



# Computational molecular engineering: Scalable simulation and reliable modelling

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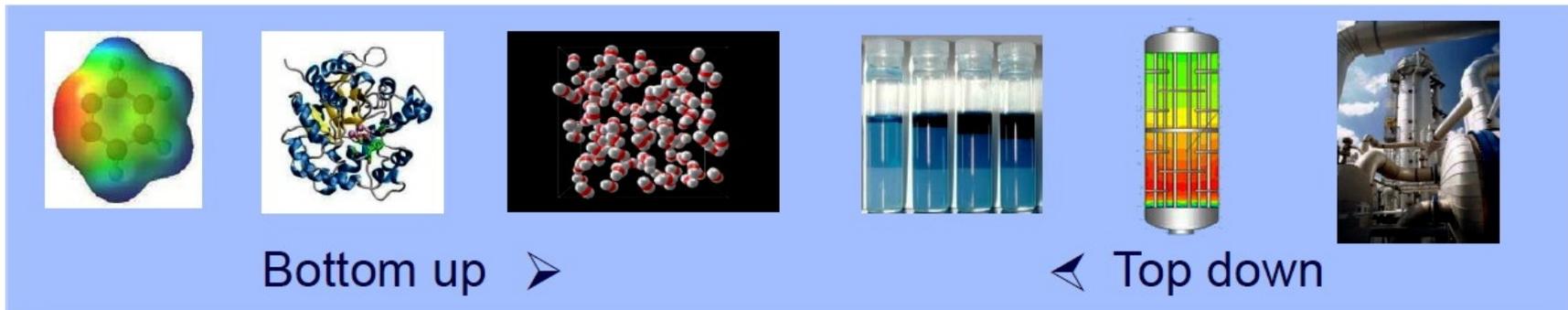
Laboratory of Engineering Thermodynamics, University of Kaiserslautern

Tianjin, 16<sup>th</sup> November 2015  
**Tianjin Center for Applied Mathematics**



**Computational  
Molecular Engineering**

# Computational molecular engineering



## From Physics (qualitative accuracy)

- Physically realistic modelling of intermolecular interactions
- Separate contributions due to repulsive and dispersive as well as electrostatic interactions

## To Engineering (quantitative reliability)

- No blind fitting, but parameters of *effective pair potentials* are adjusted to experimental data
- Physical realism facilitates reliable interpolation and extrapolation

# Force fields for molecular modelling

## Geometry

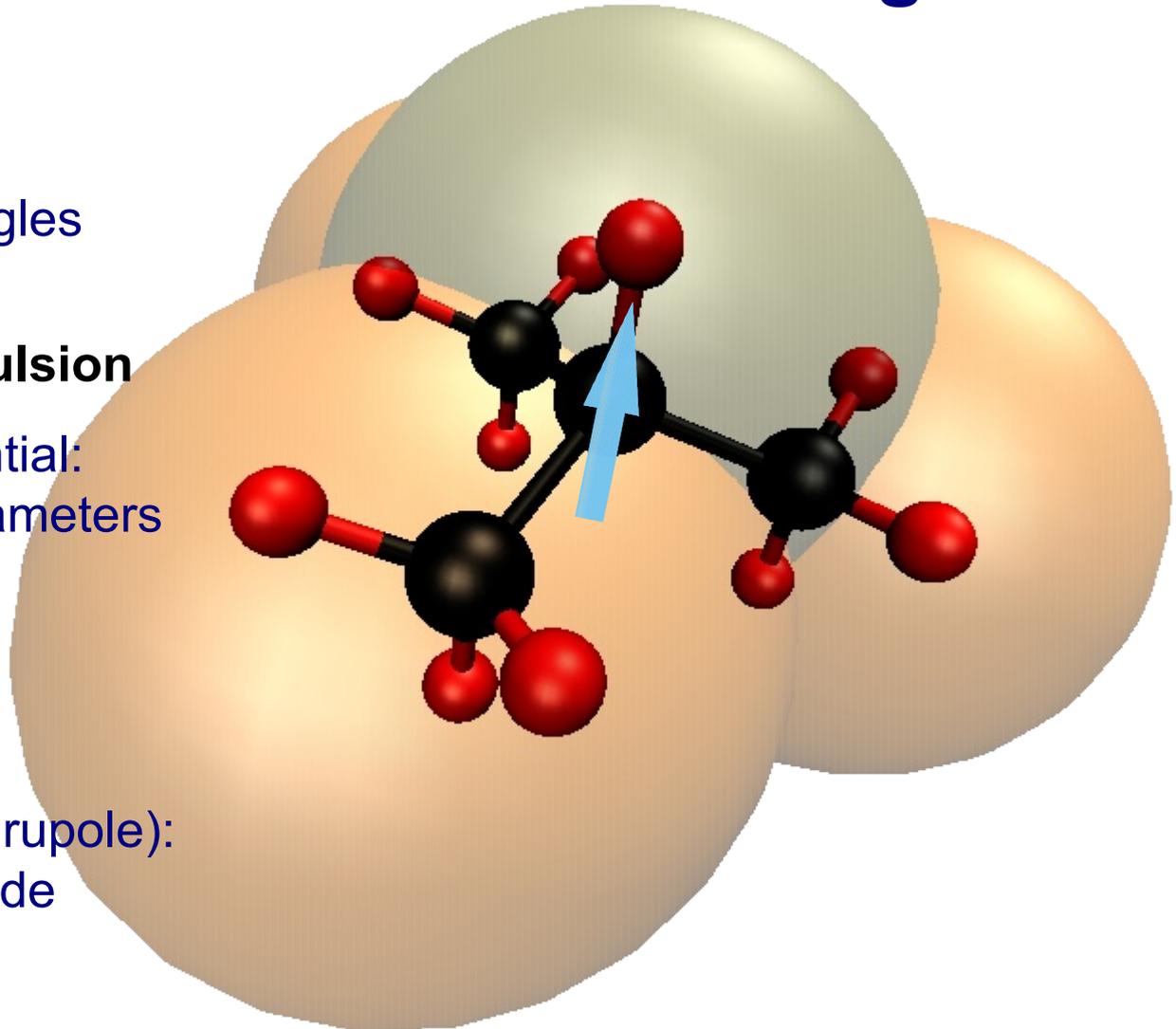
Bond lengths and angles

## Dispersion and repulsion

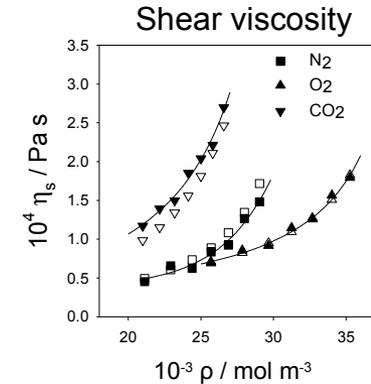
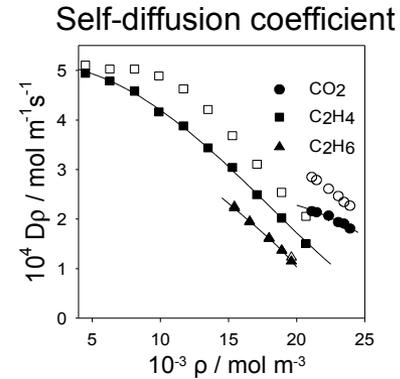
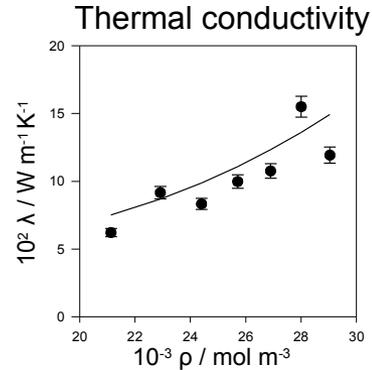
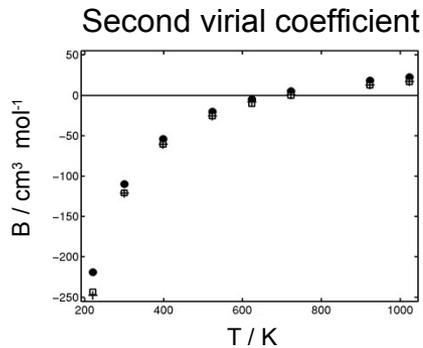
Lennard-Jones potential:  
Size and energy parameters

