



# Molecular simulation and theory of homogeneous cavitation

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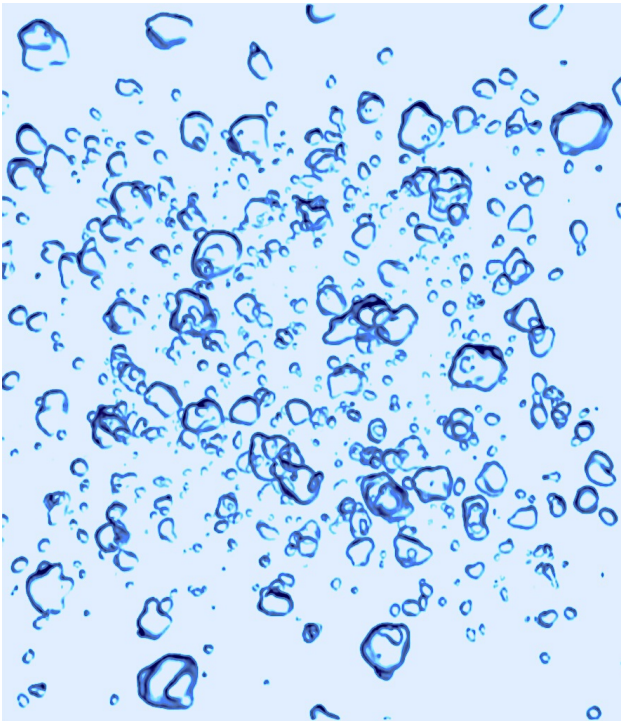


**ProcessNet MolMod Conference**  
**Frankfurt am Main, 10<sup>th</sup> March 2017**

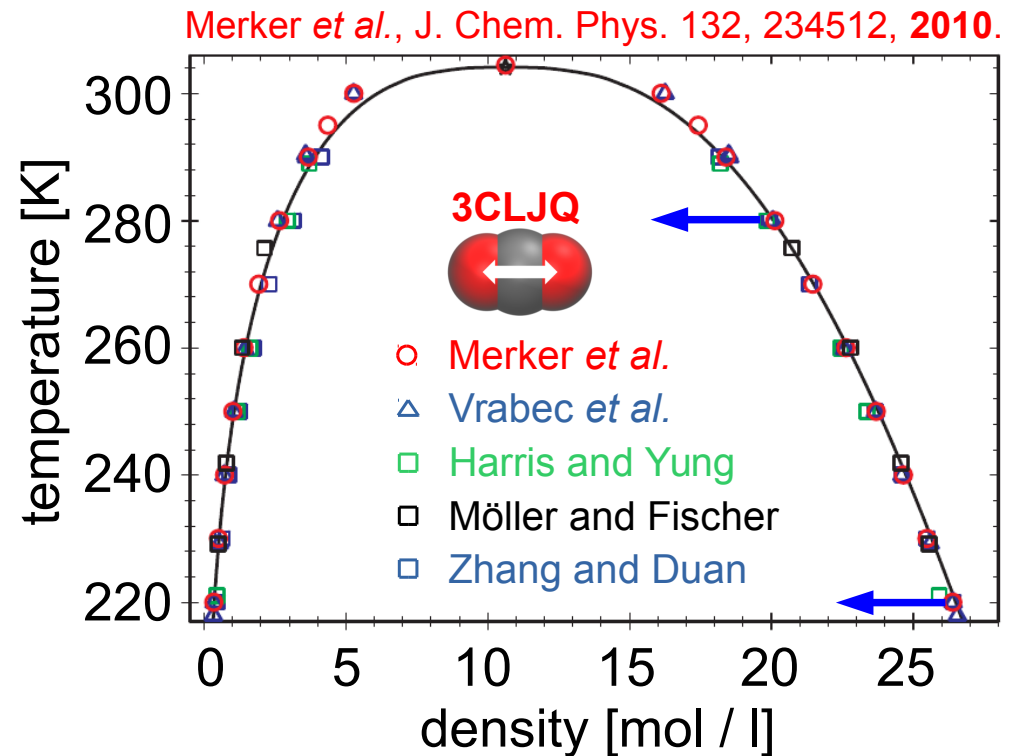
**Computational  
Molecular Engineering**

# Homogeneous liquid to vapour nucleation

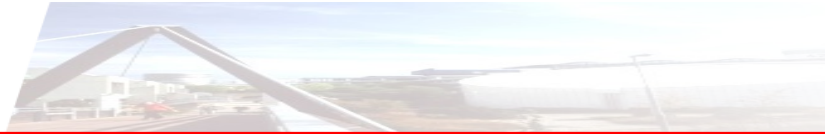
## Bubble formation



## Carbon dioxide



MD simulation of nucleation requires large systems and performant codes.



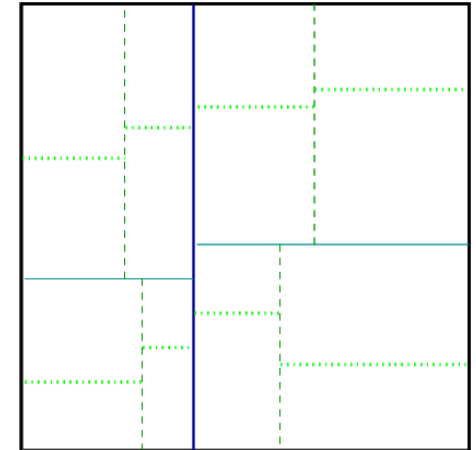
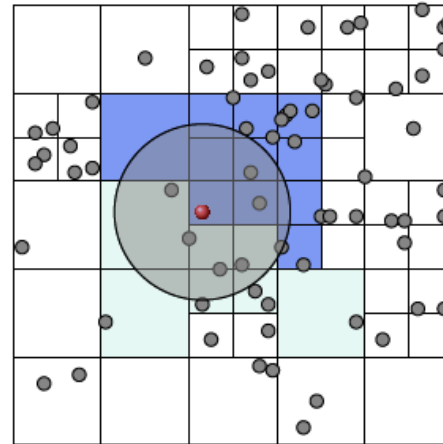
# Scalable molecular dynamics simulation

