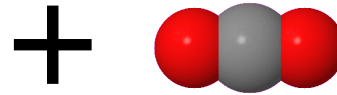


Case study: Adsorption at fluid interfaces

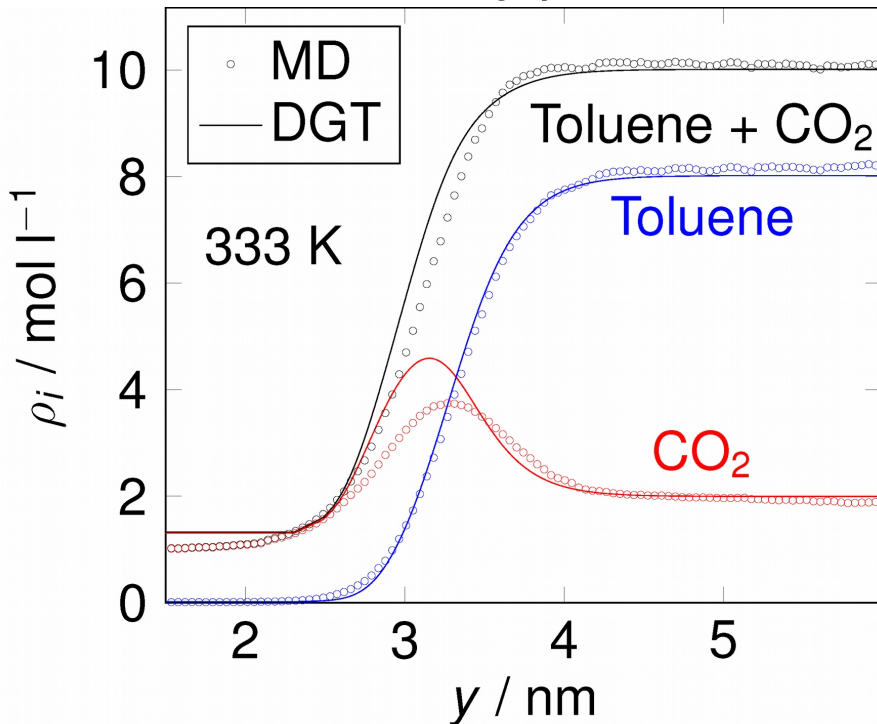
Toluene



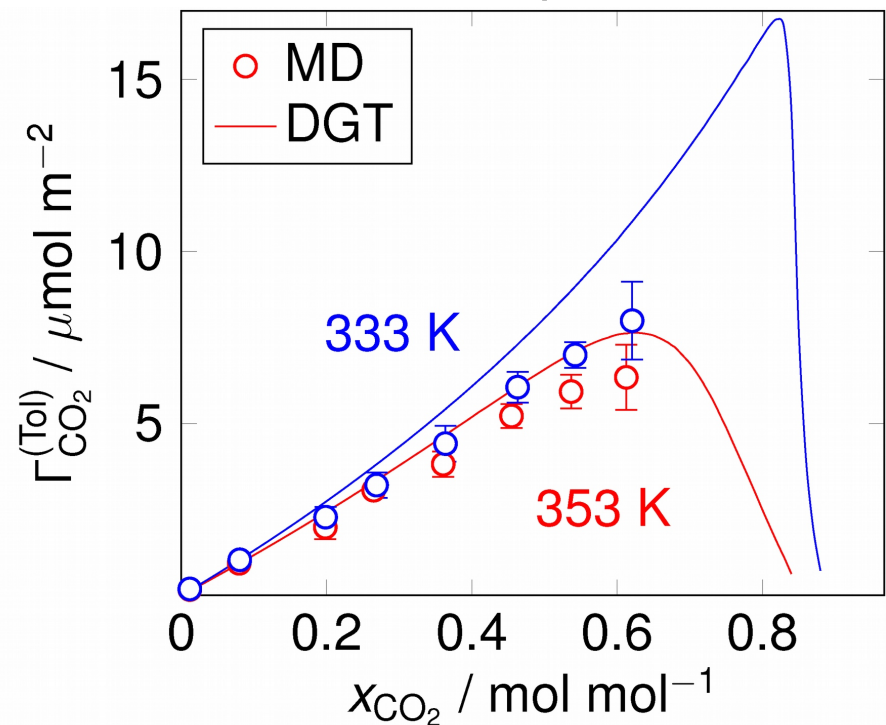
CO₂



density profile



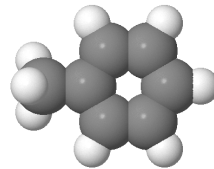
adsorption





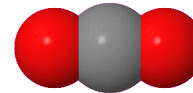
Case study: Adsorption at fluid interfaces