## Electrostatics

Point polarities  
(charge, dipole, quadrupole):  
Position and magnitude

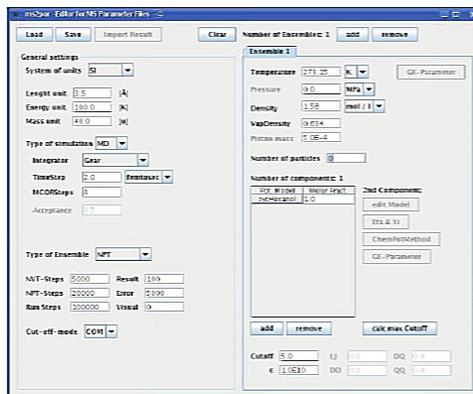


# Simulation of bulk properties with ms2

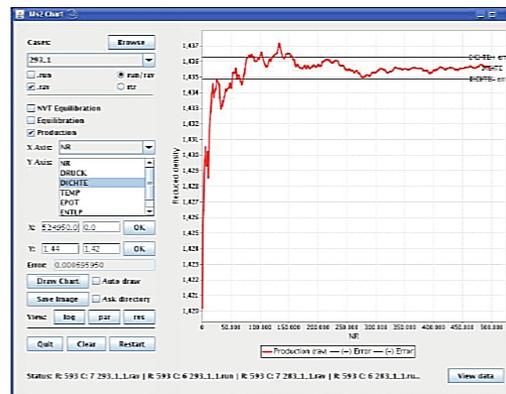


ms2 is freely available for academic use – register at <http://www.ms-2.de/>

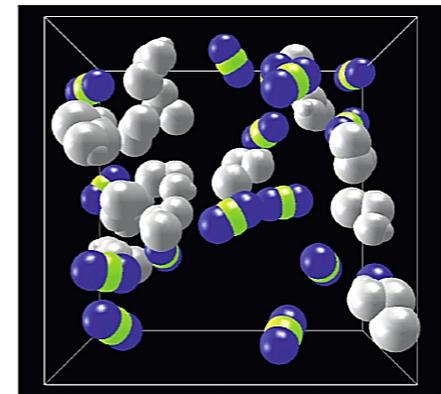
ms2par



ms2chart



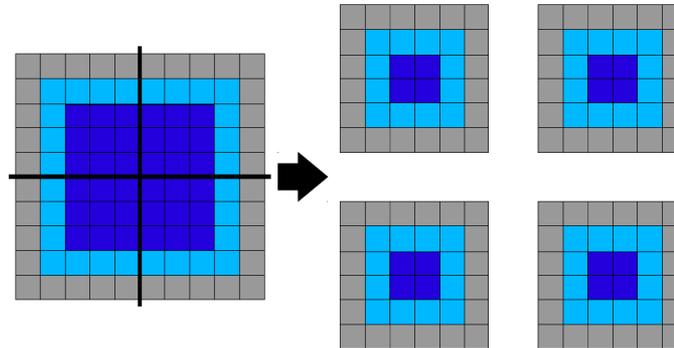
ms2molecules





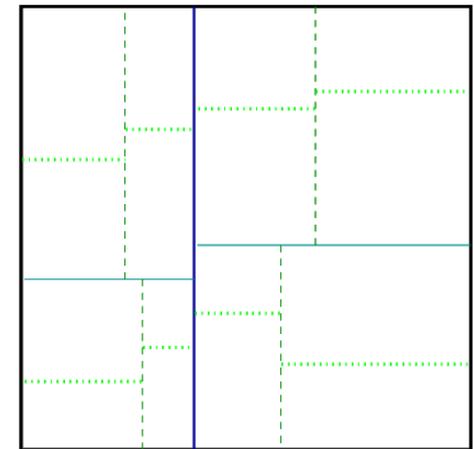
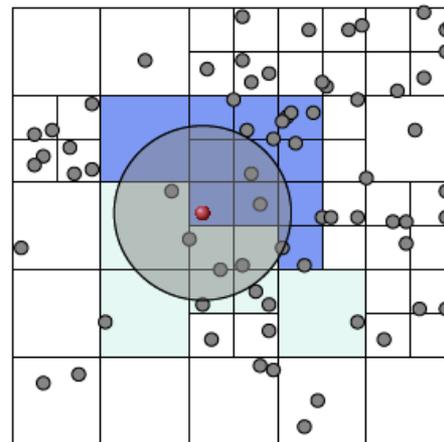
# Efficient simulation of large systems

Linked-cell data structure  
 suitable for spatial domain  
 decomposition:



(non-blocking, over-  
 lapping MPI send/  
 receive operations)

Methods for heterogeneous  
 or fluctuating particle  
 distributions:



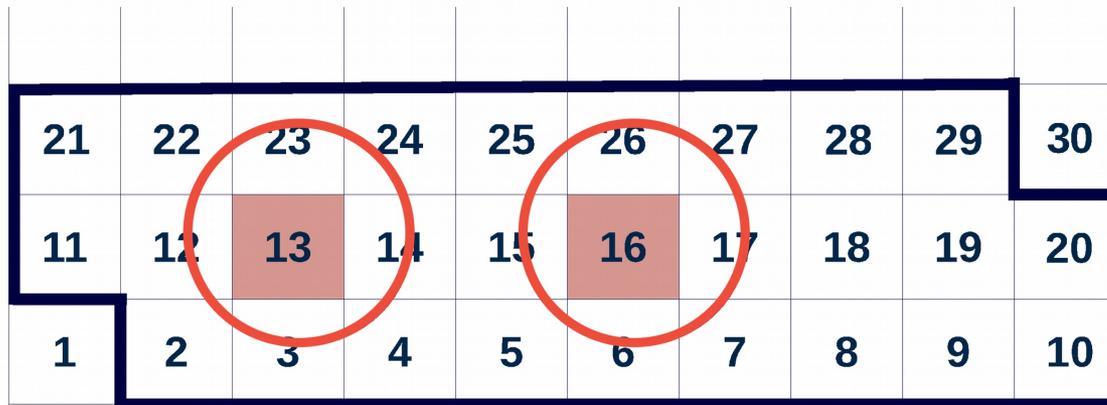
large systems “1”: molecular dynamics

<http://www.ls1-mardyn.de/>



# Efficient simulation of large systems

Memory-efficient implementation based on the linked-cell data structure:



hyperthreaded sliding window

Optionally, forces acting on molecules are only stored until their cell leaves the sliding window.

Efficient vectorization:

- Optimization by hand, using advanced vector extensions (AVX).
- Conversion from array of structures (AoS) to structure of arrays (SoA).