Collaboration within

**IMEMO** (2008 – 2011)

**SkaSim** (2013 – 2016)

**TaLPas** (2017 – 2020)



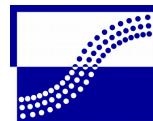
Bundesministerium  
 für Bildung  
 und Forschung



The Chemical Company



**SkaSim**



Lehrstuhl für Thermodynamik  
 Prof. Dr.-Ing. H. Hasse



Technische Universität München



**ThEt**  
 UNIVERSITÄT PADERBORN  
 Die Universität der Informationsgesellschaft





# Scalable molecular dynamics simulation

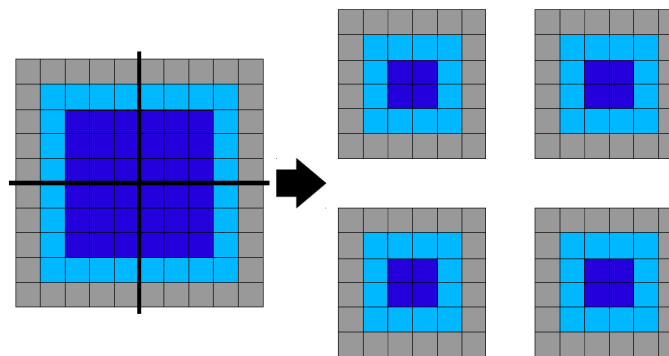
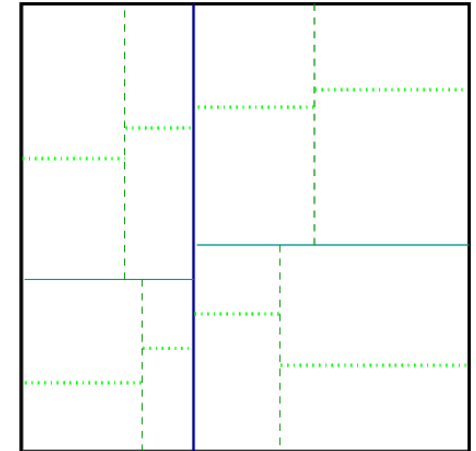
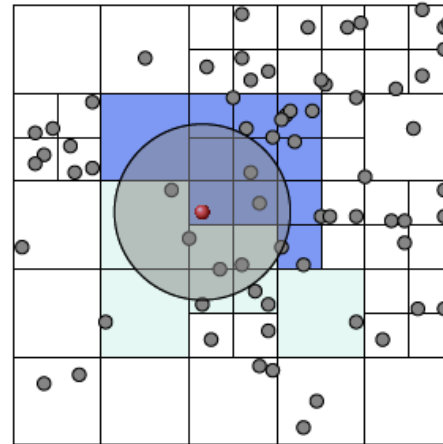
Spatial domain  
decomposition

Dynamic load balancing

Communication (almost) only  
with neighbour processes

Linked-cell data structure  
near-field pair potentials

Summation techniques, e.g.  
Janeček, FMM, for far field



(non-blocking,  
overlapping MPI  
send/receive  
operations)

