

AUIS ENGR 352 (Thermodynamics), Section 1, Course Assignment 5

Deadline:¹ November 23, 2017

Tutorial Discussion: November 28, 2017

- 1) A **refrigerator**² operating with the working fluid **R134a** keeps the refrigerated space at a temperature of $-35\text{ }^{\circ}\text{C}$. In the condenser of the refrigerator, heat is transferred from the working fluid to **cooling water**, which enters the condenser at $18\text{ }^{\circ}\text{C}$ and leaves it at $26\text{ }^{\circ}\text{C}$. The mass flow rate of the water is 250 g s^{-1} . R134a enters the condenser at 1.2 MPa and $50\text{ }^{\circ}\text{C}$ and leaves it at the same pressure as a liquid, with a temperature 5 K below the boiling point at that pressure. If the refrigerator has a power consumption of 3.3 kW , determine
 - (a) the mass flow rate of the working fluid;
 - (b) the cooling capacity of the refrigerator;
 - (c) the coefficient of performance;
 - (d) the minimum theoretical power input for a refrigerator operating between the same temperatures with the same cooling capacity.
- 2) Saturated **R134a vapor** at a pressure of 140 kPa enters a **compressor**,³ which operates under stationary conditions, with a mass flow rate of 106 g s^{-1} ; it leaves the compressor at a pressure of 1.4 MPa . During the compression, which is not adiabatic, heat is transferred to the surroundings at a rate of 400 W . Determine the **power input of the compressor**.
- 3) Two equal masses of **argon and nitrogen**, $m(\text{Ar}) = m(\text{N}_2) = 10\text{ g}$, which are initially separated from each other at the same temperature $T = 250\text{ K}$ and pressure $p = 40\text{ kPa}$, undergo an adiabatic and isochoric mixing process by which they combine to form an **ideal mixture of ideal gases**. Determine the **change of Helmholtz free energy** $A = U - TS$ during this process.
- 4) At steady state, a **power cycle** receives energy by heat transfer at a temperature of $463\text{ }^{\circ}\text{C}$ and discharges energy by heat transfer to a river.⁴ Upstream of the power plant, the river has a volume flow rate of $67.87\text{ m}^3\text{ s}^{-1}$ and a temperature of $20\text{ }^{\circ}\text{C}$. From environmental considerations, the river temperature (downstream of the plant) may not exceed $22\text{ }^{\circ}\text{C}$. Determine the **maximum theoretical technical power output** of the cycle under these conditions.
- 5) The **specific entropy of a pure ideal gas** is given by the differential form of the Sackur-Tetrode equation, i.e., $ds = Rv^{-1}dv + c_v T^{-1}dT$, wherein $v^{-1}dv$ can also be written as $d \ln v$ and $T^{-1}dT$ can also be written as $d \ln T$. Since it relates ds to dv and dT , this is a total differential for $s(v, T)$ as a function of v and T . However, s can be given as a function of any combination of two intensive quantities, e.g., pressure and enthalpy. Based on general relations between the properties of ideal gases, **give a total differential for $s(p, h)$** , relating ds to dp and dh .

1 Each problem contributes 0.5% to the overall grade. Submissions, individually or in groups of two, can be handed in on November 23 (after, not during the lecture), or deposited in the B-F2-01 mailbox by November 22. Note that it may be necessary to **look up thermodynamic properties** (NIST website, books, or other sources).

2 This is "Problem I" from the Selected Literature Problems, i.e., Problem 6-97 from Çengel and Boles.

3 This is "Problem L" from the Selected Literature Problems, i.e., Problem 4.45 from Moran, Shapiro, et al.

4 This is "Problem J" from the Selected Literature Problems, i.e., Problem 5.29 from Moran, Shapiro, et al.