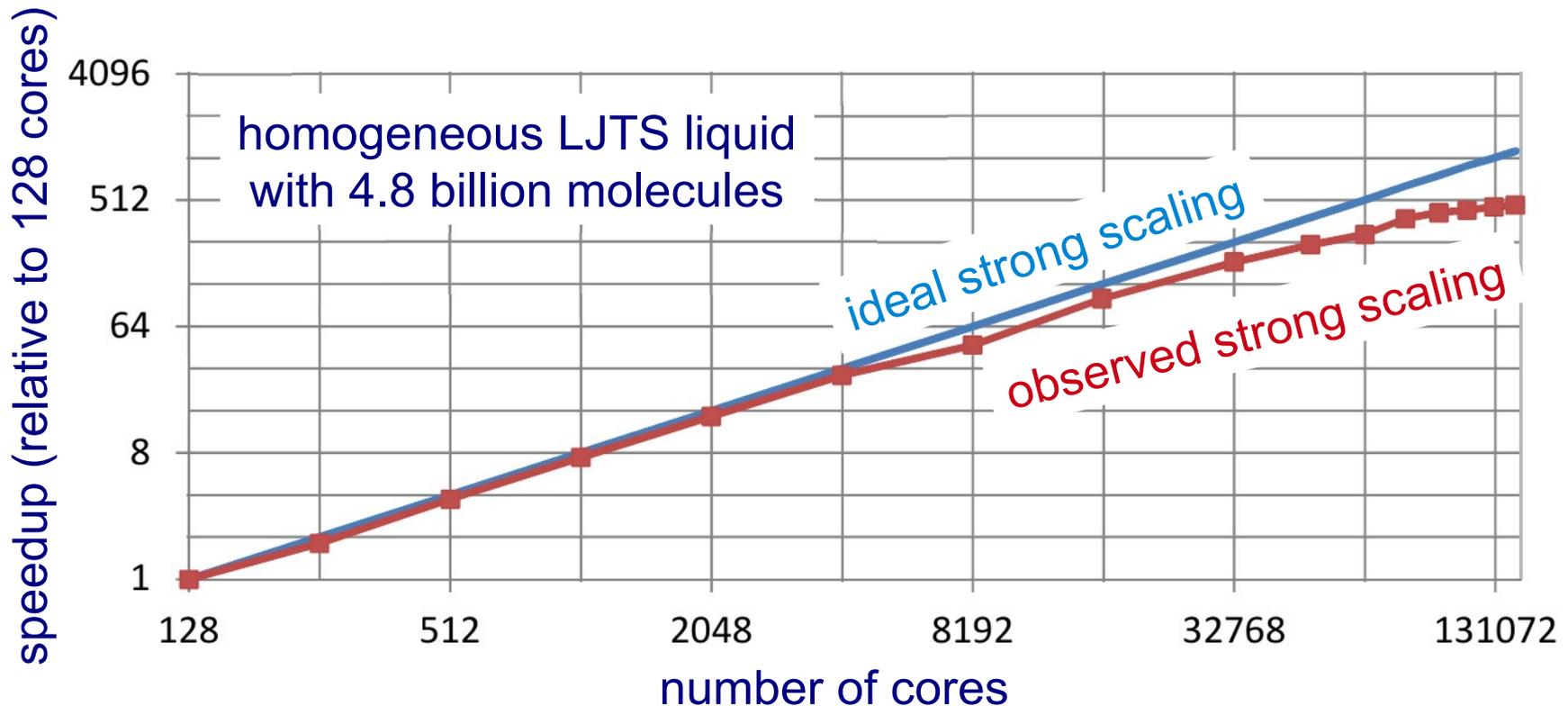
large systems “1”: molecular dynamics

<http://www.ls1-mardyn.de/>



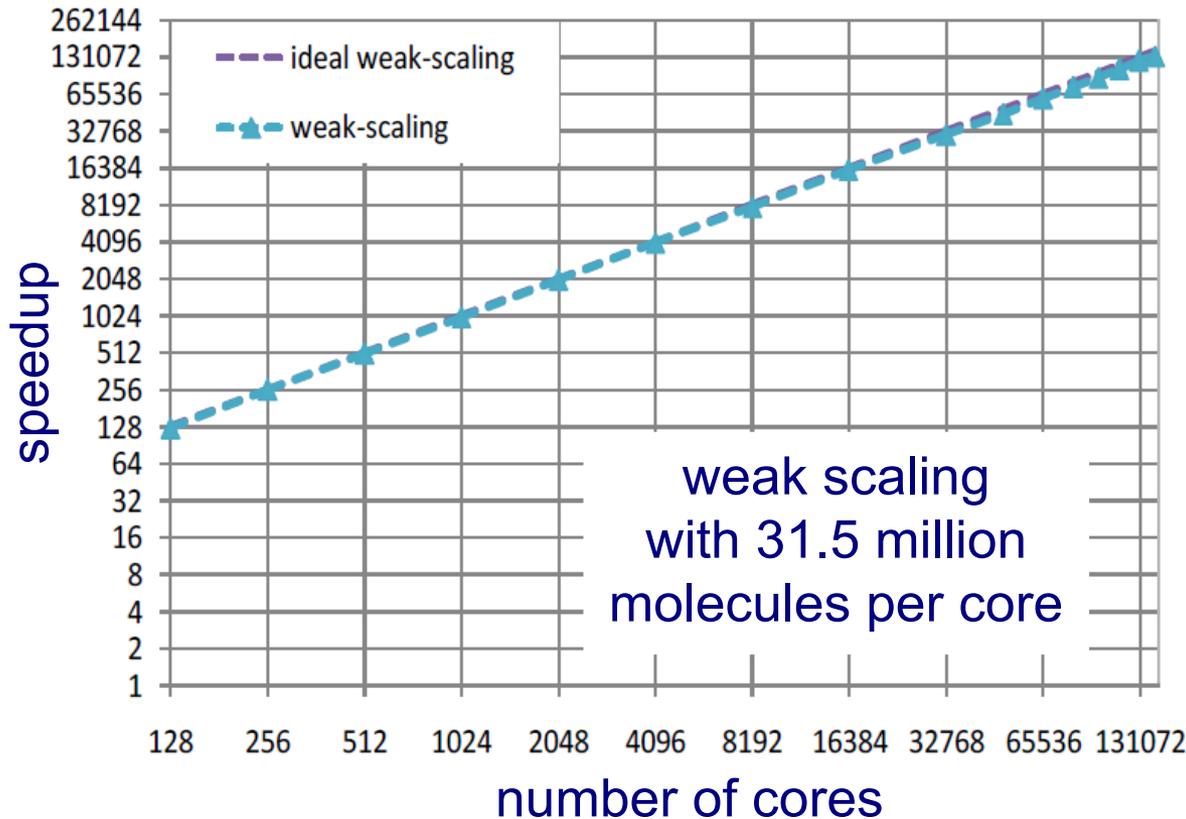
# Large-scale MD simulation on SuperMUC

Scaling of *Is1 mardyn* examined on up to 146 016 cores, i.e. the whole SuperMUC at the Leibniz Supercomputing Centre, Garching, in 2013.





# Large-scale MD simulation on SuperMUC



Up to  $N = 4 \cdot 10^{12}$   
on SuperMUC



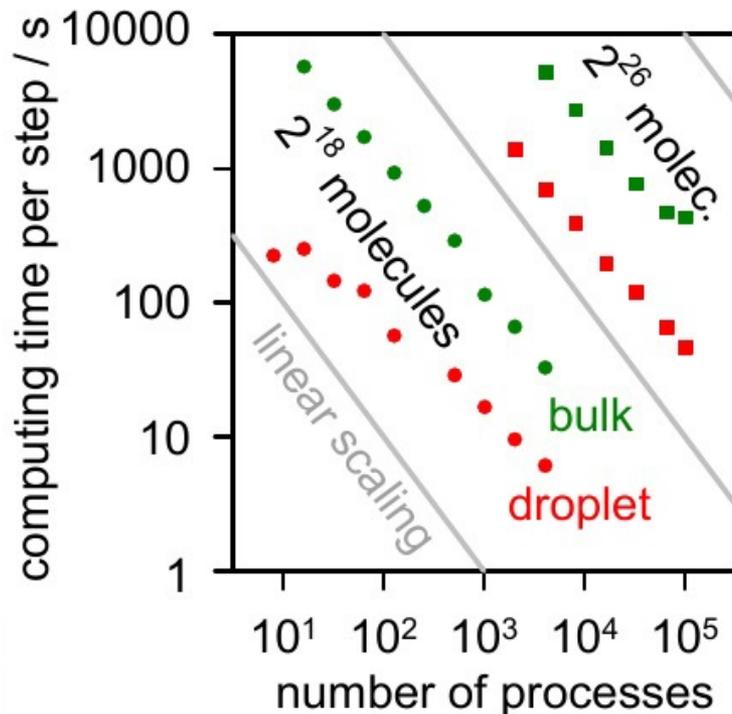
large systems "1": molecular dynamics

<http://www.ls1-mardyn.de/>

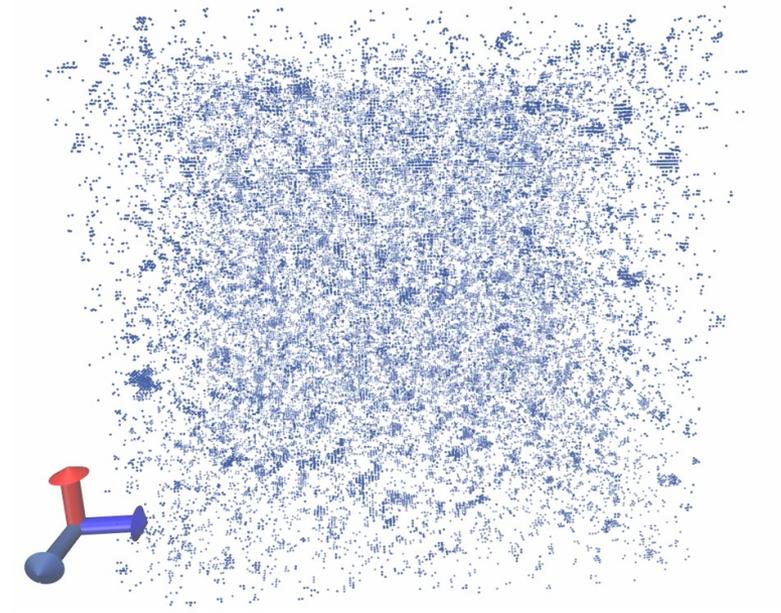


# Large-scale MD simulation on hermit

strong scaling (Amdahl)



homogeneous cavitation

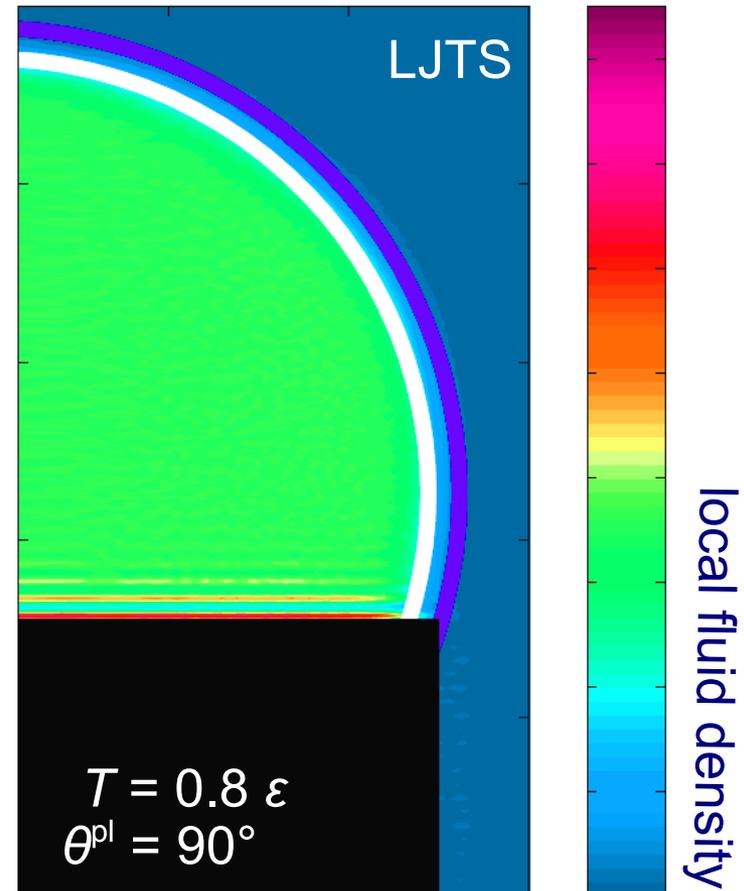
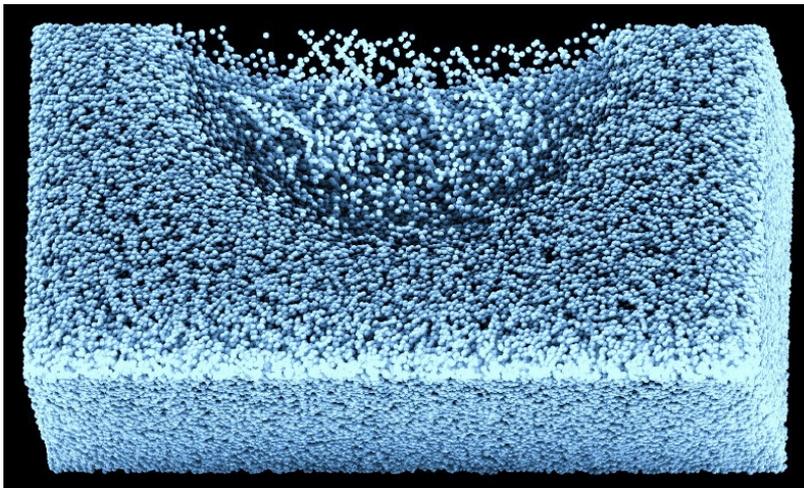