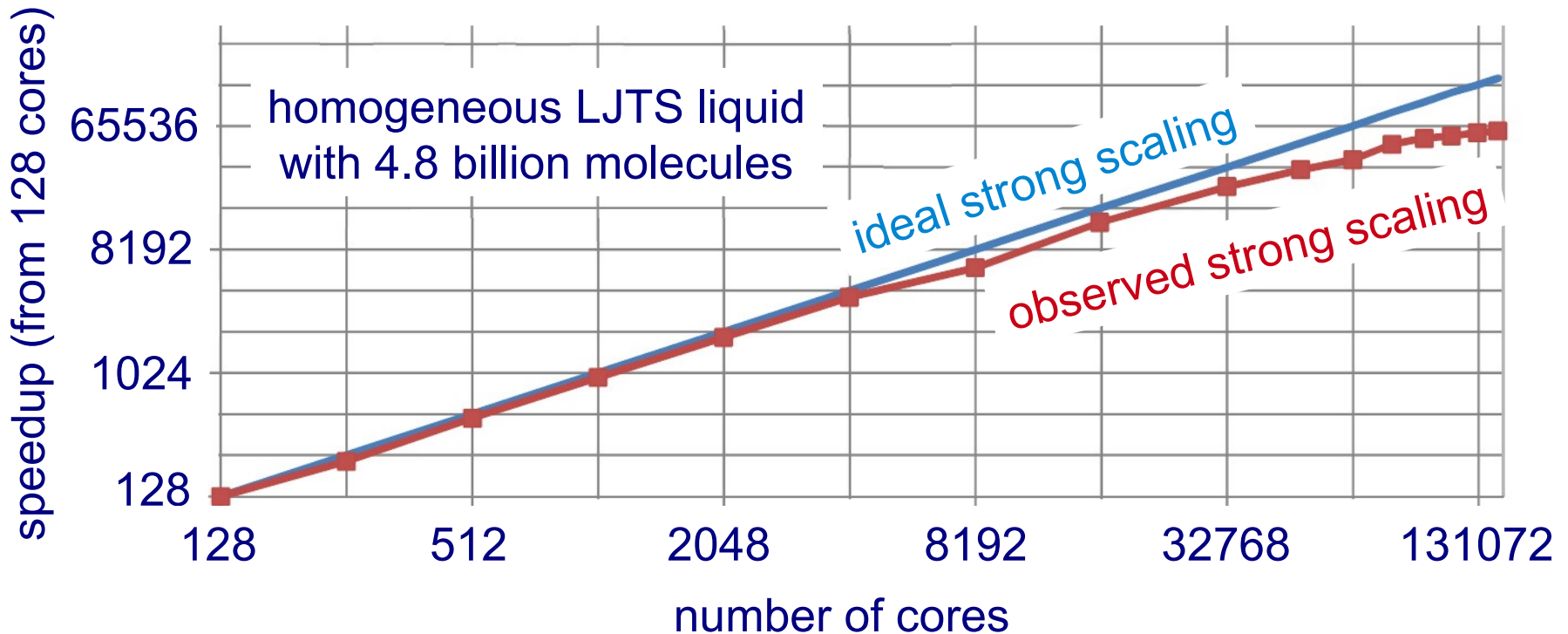
large systems “1”: molecular dynamics

<http://www.ls1-mardyn.de/>



# Scalable molecular dynamics simulation

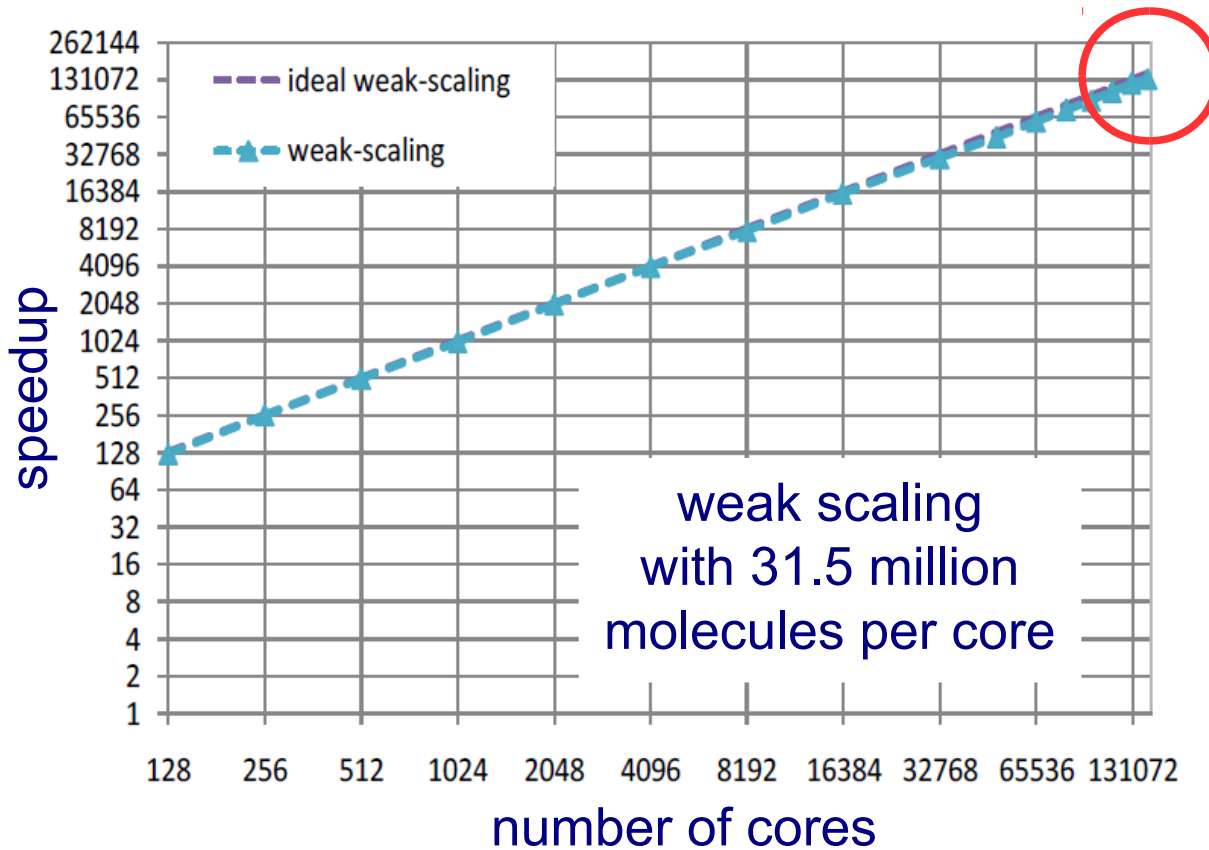
Scaling of *Is1 mardyn* examined on SuperMUC up to 146 016 cores.<sup>1</sup>



<sup>1</sup>W. Eckhardt, A. Heinecke, *et al.*, *Proceedings of ISC 2013*, Springer, LNCS 7905, 1 – 12, **2013**.



# Scalable molecular dynamics simulation



Up to  $N = 4 \cdot 10^{12}$   
on SuperMUC<sup>1</sup>



<sup>1</sup>Eckhardt *et al.*, *ISC 2013*, LNCS 7905, 1 – 12, **2013**.

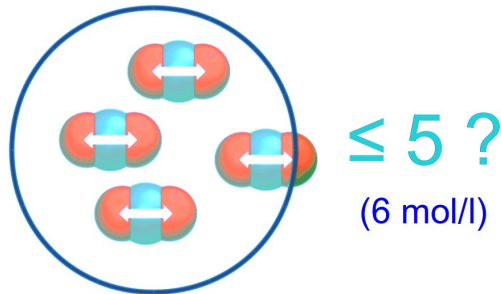
MD simulation world record achieved for a liquid Lennard-Jones system.<sup>1</sup>