Toluene

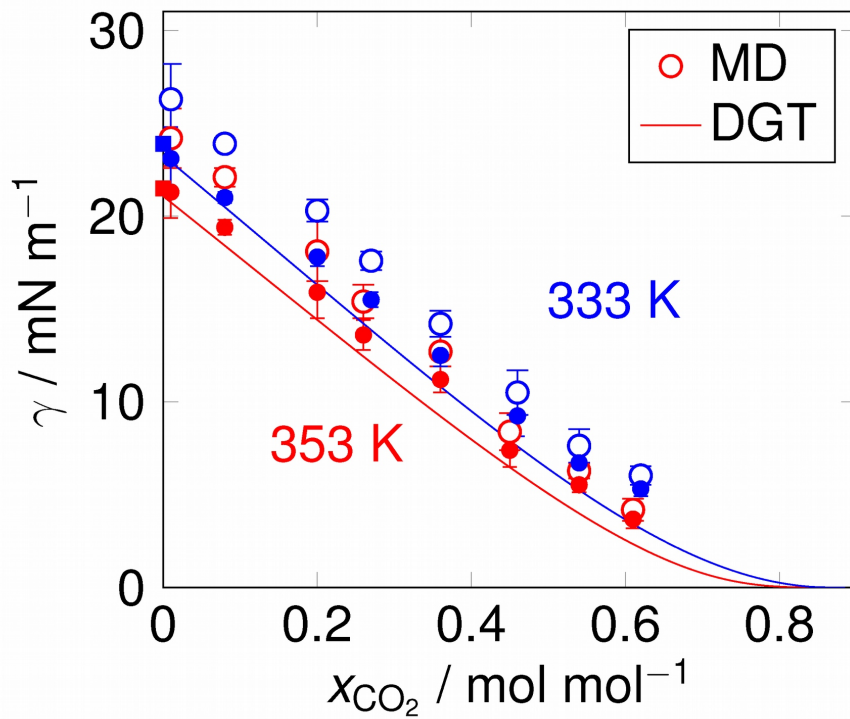


+

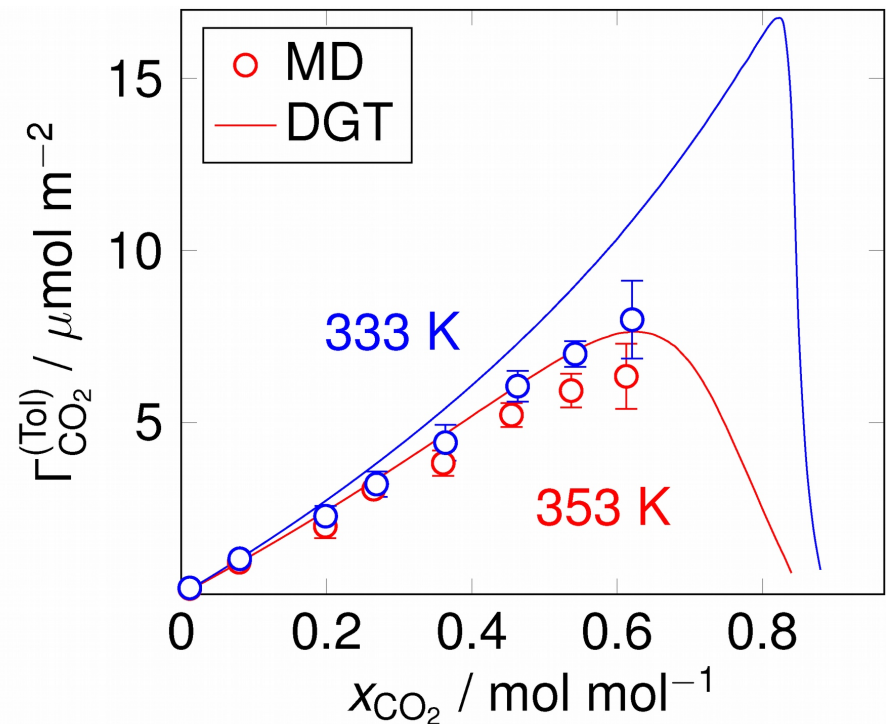
CO₂



surface tension



adsorption





Conclusion

By massively-parallel molecular modelling, the thermodynamic behaviour of model classes (e.g. 2CLJD, 2CLJQ) can be characterized and used to tune molecular models to an application by **multicriteria optimization**.

Validated molecular models enable **reliable predictions** for thermodynamic properties by which empirical rules of thumb become obsolete.

By massively-parallel molecular simulation, complex activated processes like **cavitation** in metastable liquids and **nucleation** in supersaturated vapours can be investigated at molecular resolution.

Adsorption of light-boiling components at vapour-liquid interfaces of fluid mixtures can be determined and related to the surface tension.