CO<sub>2</sub> ( $T = 280$  K and  $\rho = 17.2$  mol/l), 3CLJQ  
 100 million interaction sites, 110 592 cores



# Molecular simulation of fluids at interfaces

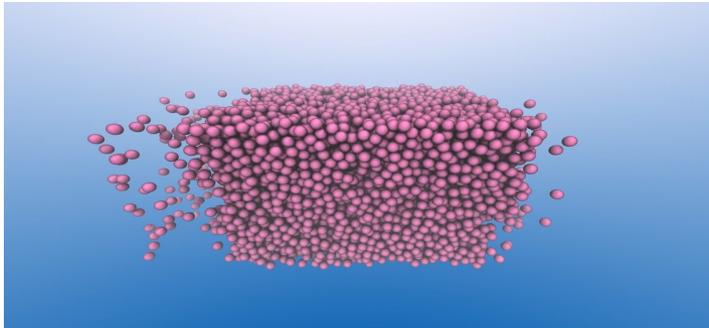
- Vapour-liquid surface tension
- Nucleation and dispersed phases
- Adsorption (fluid-fluid and fluid-solid)
- Contact angle and contact line pinning



# Long-range correction at planar interfaces

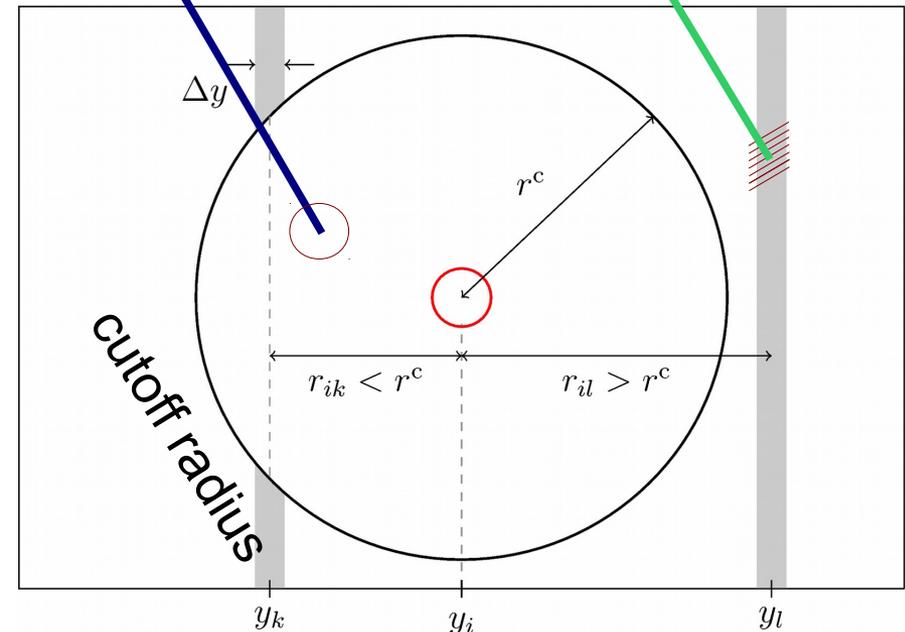
For planar interfaces:

**Long-range correction** from the density profile, following **Janeček**.



short range  
(explicit)

long range  
(correction)



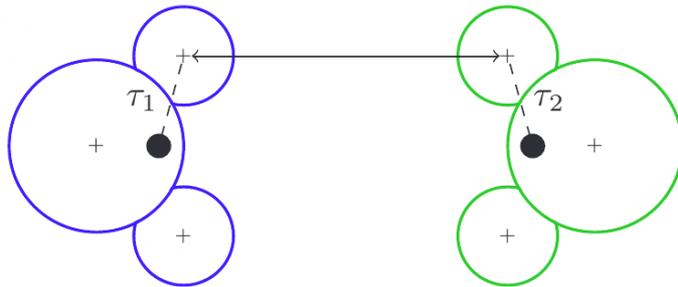
Full evaluation of all pairwise interactions is too expensive ...

... **short-range interactions** are evaluated only for **neighbours**.

# Long-range correction at planar interfaces

For planar interfaces:

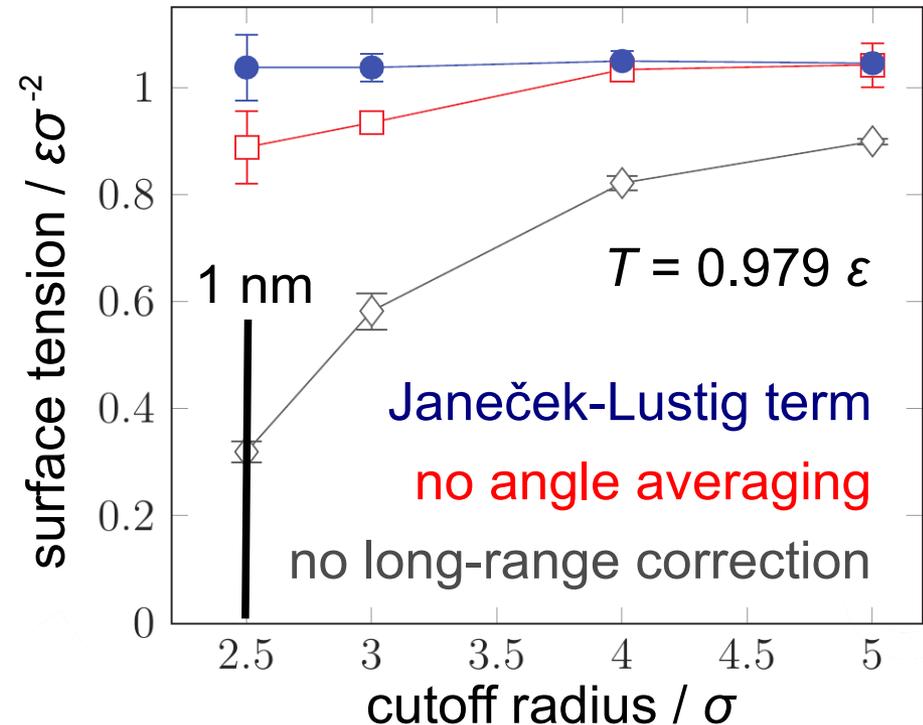
**Long-range correction** from the density profile, following **Janeček**.



**Angle-averaging** expression for multi-site models, following **Lustig**.

Dipole and dispersion lead to analogous long-range correction expressions. The long-range contribution of the quadrupole can be neglected.

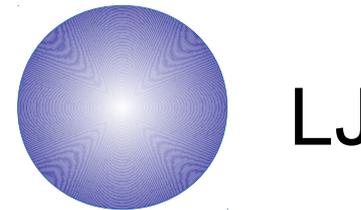
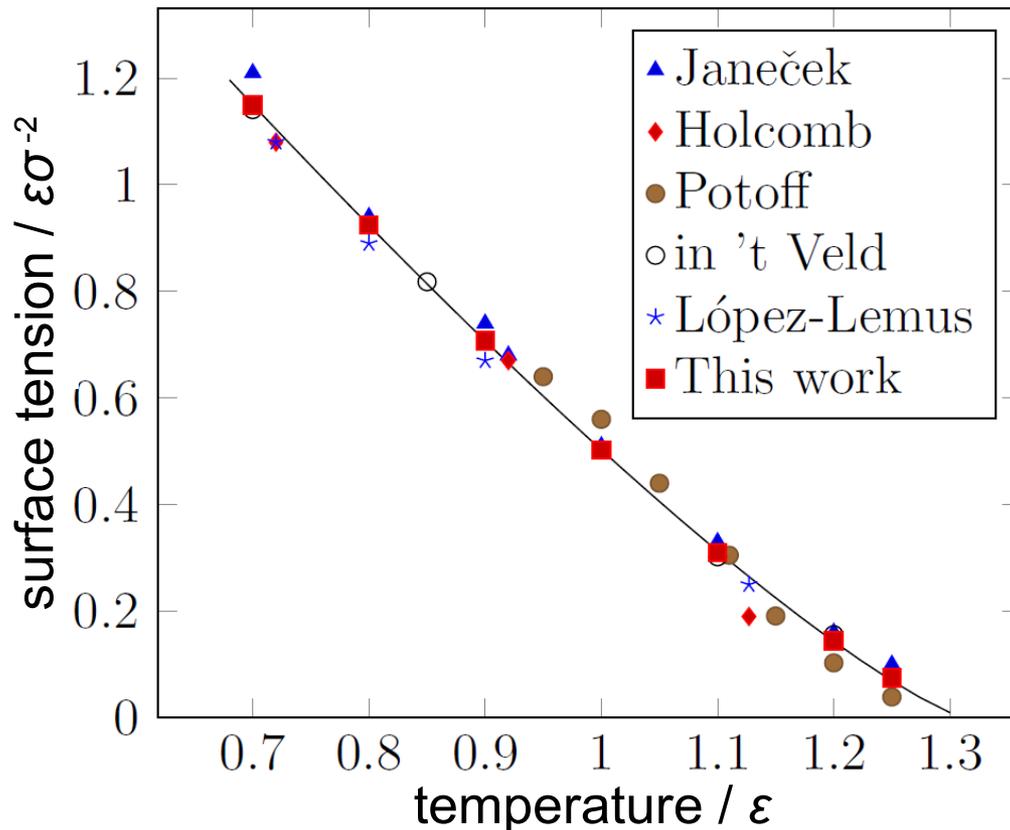
Two-centre LJ fluid (2CLJ)