# Bubble formation in metastable liquid CO<sub>2</sub>

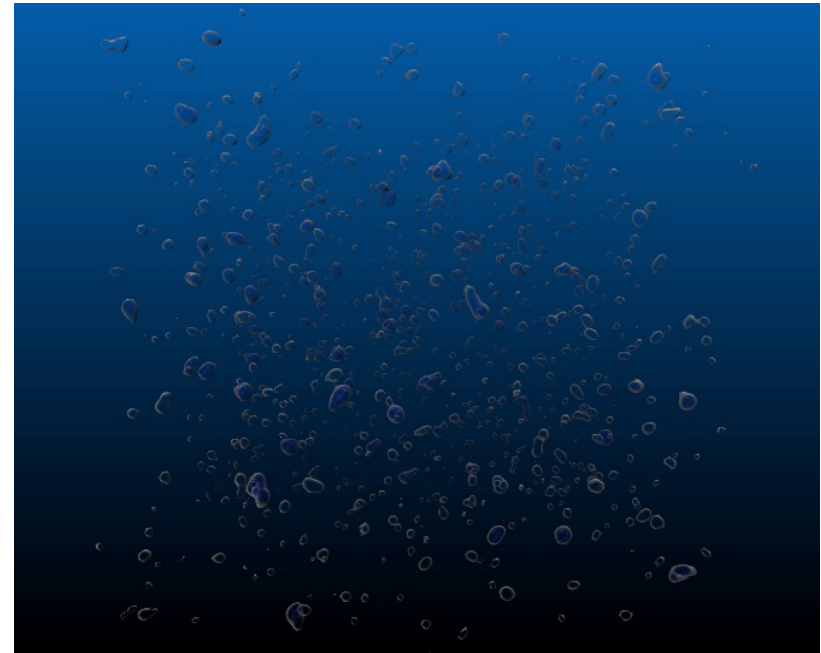
Canonical MD simulation of cavitation in carbon dioxide.

Evaluation of local density at 180 x 180 x 180 grid points:



Liquid phase: More than five neighbours present within a radius of 6.9 Å around the grid point.

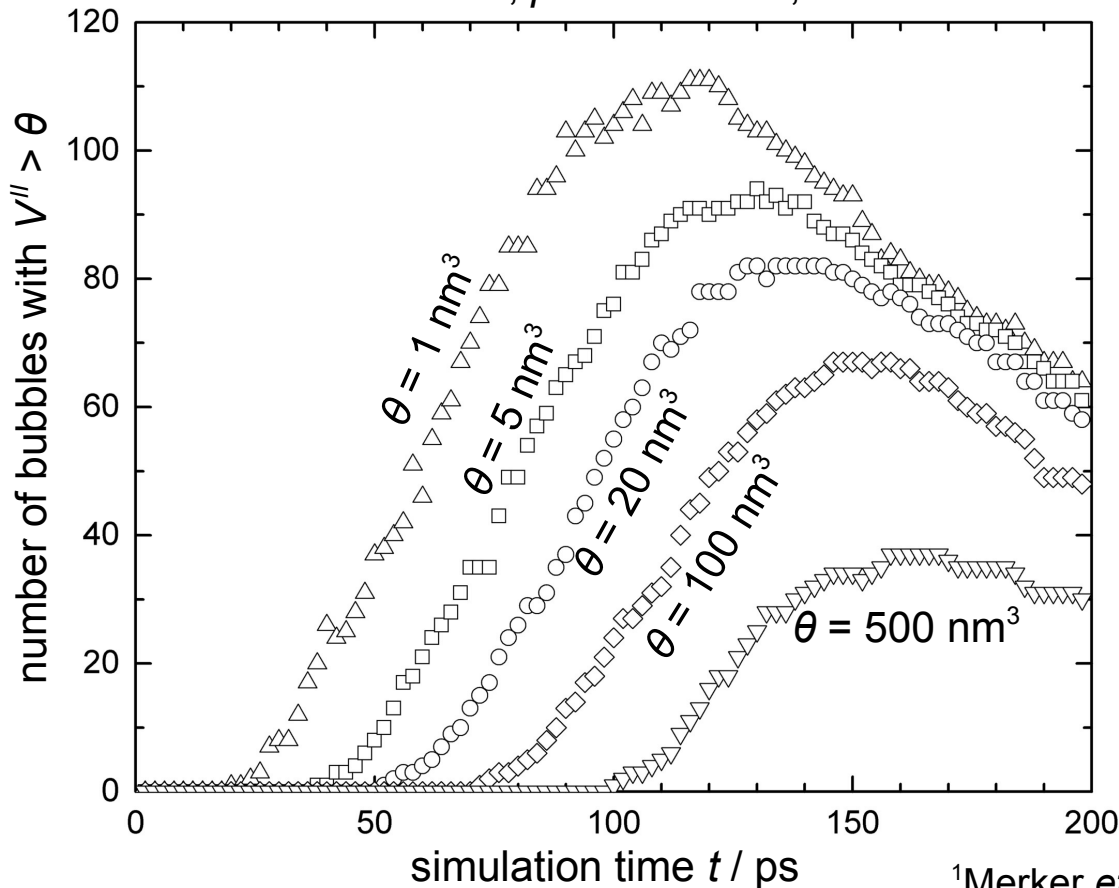
metastable liquid carbon dioxide



up to 100 million interaction sites

# Nucleation rate from population statistics

$N = 13\,000\,000$ ,  $\rho = 23.6$  mol/l,  $T = 220$  K



Observation of

- metastable relaxation,
- nucleation,
- growth of supercritical bubbles,
- ripening / coalescence