# Surface tension at high precision

Lennard-Jones fluid

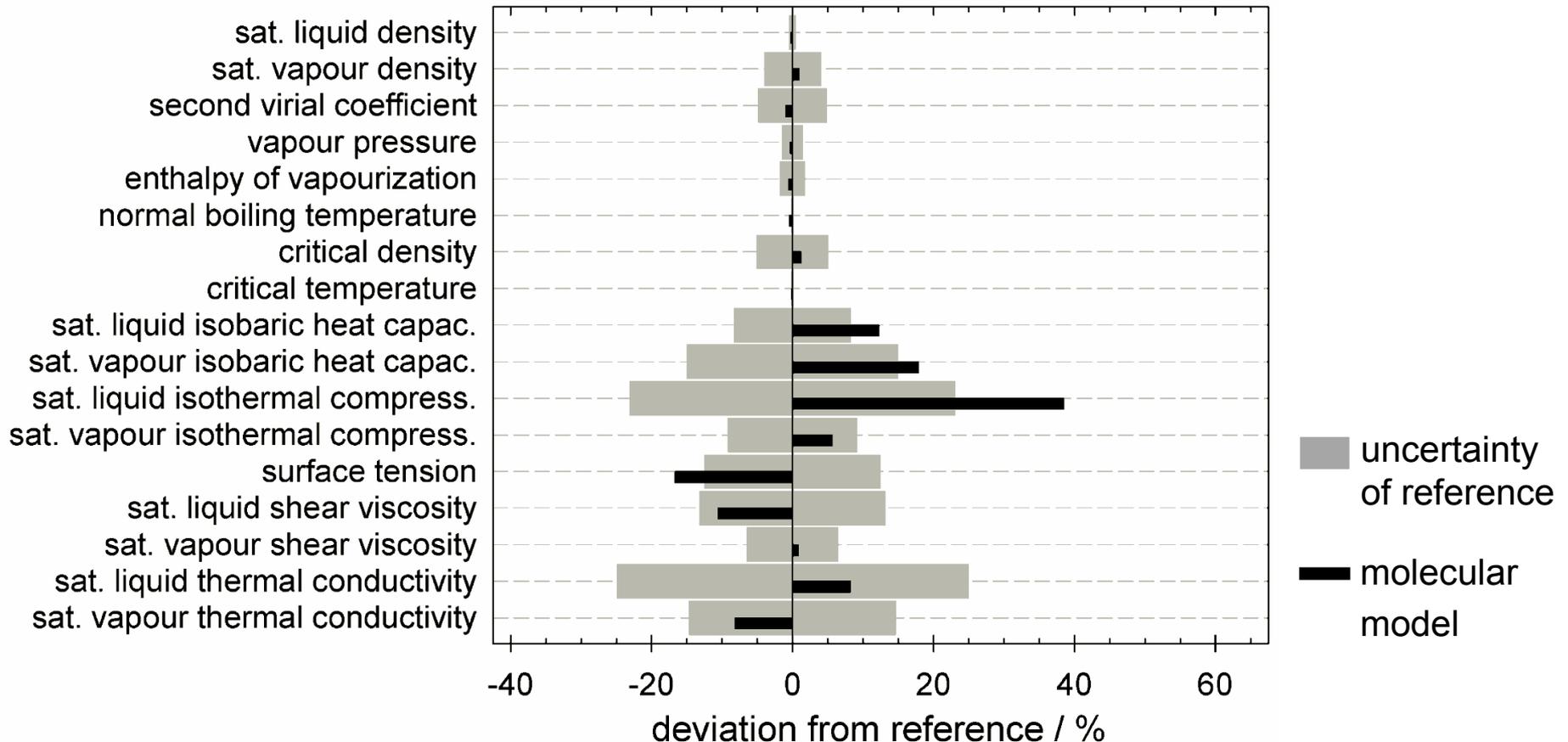


$$\gamma_0(T) = 2.94 \frac{\varepsilon}{\sigma^2} \left( 1 - \frac{T}{T_c} \right)^{1.23}$$

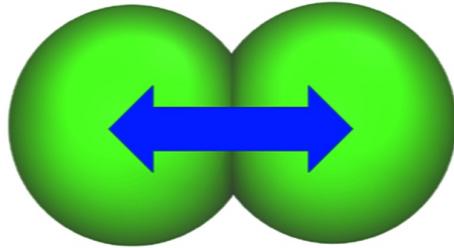


# Objective: Accuracy for multiple properties

ethylene oxide model by Eckl *et al.* (2008)



# Force fields for molecular modelling



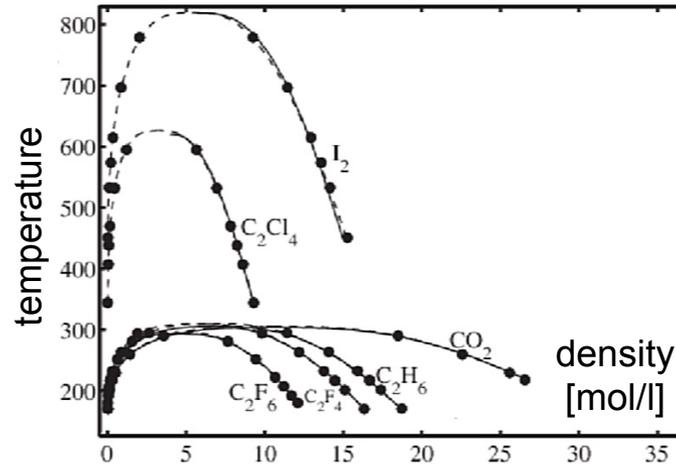
2CLJQ models:

- 2 LJ centres
- Quadrupole

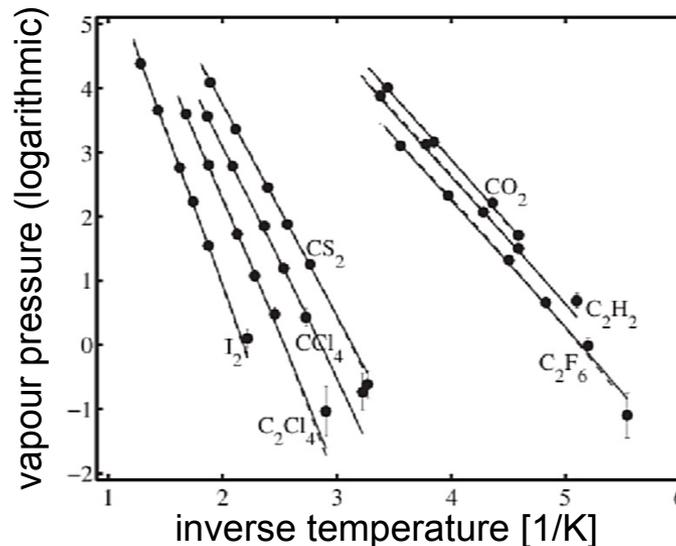
Fit of parameters  $\sigma$ ,  $\epsilon$ ,  $L$ ,  $Q$  to VLE data of 29 fluids by Stoll *et al.*

Deviation:

- $\delta\rho' \approx 1\%$
- $\delta P^{\text{sat}} \approx 5\%$



● simulation  
— DIPPR correlation

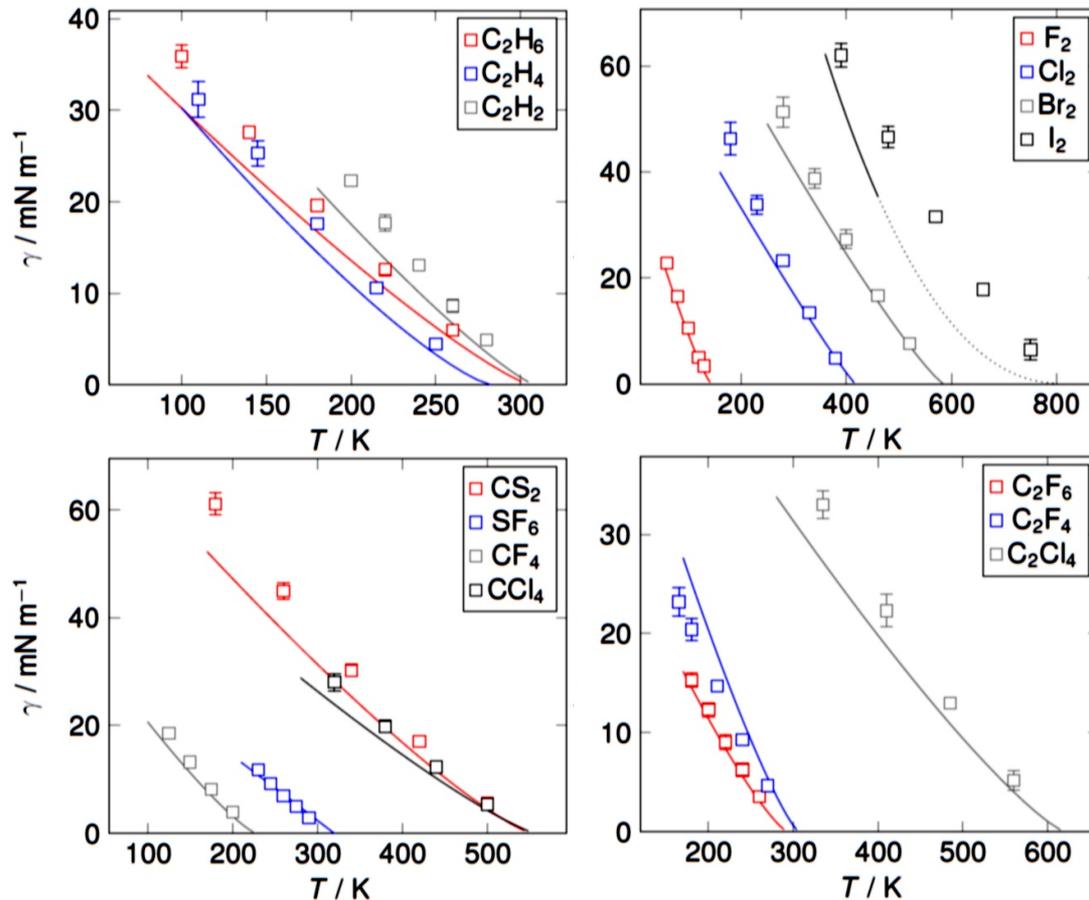


No interfacial properties were considered for the parameterization.

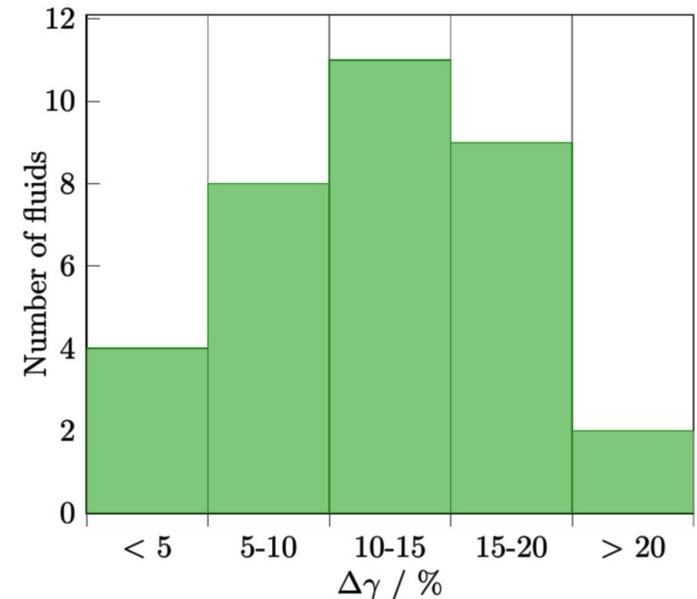


# Predictive capacity of literature models

Two LJ + quadrupole (2CLJQ)



Two LJ + dipole (2CLJD)

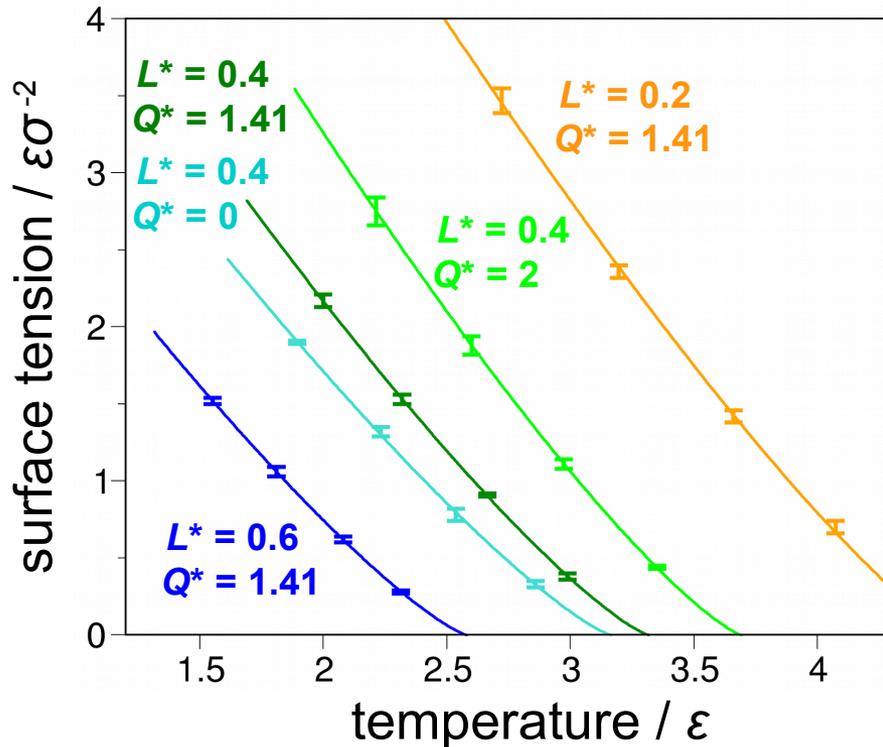


Fit to bulk properties  $\searrow$   
10 to 20 % overestimation of  
vapour-liquid surface tension

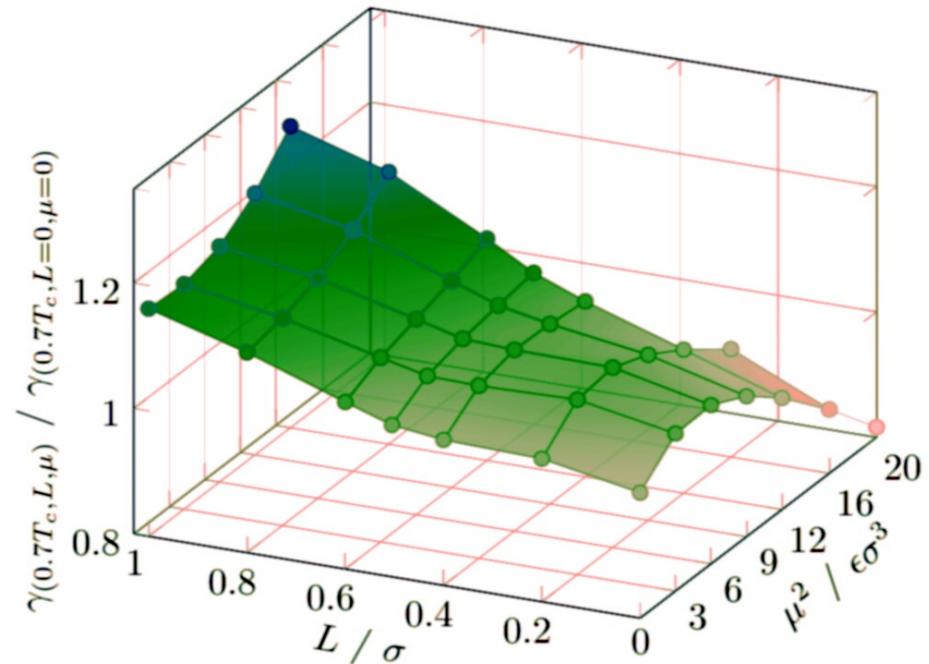


# Massively parallel molecular modelling

Two LJ + quadrupole (2CLJQ)



Two LJ + dipole (2CLJD)