$\theta = 1, 2, 5, 10, 20, 50,$   
 $100, 200, \text{ and } 500 \text{ nm}^3$

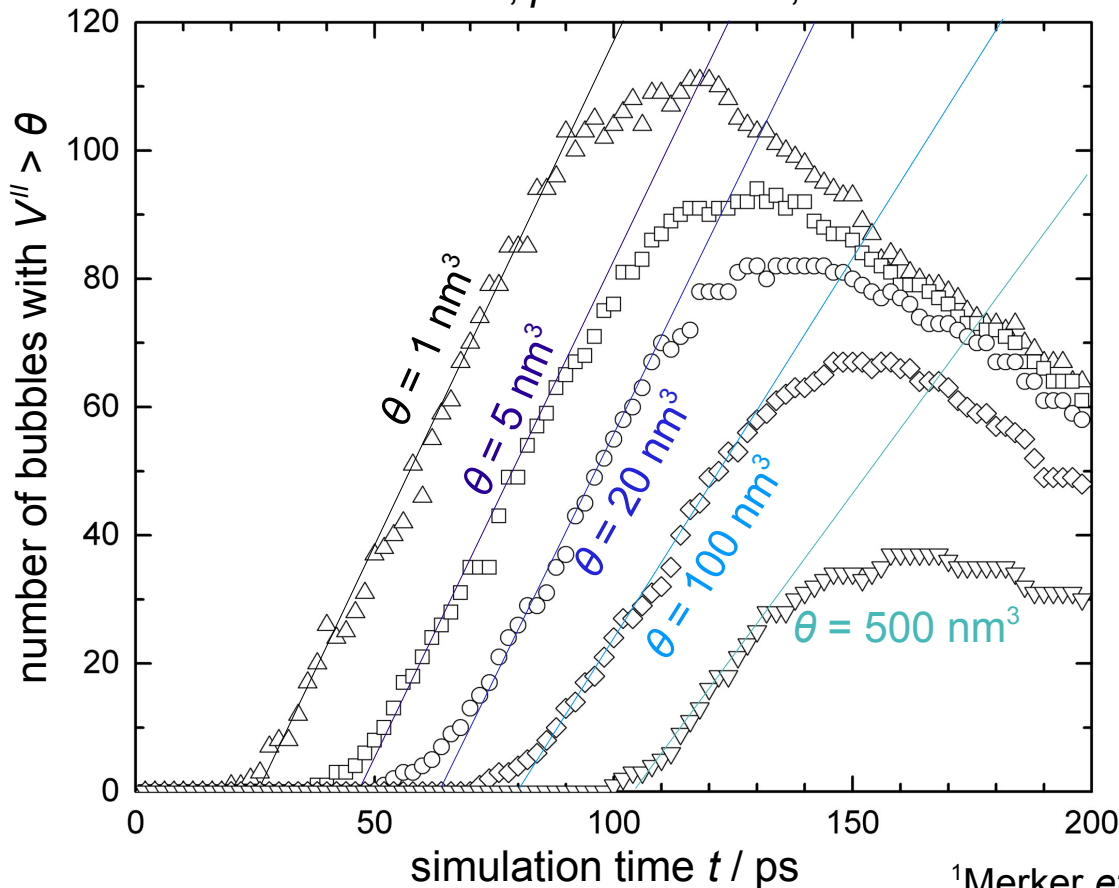
3CLJQ model by Merker  
*et al.*<sup>1</sup> for carbon dioxide

<sup>1</sup>Merker *et al.*, *J. Chem. Phys.* 132, 234512, 2010.



# Nucleation rate from population statistics<sup>2</sup>

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<sup>1</sup>Merker *et al.*, *J. Chem. Phys.* 132, 234512, 2010;

<sup>2</sup>Yasuoka and Matsumoto, *J. Chem. Phys.* 109, 8451, 1998.

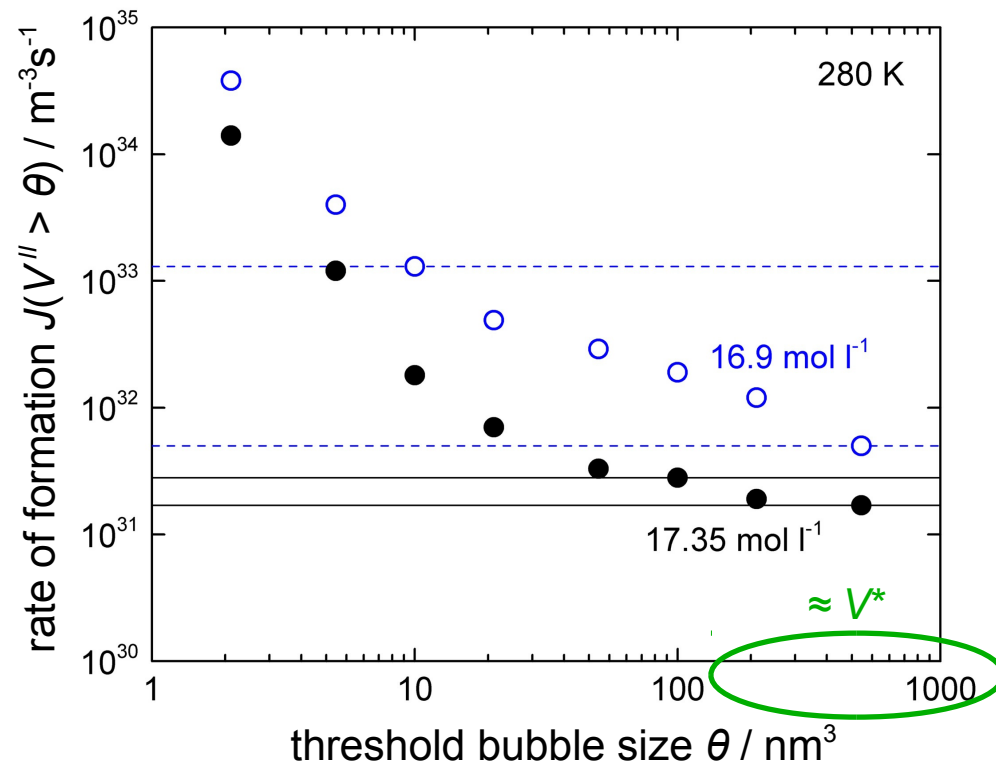


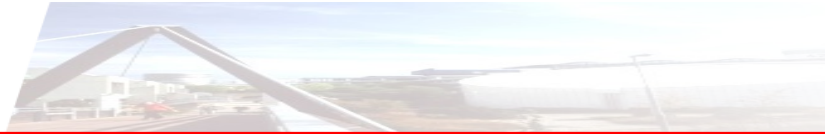
# Nucleation rate from population statistics

**Objective:** Determine the macroscopic nucleation rate  $J$ .

The rate of formation  $J(V'' > \theta)$  from the method of Yasuoka and Matsuomoto depends on the threshold size  $\theta$ .

Two types of finite-size effects are present, due to bubble size and due to system size.