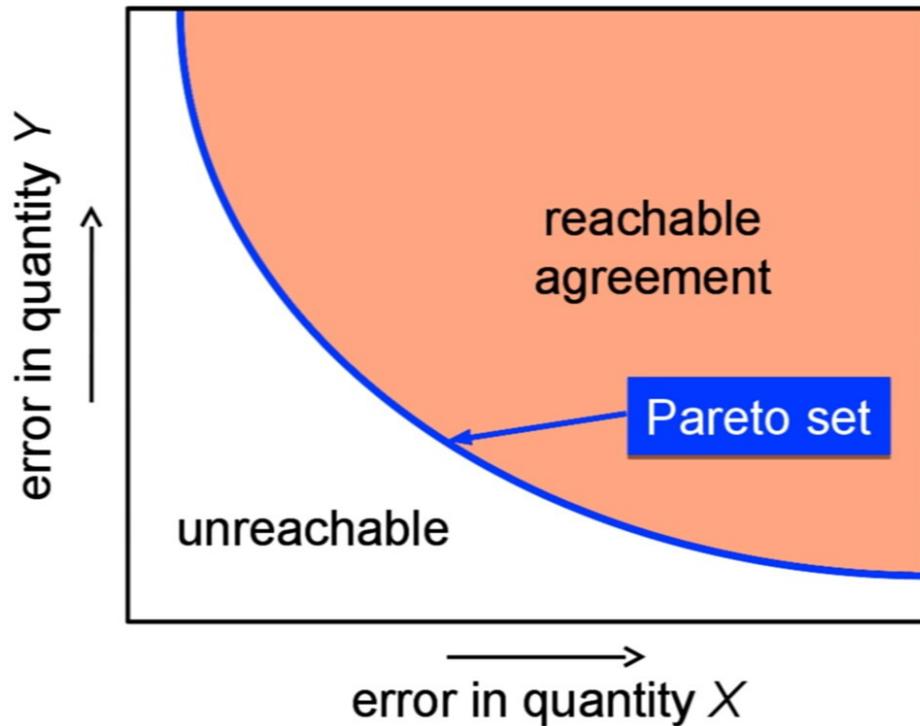


- Systematic exploration of the four-dimensional model parameter space
- Correlation of the surface tension by a critical scaling expression

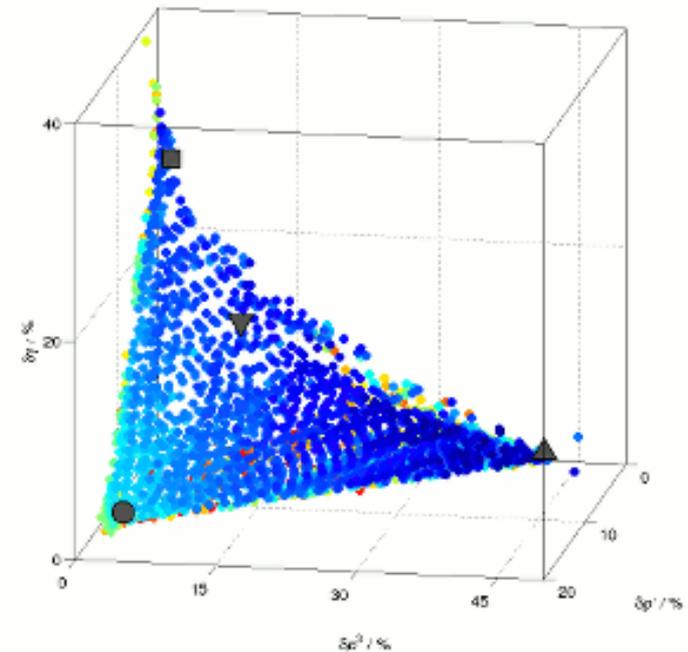


# Multicriteria model optimization

Pareto optimality criterion



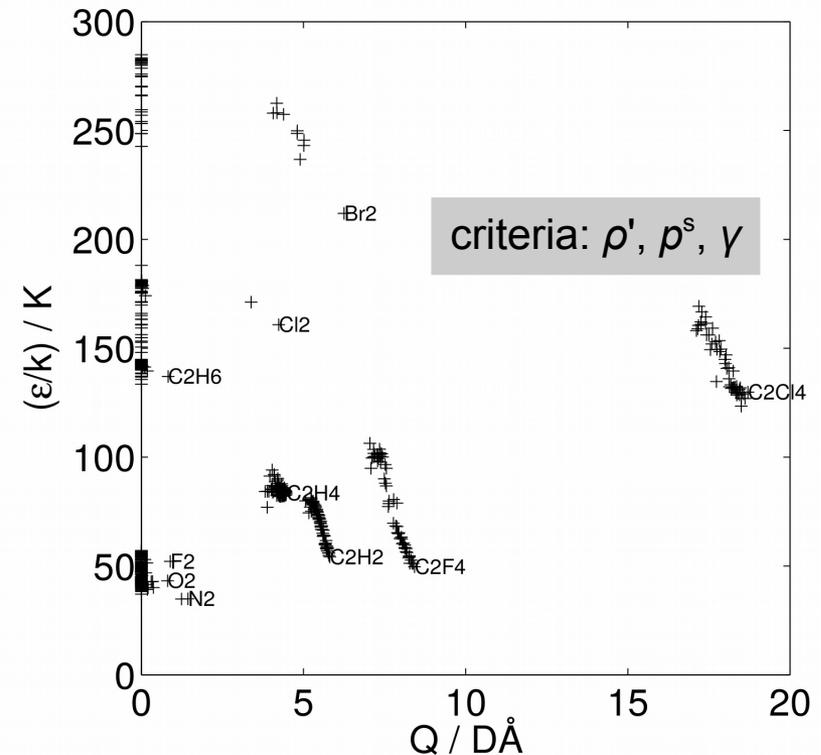
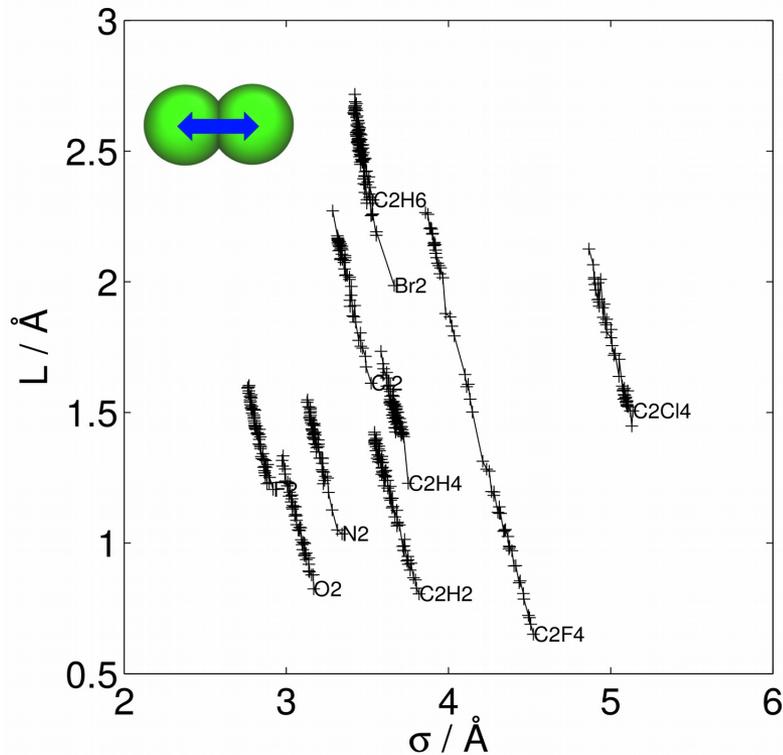
Pareto set for carbon dioxide



Multicriteria optimization requires massively-parallel molecular modelling.



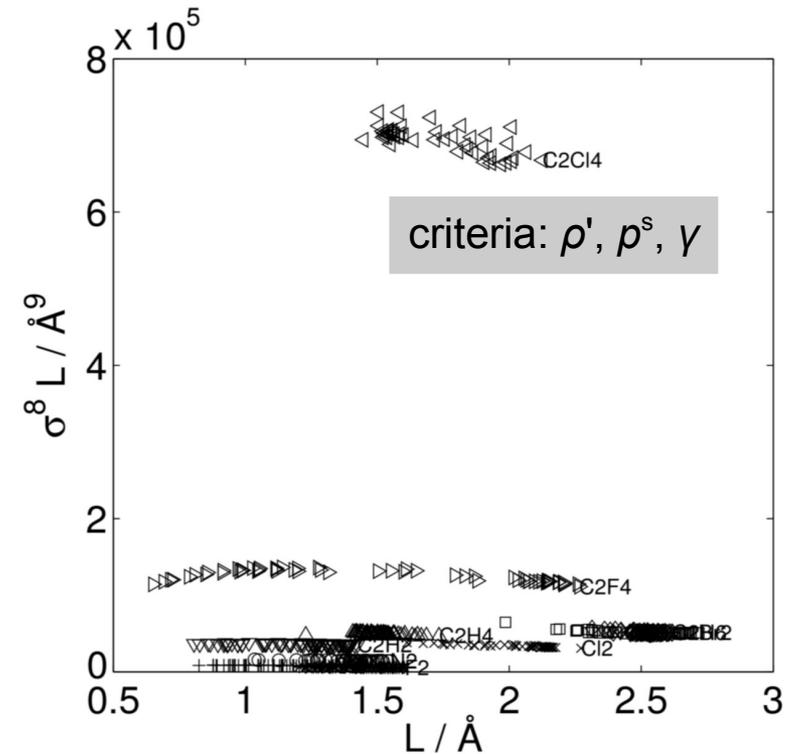
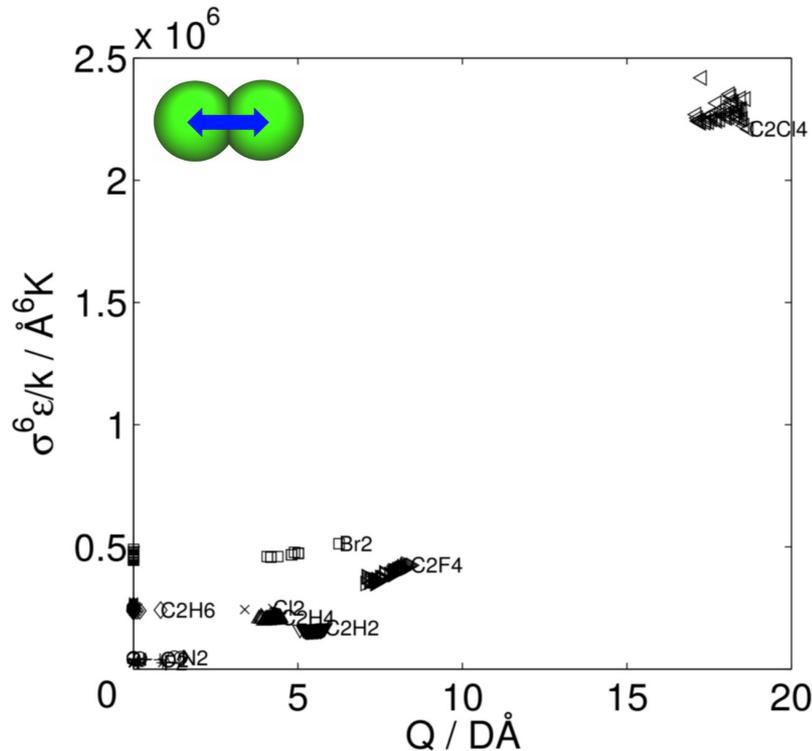
# Pareto sets for 2CLJQ models of real fluids