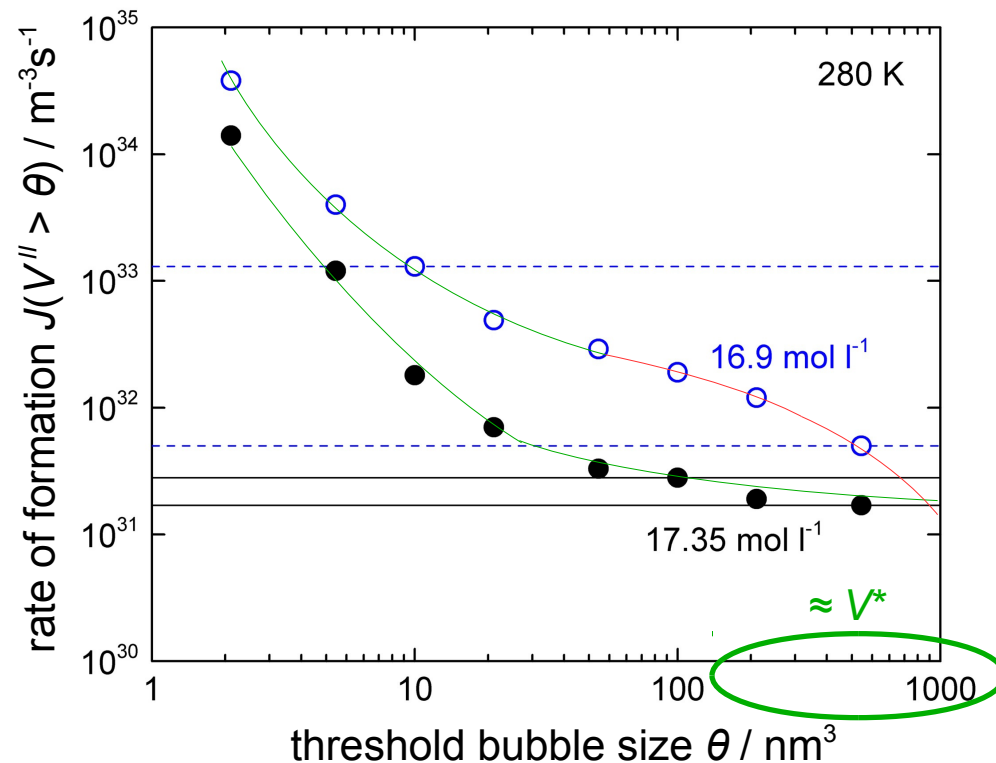
# Nucleation rate from population statistics

Subcritical bubbles are formed at a higher rate.

**Objective:** Determine the macroscopic nucleation rate  $J$ .

The rate of formation  $J(V'' > \theta)$  from the method of Yasuoka and Matsuomoto depends on the threshold size  $\theta$ .

Two types of finite-size effects are present, due to **bubble size** and due to **system size**.

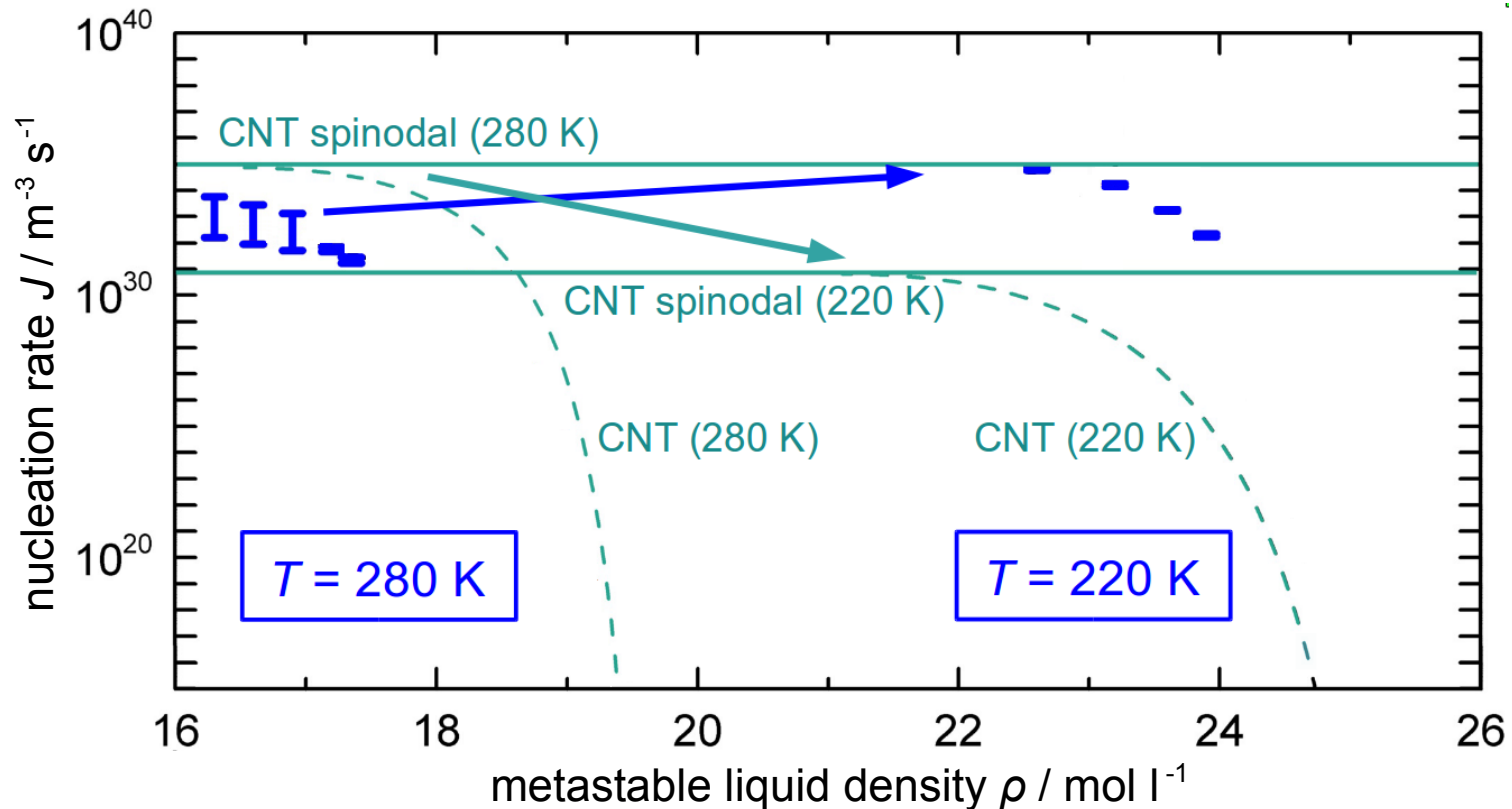


For large bubbles, the rate of formation is limited by the system volume.