Projections of the Pareto set on the parameter space reveal intrinsic correlations between different model parameters, such as  $\epsilon$  and  $Q$ .



# Pareto sets for 2CLJQ models of real fluids

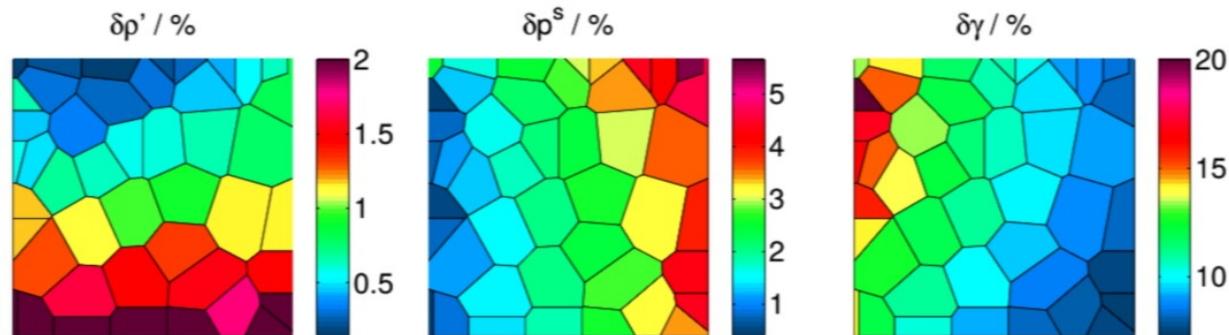


The dimension of the parameter space is effectively reduced, facilitating an efficient multicriteria optimization by navigating on the Pareto set.

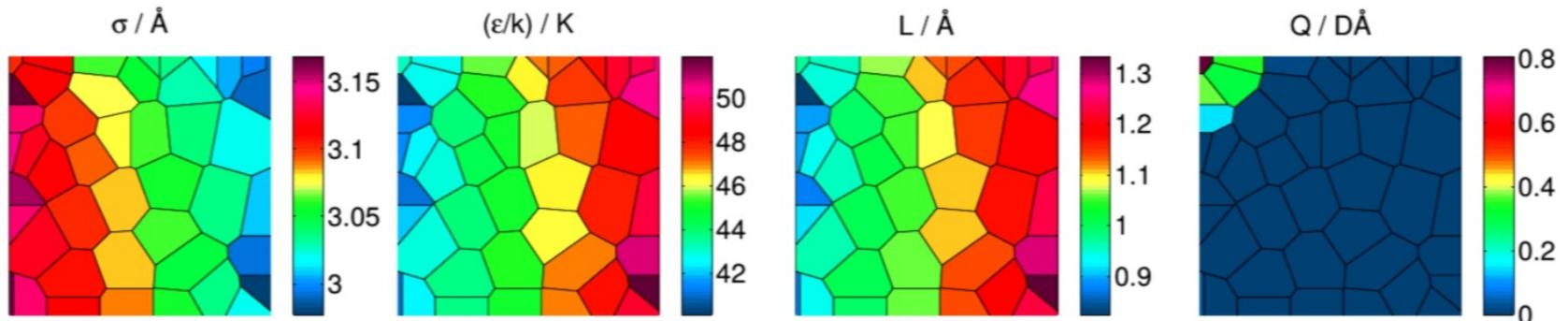


# Pareto sets for 2CLJQ models of real fluids

Representation of objective and parameter spaces by **patch plots**:

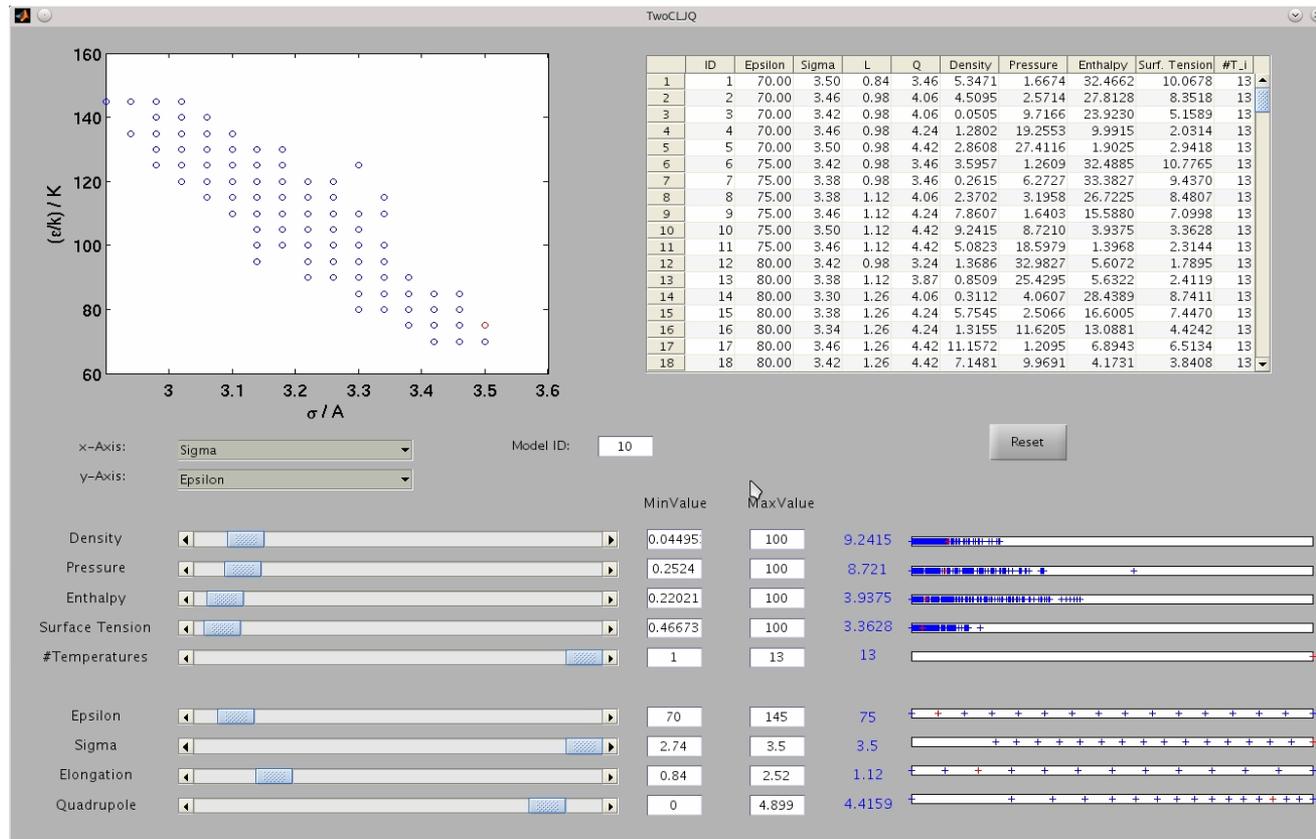


Pareto-optimal 2CLJQ models for molecular oxygen





# Fast and simple model parameterization





# Summary

## The traditional art of molecular modelling

An **expert modelling artist** designs and publishes

- a single optimized model for a particular fluid,
- according to his choice of criteria (often unknown to the public),
- users are passive, they have to live with the artists' decision.

## Scientific modelling by multicriteria optimization

For established model classes and multiple thermodynamic criteria,

- the dependence of thermodynamic properties on the model parameters is determined and correlated,
- the deviation between model properties and real fluid behaviour is characterized, and the Pareto set is published,
- users can design their own tailored model **with minimal effort**.