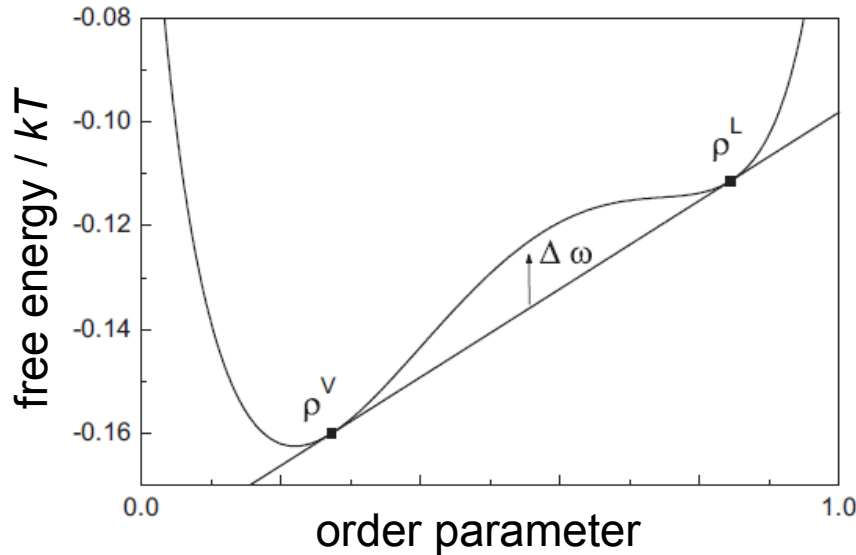


# Comparison to classical nucleation theory

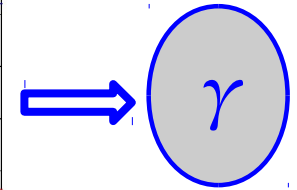
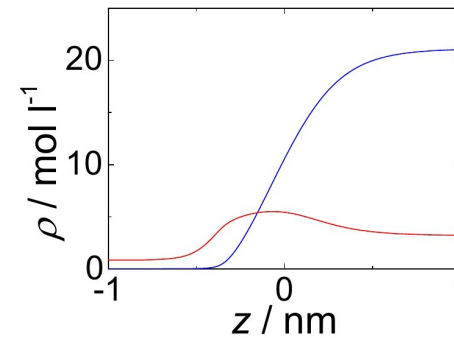
**CNT** → capillarity approximation  
 $\gamma = \gamma_{\text{planar}}(T)$  independent of the bubble radius



# Density gradient theory



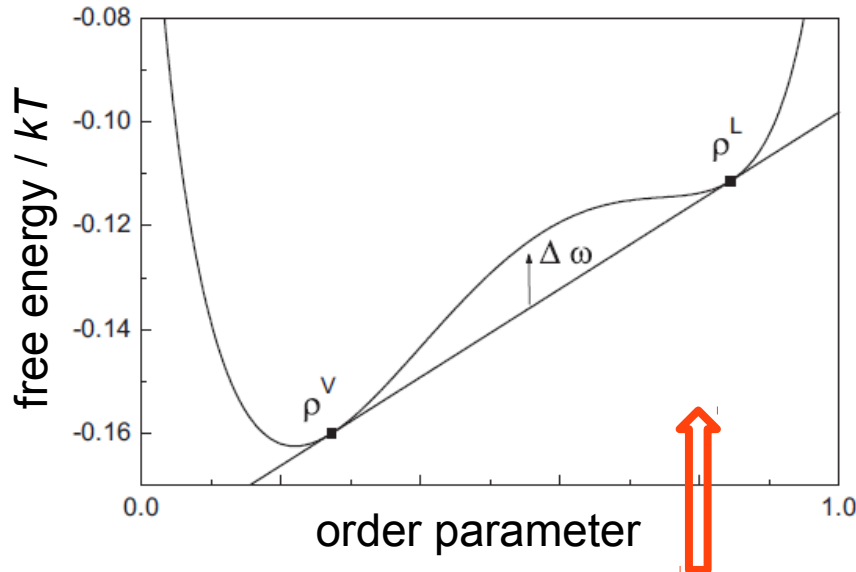
$\Rightarrow$   
 $+ \kappa (\nabla \rho)^2$



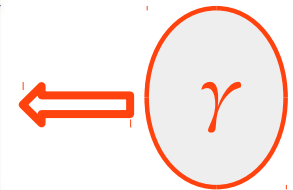
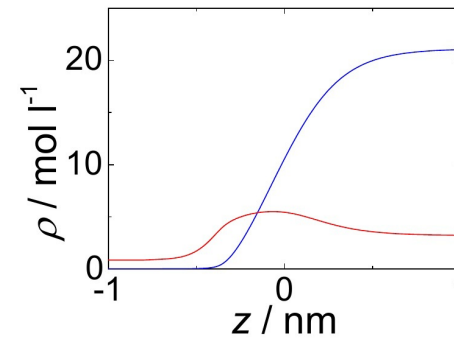
- <sup>1</sup>L. D. Landau, E. M. Lifshitz, *Phys. Z. Sowjet.* 8, 153, **1935**;
- <sup>2</sup>J. W. Cahn, J. E. Hilliard, *J. Chem. Phys.* 28, 258, **1958**;
- <sup>3</sup>C. I. Poser, I. C. Sanchez, *Macromol.* 14, 361, **1981**;
- <sup>4</sup>M. P. A. Fisher, M. Wortis, *Phys. Rev. B* 29, 6252, **1984**;
- <sup>5</sup>H. Kahl, S. Enders, *Phys. Chem. Chem. Phys.* 4, 931, **2002**.



# Density gradient theory + PC-SAFT EOS

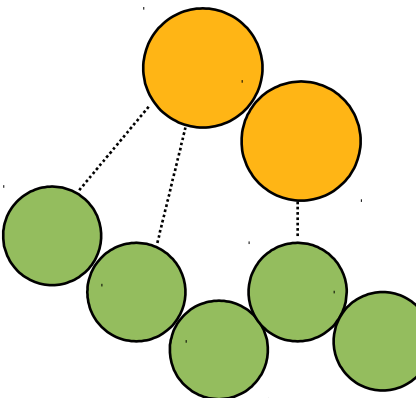


$+ \kappa (\nabla \rho)^2$



Perturbed-Chain Statistical  
Associating Fluid Theory

$$A = A^{\text{ideal}} + A^{\text{hard chain}} + A^{\text{dispersion}} + A^{\text{association}}$$



adjusted  
to model  
properties

- <sup>1</sup>L. D. Landau, E. M. Lifshitz, *Phys. Z. Sowjet.* 8, 153, **1935**;
- <sup>2</sup>J. W. Cahn, J. E. Hilliard, *J. Chem. Phys.* 28, 258, **1958**;
- <sup>3</sup>C. I. Poser, I. C. Sanchez, *Macromol.* 14, 361, **1981**;
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- <sup>5</sup>H. Kahl, S. Enders, *Phys. Chem. Chem. Phys.* 4, 931, **2002**.

<sup>6</sup>J. Gross, G. Sadowski, *Ind. Eng. Chem. Res.* 40, 1244, **2001**;

<sup>7</sup>J. Gross, G. Sadowski, *Ind. Eng. Chem. Res.* 41, 5510, **2002**.

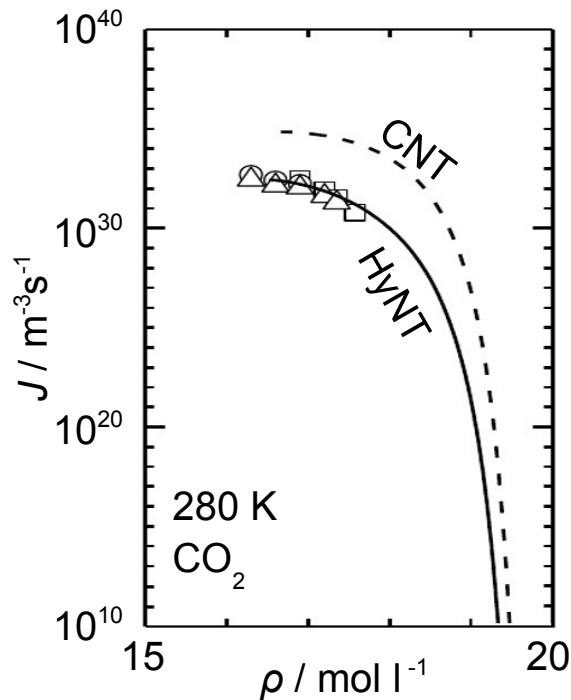


# Hybrid Nucleation Theory

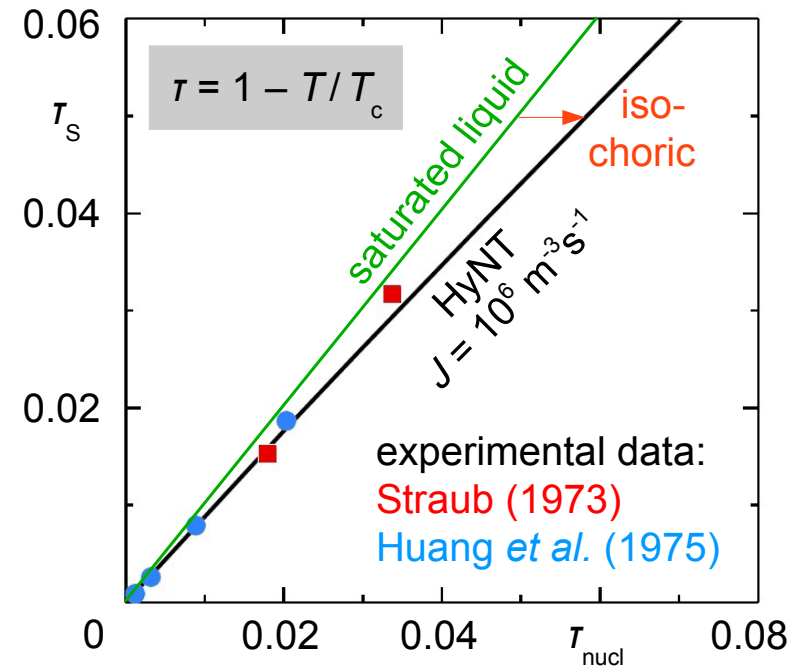
$$J = J_0 \exp\left(-\frac{\Delta A^*}{kT}\right)$$

thermodynamic factor from density gradient theory with the PC-SAFT EOS

kinetic factor from molecular dynamics



extrapolation  
by the hybrid  
nucleation theory





# Conclusion

Molecular modelling and simulation of **bubble formation by homogeneous nucleation** requires the efficient use of HPC resources by scalable MD simulation.

Here, *Is1 mardyn* was employed on over 100 000 cores to simulate **metastable liquid carbon dioxide** in systems containing up to 100 000 000 interaction sites.

The **classical nucleation theory** predicts an unphysical temperature dependence of the thermodynamic factor which determines the nucleation rate in the spinodal limit.

A **hybrid nucleation theory** was developed by combining density gradient theory and the PC-SAFT equation of state with MD simulation results.

